Wind-Wave Propagation
Over Flooded, Vegetated Land

by
Frederick E. Camfield

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**Title:** Wind-Wave Propagation Over Flooded, Vegetated Land

**Author:** Frederick E. Camfield

**Abstract:** This report presents an approximate method for estimating wind-wave growth and decay over flooded areas where there is a major effect from bottom friction because of dense vegetation.
PREFACE

This report describes a method for estimating wind-wave growth and decay over flooded areas where there is a major friction effect because of dense vegetation. The report was initiated in response to a request from the U.S. Army Engineer Division, Lower Mississippi Valley, New Orleans District at the Division's 14 September 1976 Research and Development Workshop, indicating a need for technical guidelines for predicting wind-wave generation over flooded coastal areas. The work was carried out under the coastal construction program of the U.S. Army Coastal Engineering Research Center (CERC).

These technical guidelines are an extension of the procedures given in the Shore Protection Manual (SPM) (U.S. Army, Corps of Engineers, Coastal Engineering Research Center, 1975). The design curves in the SPM are limited to waves passing over a sandy bottom. A condensed description of the method is presented in CERC Coastal Engineering Technical Aid No. 77-6 (Camfield, 1977).

This report was prepared by Dr. Frederick E. Camfield, Hydraulic Engineer, under the general supervision of R.A. Jachowski, Chief, Coastal Design Criteria Branch.

Comments on this publication are invited.

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JOHN H. COUSINS
Colonel, Corps of Engineers
Commander and Director
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UNITS OF MEASUREMENT

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¹To obtain Celsius (C) temperature readings from Fahrenheit (F) readings, use formula: \( C = \left(\frac{5}{9}\right)(F - 32) \).

To obtain Kelvin (K) readings, use formula: \( K = \left(\frac{5}{9}\right)(F - 32) + 273.15 \).
SYMBOLS AND DEFINITIONS

d  water depth

d_e  water depth at seaward or beginning edge of segment

F  fetch length

F_a  adjusted fetch length for distance across a segment in the direction of wave motion

F_e  equivalent fetch length for the initial wave at seaward or beginning edge of segment

f_f  bottom-friction factor (Darcy-Weisbach friction factor)

f_f01  bottom-friction factor at seaward or beginning edge of segment

G_f  fractional growth factor at seaward or beginning edge of segment

g  gravitational acceleration

H  wave height

H_D  decayed wave height at end of fetch

H_e  equivalent wave height at end of fetch

H_f  wave height at end of fetch

H_e  wave height at seaward or beginning edge of segment

H_{i,e}  equivalent initial wave height

H_m  maximum stable wave height

H_{am}  maximum significant wave height which would be generated for given windspeed and water depth

K_f  decay factor

K_f01  decay factor when the bottom-friction factor, \( f_f = 0.01 \)

K_{f,F}  decay factor when the bottom-friction factor, \( f_f \), has a value different than 0.01

K_g  shoaling coefficient

L  wavelength

L_o  deepwater wavelength for a wave with period, \( T \)
SYMBOLS AND DEFINITIONS--Continued

\( n \)  
Manning's roughness coefficient

\( p \)  
incremental multiple of wave height

\( R_f \)  
fractional reduction of initial wave at seaward edge of segment, as compared to the maximum stable wave height

\( T \)  
wave period

\( U \)  
wind speed

\( x \)  
distance in the direction of wave motion

\( \alpha \)  
factor for reducing fetch length to the adjusted length

\( \alpha_r \)  
factor for increasing fetch length to the adjusted length = \( 1/\alpha \)

\( \Delta \)  
incremental change

\( \Delta x \)  
actual distance across a segment in the direction of wave travel
WIND-WAVE PROPAGATION OVER FLOODED, VEGETATED LAND

by
Frederick E. Camfield

I. INTRODUCTION

An important factor in the planning and design of works to protect upland property during periods of storm surge is the prediction of the wave height and period that will prevail at and seaward of the protective works (i.e., levee, dike, seawall) for a selected design storm. Although improvements are needed, guidelines are available for prediction of the water levels in upland areas resulting from storm surge; however, no guidelines are presently available for computing the wave attenuation for conditions when storm-generated waves travel a distance across shallow flooded areas where the bottom characteristics include vegetation which causes a moderate to high frictional stress. Therefore, it is necessary to estimate the heights and periods of these storm-generated waves.

Theoretical methods and field measurements are currently unavailable to provide an estimation procedure. This report presents a preliminary (approximate) method for estimating the growth or decay of waves traveling through shallow water over areas with a high frictional resistance from vegetation. The method is based on previously developed equations (U.S. Army, Corps of Engineers, Coastal Engineering Research Center, 1975) for wave growth over areas with low bottom friction, and an equation for the decay of gravity waves over areas with a constant water depth and high bottom friction. This method uses existing shallow-water wave forecasting curves by adjusting fetch lengths to account for higher bottom friction. Simplifying assumptions are used. The water depth is assumed to have only gradual variations, and the frictional resistance is treated as bottom friction. The procedure discussed in this report has not been verified in the field and may not be applicable to other problems relating frictional resistance to wave development.

Only limited data are available on the effects of high values of bottom friction on wind waves. Friction factors are estimated by comparing vegetation to similar conditions in river channels and on flood plains. The effect of the vegetation on wind stress and the possible effects of motion of the vegetation are not considered. Dense vegetation effects near the water surface which will dampen short-period waves much faster than long-period waves are also not considered. The results obtained are considered to be conservative; i.e., the predicted wave heights are expected to be slightly higher than the wave heights which actually occur.

II. WAVE FORECASTING CURVES

The Shore Protection Manual (SPM) (U.S. Army, Coastal Engineering Research Center, 1975) discusses a procedure for predicting the growth of waves over shallow water, which is a modification of a method
developed by Bretschneider (1952, 1958, 1970) and incorporates the results of Ijima and Tang (1966). The SPM method assumes that bottom friction \( f_b = 0.01 \). The significant wave height and wave period are obtained from empirical equations given as

\[
\frac{gH}{U^2} = 0.283 \tanh \left[ 0.530 \left( \frac{gd}{U^2} \right)^{0.75} \right] \tanh \left[ \frac{0.0125 \left( \frac{gf}{U^2} \right)^{0.42}}{\tanh 0.530 \left( \frac{gd}{U^2} \right)^{0.75}} \right] \tag{1}
\]

and

\[
\frac{gT}{2\pi U} = 1.20 \tanh \left[ 0.833 \left( \frac{gd}{U^2} \right)^{0.375} \right] \tanh \left[ \frac{0.077 \left( \frac{gf}{U^2} \right)^{0.25}}{\tanh 0.833 \left( \frac{gd}{U^2} \right)^{0.375}} \right] \tag{2}
\]

where

- \( H \) = significant wave height
- \( T \) = significant wave period
- \( d \) = water depth
- \( U \) = windspeed
- \( F \) = fetch length
- \( g \) = gravitational acceleration.

Since the terms are evaluated in dimensionless form, any consistent system of measurements may be used. Equations (1) and (2) are plotted as curves in Figures 1 and 2, respectively, for constant values of water depth. Design curves for predicting the growth of waves in shallow water for specified constant water depths are shown in Figures 3 to 12 (after SPM, U.S. Army, Corps of Engineers, Coastal Engineering Research Center, 1975).

### III. CALCULATION OF ADJUSTED FETCH

The long dashline in Figure 1 indicates the maximum significant wave height, \( H_{gm} \), which will occur for any given water depth and windspeed.
Figure 2. Forecasting curves for wave period (water depths constant).
Figure 5. Forecasting curves for shallow-water waves (constant depth, 5 feet).
Figure 4. Forecasting curves for shallow-water waves (constant depth, 10 feet).
Figure 5. Forecasting curves for shallow-water waves (constant depth, 15 feet).
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Figure 12. Forecasting curves for shallow-water waves (constant depth, 50 feet).
when the fetch is sufficiently long. From Figure 1, the relationship between the wave height, \( H_{am} \), and the water depth, \( d \), is given by

\[
g \frac{H_{am}}{U^2} = 0.146 \left[ \frac{g d}{U^2} \right]^{0.75}
\]

(3)

Where the bottom-friction factor \( f_f = 0.01 \), and for a given water depth and windspeed, when the initial wave height, \( H_i \), at the beginning of the fetch is less than \( H_{am} \), the wave will continue to grow in height as it travels across the fetch, with the height approaching the maximum significant wave height, \( H_{am} \). When \( H_i \) is greater than \( H_{am} \), it is assumed that the wave height will decay as the wave travels across the fetch, with the wave height again approaching the maximum significant wave height, \( H_{am} \).

Where the bottom-friction factor \( f_f > 0.01 \), i.e., vegetation increases the frictional resistance, and the initial wave height \( H_i < H_{am} \), it is assumed that the wave will grow to a final height less than or equal to \( H_{am} \), but that the growth will occur at a slower rate than where \( f_f = 0.01 \) (Fig. 13). Although the higher frictional resistance may limit the wave growth in this case to a height less than \( H_{am} \), no data are available on this effect. Therefore, as a conservative estimate, it is assumed that the maximum significant wave height will have the same value, \( H_{am} \), as where \( f_f = 0.01 \).

Where the bottom-friction factor \( f_f > 0.01 \), and the initial wave height \( H_i > H_{am} \), it is assumed that the wave will decay to a final height less than or equal to \( H_{am} \), but that the decay will occur at a greater rate than where \( f_f = 0.01 \) (Fig. 14). Although the higher frictional resistance may cause the wave to decay to a height less than \( H_{am} \), no data are presently available. Therefore, the maximum significant wave height is assumed equal to the value of \( H_{am} \) where \( f_f = 0.01 \) as before.

Where the bottom-friction factor \( f_f > 0.01 \), the fetch length is adjusted to an equivalent fetch, \( F_{eq} \), which has a bottom friction \( f_f = 0.01 \), and which will give the same growth or decay as the actual fetch with the actual bottom friction. The relationship between the adjusted fetch, \( F_{eq} \), and the actual fetch distance, \( \Delta x \), is shown in Figures 13 and 14. After the adjusted fetch, \( F_{eq} \), has been determined, Figures 1 to 12 are used to predict wave growth or decay (see Secs. IV and V).

1. Determination of Friction Factor.

Limited data are available to define friction factors for water wave motion through dense stands of marsh grass, brush, or trees. Saville (1952) presented marsh correction factors for correcting values of wave setup over flooded marsh areas. However, this was not extended to provide corrections for wave heights. Whitaker, et al. (1975) developed numerical simulations of water level changes which considered the effects
Figure 13. Wave growth.

Figure 14. Wave decay.
of vegetation in terms of drag coefficients, but effects on wave heights were not considered. Wayne (1975) investigated the decay of very low amplitude waves, from 0.126 to 0.744 foot high (0.038 to 0.227 meter), traveling short distances over grass. However, he did not establish the dependence of wave period, initial wave height, and water depth, or consider the combination of wind stress with bottom friction.

To obtain values of bottom-friction factors, estimates of Manning's roughness coefficient, \( n \), have been made using values shown in Chow (1959) for flow over flood plains. These estimated roughness coefficients are conservative; i.e., they are expected to give predicted wave heights somewhat greater than the wave heights which actually occur. The reduction in wind stress due to vegetation extending above the water surface is not considered. The roughness coefficient, \( n \), can be related to the friction factor, \( f_f \), for flow over ground by combining the Darcy-Weisbach and Manning equations for energy losses due to friction. However, the Manning equation contains a dimensional coefficient which varies depending on the dimensional units in the equation. Using a foot-pound-second system of units,

\[
f_f = \frac{3.60 \ g \ n^2}{d^{1/3}},
\]  

where \( d \) is in feet and \( g \) is in feet per second squared. (In a meter-kilogram-second system of units, the coefficient 3.60 in equation (4) becomes 8.0.)

The roughness coefficient, \( n \), will vary as a function of depth due to the height of the vegetation in relation to the depth of the water. In addition, the friction factor, \( f_f \), has an inverse relationship to the water depth, \( d \), as shown by equation (4). Values of \( f_f \) used for various kinds of ground cover are shown as curves A to D in Figure 15. Curve A is for a sandy bottom (Bretschneider, 1952, 1958, 1970), where \( f_f \) is assumed constant. This curve was used for developing the curves in Figures 1 to 12. Curve B is for coastal areas with thick stands of grass. The grass will create a high resistance at low water levels where the depth of water and the height of the grass are nearly equal, but the resistance will rapidly diminish as the water depth becomes greater than the grass height; i.e., the water particle motion under the wave is influenced less by the vegetation. Curve C is for higher levels of vegetation, such as brush or low bushy trees which extend above the height of the grass. The friction effects will be higher for curve C than for curve B because the higher vegetation will have more influence on the water particle motion for any given water depth. Curve D is for tall trees which will always be higher than the depth of water. The frictional resistance will be high at all water levels, and somewhat higher at low water levels because of the added resistance from the ground. Curve D is for a relatively close spacing of trees; e.g., a second-growth pine forest which will give the highest frictional resistance. A more scattered spacing of trees would give a lower value of \( f_f \) for a given
Figure 15. Bottom friction factors.
water depth. Chow (1959) provides values of \( n \) for a wider range of conditions.

2. Selection of Fetch Segment.

The growth or decay of a wave at any point is dependent on the water depth, the wave height and period at that point, the bottom friction, and the windspeed. For the method used here, the windspeed is assumed to be constant across a fetch. To accurately predict the growth or decay of waves traversing a particular fetch, it is necessary to divide the fetch into segments according to water depth and bottom friction. The bottom friction may vary substantially as a function of water depth for a particular type of vegetation (Fig. 15).

Figures 1 to 12 were derived for a constant depth; any variation in depth is assumed to be very gradual, and these figures are applied to an average depth across a fetch segment. Therefore, the total variation in depth across a fetch must be considered. The type of vegetation may also vary, with sections of marsh grass, brush, trees, or shallow lagoons. Wave heights will normally vary across a fetch and, as the decay factors will depend on the wave height, new decay factors must be calculated if the wave height varies excessively. A fetch segment is also considered to be much longer than a single wavelength.

Dividing the fetch into segments, the segment distance (length in the direction of wave travel) is determined so that, first,

\[
\Delta d < 0.25 \, d_f^s \tag{5}
\]

where \( \Delta d \) is the change in depth over the segment distance and \( d_f^s \) is the depth at the seaward or beginning edge of the segment; second,

\[
\Delta f_f < 0.25 \, f_f^s \tag{6}
\]

where \( \Delta f_f \) is the change in the bottom-friction factor over the segment distance and \( f_f^s \) is the friction factor at the seaward or beginning edge of the segment; and third, after the change in wave height across the segment, \( \Delta H \), has been determined,

\[
\Delta H < 0.5 \, H_f^s \tag{7}
\]

where \( H_f^s \) is the initial wave height at the seaward edge of the segment. Wave decay is also assumed to be small (less than 0.1 \( H_f^s \)) over a single wavelength. The segment distance may require adjustment; i.e., a shorter segment may be necessary if the computed value of \( \Delta H \) is unacceptable. The numerical coefficients used on the right-hand side of equations (5), (6), and (7) are arbitrarily chosen. Smaller coefficients would be expected to increase the calculations required for a solution; larger coefficients would be expected to produce a greater error in the estimated wave height obtained.
Because of the storm conditions producing the surge, it is assumed that waves will always exist at the seaward edge of the initial segment (i.e., $H_i \gg 0$), and values of wind velocity, $U$, greater than, e.g., 50 miles per hour (73 feet or 22.4 meters per second) will be expected. In case where $H_i = 0$, the methods presented here do not apply. Initial wave growth would consist of very low amplitude waves with very short periods. These initial waves will only be influenced by vegetation if the vegetation extends above the wave surface. That case has not been investigated, and cannot be treated by the method discussed in this report.

3. Adjustment of Fetch Length.

The adjusted fetch length of the segment is determined by comparing the decay factor, $K_f$, for the actual bottom friction of the segment (from Fig. 15) with the decay factor obtained for the friction factor $f_f = 0.01$ which was used for the wave predictions in Figures 1 to 12. Using the method of Bretschneider (1954) (Fig. 16), the decay factor, $K_f$, is obtained by using the two factors $f_f H_i \Delta x/d^2$ and $2\pi d/(gT^2)$, where $\Delta x$ is the actual segment distance in feet in the direction of wave motion.

The decay factor, $K_f$, was defined by Bretschneider as

$$K_f = \frac{1}{f_f H_i \Delta x \left(\frac{2\pi d}{gT^2}\right)^2 \left(\frac{16\pi K_f^2}{3(\sinh \left(\frac{2\pi d}{L}\right))^3 + 1}\right)}$$

where $K_f$ is the shoaling coefficient defined as $H/H_0$ in Table C-1 of the SPM. By noting that

$$\frac{d}{L_0} = \frac{2\pi d}{gT^2}$$

where $L_0$ is the deepwater wavelength, and $K_f$ and $\sinh (2\pi d/L)$ are functions of $d/L_0$, and therefore of $2\pi d/(gT^2)$, it can be shown that when $2\pi d/(gT^2)$ is held constant that the right-hand side of equation (8) is then a function of $f_f H_i \Delta x/d^2$ only.

Bretschneider (1954) used the work of Putnam and Johnson (1949) to define a friction factor for an impermeable sandy bottom as $f_f = 0.01$. The curves in Figures 1 to 12 were developed for that friction factor. The wave decay is proportional to $(1 - K_f)$. To compare wave decay over a fetch segment with high bottom friction to wave decay over a fetch segment where the bottom friction $f_f = 0.01$ ($H_i$, $d$, and $U$ being the same), a proportionality factor, $a$, is defined by
Figure 16. Decay factors.
\[ \alpha = \frac{(1 - K_{f, 0.01})}{(1 - K_{f_0})} \]  

where \( K_{f, 0.01} \) is the decay factor defined for \( f_f = 0.01 \) and \( K_{f_0} \) is the decay factor defined for the actual bottom friction with water depth, \( d \), initial wave height, \( H_i \), windspeed, \( U \), and segment length, \( \Delta x \), remaining the same.

For wave growth, a segment with bottom friction \( f_f > 0.01 \) would require a longer segment length for waves to grow to a given height than the length that would be required where \( f_f = 0.01 \). Therefore, the segment with greater bottom friction is equivalent to a shorter segment with \( f_f = 0.01 \). As an approximation, the shorter adjusted segment length, \( F_a \), is defined as

\[ F_a = \alpha \Delta x \]  

where \( \Delta x \) is the actual segment length (see Fig. 13).

For wave decay, a fetch segment with bottom friction \( f_f > 0.01 \) would require a shorter length for waves to decay to a given height than would be required where \( f_f = 0.01 \). Therefore, the segment with higher bottom friction is equivalent to a longer segment with \( f_f = 0.01 \) (see Fig. 14). The longer adjusted segment length, \( F_{a_0} \), in this case is defined as

\[ F_{a_0} = \alpha_n \Delta x \]  

where

\[ \alpha_n = \frac{1}{\alpha} = \frac{(1 - K_{f_0})}{(1 - K_{f, 0.01})} \]  

IV. WAVE GROWTH IN SHALLOW WATER

From Figure 1 or equation (3), for any given water depth, windspeed, and fetch length, a maximum significant wave height, \( H_{sgm} \), which would be generated can be defined. If the initial wave height, \( H_i \), at the seaward or beginning edge of the fetch segment is less than \( H_{sgm} \), it is assumed that the wave will grow to a higher height as discussed previously.

To determine the wave growth, it is necessary to first determine an equivalent fetch length, \( F_e \), for the initial wave. This is obtained directly from Figures 1 to 12 using the given windspeed and water depth. Secondly, the adjusted fetch, \( F_a \), is determined using equations (10) and (11) and Figure 16. The total fetch is then given as

\[ F = F_e + F_a \]
Re-entering Figures 1 to 12 with the fetch length, F, the windspeed, U, and water depth, d, the final wave height at the end of the fetch segment, $H_f$, is determined. This is shown schematically in Figure 17 and in the following example problem.

**EXAMPLE PROBLEM 1**

**GIVEN:** A wave passes into shallow water over a flooded coastal area. The water depth, $d_\text{f}$, at the seaward edge of the area is 23 feet (7 meters), and at the landward edge of the area the depth is 13 feet (4 meters). The distance across the area in the direction of wave motion is 10,000 feet (3,050 meters). The wave height, $H_f$, at the seaward edge of the area is limited by large sandbars seaward of the area being considered and is 3 feet (0.91 meter); the wave period is 3.2 seconds. The windspeed is 70 miles per hour (102.7 feet or 31.3 meters per second). The flooded area is covered with thick stands of tall grass.

**FIND:** The height and period of the significant wave at the landward edge of the segment.

**SOLUTION:**

\[
0.25 \ d_\text{f} = 0.25 \ (23) = 5.75 \text{ feet}
\]

\[
\Delta d = 23 - 13 = 10 \text{ feet} > 0.25 \ d_\text{f} .
\]

Since this does not meet the condition of equation (5), the area should be divided into two fetch segments. Assuming a uniform variation in depth, take the first segment as a distance $\Delta x = 5,000$ feet with a depth variation from 23 to 18 feet. Then

\[
\Delta d = 23 - 18 = 5 \text{ feet} < 0.25 \ d_\text{f} .
\]

At the 23-foot depth (from Fig. 15, curve B),

\[
f_f = 0.080
\]

and at the 18-foot depth (curve B),

\[
f_f = 0.095
\]

\[
\Delta f_f = 0.095 - 0.080 = 0.015
\]

\[
0.25 \ f_f = 0.25 \ (0.080) = 0.020
\]

\[
\Delta f_f = 0.25 \ f_f .
\]

Equations (5) and (6) are satisfied, so the fetch segment chosen is used. For a uniformly varying depth, the average depth can be taken as the average of the depths at the beginning and the end of the segment; i.e.,
Figure 17. Schematic of wave growth calculation.
\[ d = \frac{23 + 18}{2} = 20.5 \text{ feet} . \]

For a uniform type of vegetation, the friction factor will vary as a function of water depth (Fig. 15). As an approximation, the average friction factor can be taken as the average of the friction factors at the beginning and the end of the segment, i.e.,

\[ f_f = \frac{0.080 + 0.095}{2} = 0.088 . \]

For \( d = 20.5 \text{ feet}, H_L = 3 \text{ feet}, \) and \( U = 70 \text{ miles per hour from Figures 1 or 6} \)

\[ \frac{gd}{U^2} = \frac{32.2 \times 20.5}{(102.7)^2} = 0.0626 \]

\[ \frac{gH_1}{U^2} = \frac{32.2 \times 3}{(102.7)^2} = 0.00916 \]

and from Figure 1

\[ \frac{gF}{U^2} = 12.2 \]

\[ F_e = 12.2 \frac{U^2}{g} = 12.2 \frac{(102.7)^2}{32.2} = 4,000 \text{ feet} . \]

For \( f_f = 0.01, \)

\[ \frac{f_f H_L \Delta x}{d^2} = \frac{0.01 \times 3 \times 5,000}{20.5^2} = 0.357 ; \]

for \( f_f = 0.088, \)

\[ \frac{f_f H_L \Delta x}{d^2} = \frac{0.088 \times 3 \times 5,000}{20.5^2} = 3.14 . \]

For the period, \( t = 3.2 \text{ seconds, and } d = 20.5 \text{ feet,} \)

\[ \frac{2\pi d}{gT^2} = \frac{2\pi (20.5)}{32.2 (3.2)^2} = 0.391 . \]

For \( 2\pi d/(gT^2) = 0.391 \text{ (from Fig. 16)} \)
\[ K_{f_{01}} = 0.996 \text{ for } f_f = 0.01 \text{ and } f_f H_f \Delta x/d^2 = 0.357 \]

\[ K_{fa} = 0.965 \text{ for } f_f = 0.088 \text{ and } f_f H_f \Delta x/d^2 = 3.14 . \]

From equation (10),

\[ \alpha = \frac{1 - K_{f_{01}}}{1 - K_{fa}} = \frac{1 - 0.996}{1 - 0.965} = \frac{0.004}{0.035} = 0.114 ; \]

from equation (11),

\[ F_a = \alpha \Delta x = 0.114 (5,000) = 570 \text{ feet} ; \text{ and} \]

from equation (14),

\[ F = F_e + F_a = 4,000 + 570 = 4,570 \text{ feet} . \]

For \( d = 20.5 \text{ feet}, U = 70 \text{ miles per hour, and } F = 4,570 \text{ feet (from Figs. 1 and 2, or 6)} \)

\[ H_f = 3.17 \text{ feet and } T = 3.31 \text{ seconds} \]

\[ \Delta H = 3.17 - 3 = 0.17 \text{ feet} < 0.50 H_f . \]

This satisfies the requirements of equation (7), and the solution may proceed to the next segment which is the remaining 5,000 feet of the area, with the water depth varying from 18 to 13 feet, so

\[ 0.25 \Delta d = 0.25 (18) = 4.50 \text{ feet} . \]

Since \( \Delta d = 18 - 13 = 5 \text{ feet} > 0.25 \Delta d, \) which does not satisfy equation (5), a shorter segment is required. For a 3,000-foot segment, assuming a uniform depth variation, the depth will vary from 18 to 15 feet. For the 15-foot depth (using curve B in Fig. 15)

\[ f_f = 0.120 \]

\[ f_{f_2} = 0.095 \text{ at the 18-foot depth as previously shown.} \]

\[ \Delta f_f = 0.120 - 0.095 = 0.025 \approx 0.25 f_{f_2} . \]

This satisfies equation (6) and the solution may proceed. The average depth, \( d = 16.5 \text{ feet}, \) and the average friction factor, \( f_f = 0.108. \)

For \( d = 16.5 \text{ feet and } H = 3.17 \text{ feet (from Fig. 1)} \)

\[ F_e = 5,400 \text{ feet} ; \]
for $d = 16.5$ feet, $H_f = 3.17$ feet, $f_f = 0.108$, $\Delta x = 3,000$ feet, and $T = 3.31$ seconds (from Fig. 16)

$$\frac{2\pi d}{gT^2} = 0.294$$

$$K_{f0.01} = 0.988 \text{ for } f_f = 0.01 \text{ and } f_f H_f \frac{\Delta x}{d^2} = 0.349$$

$$K_{f\alpha} = 0.88 \text{ for } f_f = 0.108 \text{ and } f_f H_f \frac{\Delta x}{d^2} = 3.77$$

Using equation (10), $\alpha = 0.1$ and

$$F_\alpha = \alpha \frac{\Delta x}{2} (3,000) = 300 \text{ feet}$$

$$F = F_e + F_\alpha = 5,400 + 300 = 5,700 \text{ feet}$$

For $d = 16.5$ feet (from Figs. 1 and 2)

$$H_f = 3.27 \text{ feet and } T = 3.41 \text{ seconds}$$

The remaining 2,000 feet of the fetch can then be treated as a third segment. The average depth, $d = 14$ feet, and the average friction factor, $f_f = 0.13$.

For $d = 14$ feet and $H_f = 3.27$ feet (from Fig. 1),

$$F_e = 7,200 \text{ feet; }$$

for $d = 14$ feet, $H_f = 3.34$ feet, $f_f = 0.13$ (from Fig. 16)

$$\Delta x = 2,000 \text{ feet}, T = 3.41 \text{ seconds, and } 2\pi d/(gt^2) = 0.235$$

$$K_{f0.01} = 0.98 \text{ for } f_f = 0.01 \text{ and } f_f H_f \frac{\Delta x}{d^2} = 0.334$$

$$K_{f\alpha} = 0.80 \text{ for } f_f = 0.13 \text{ and } f_f H_f \frac{\Delta x}{d^2} = 4.34$$

Using equation (10), $\alpha = 0.1$ and

$$F_\alpha = \alpha \frac{\Delta x}{2} (2,000) = 200 \text{ feet}$$

$$F = F_e + F_\alpha = 7,200 + 200 = 7,400 \text{ feet}$$

For $d = 14$ feet, $U = 70$ miles per hour, and $F = 7,400$ feet (from Figs. 1 and 2)

$$H_f = 3.34 \text{ feet and } T = 3.51 \text{ seconds}$$

Note.--For a sandy bottom $f_f = 0.01$, the wave would have increased to a height of approximately 4.26 feet, a 42-percent increase from
the initial wave height of 3 feet. For the thick stands of tall grass, the predicted increase in wave height is only 11 percent using the approximate method of solution discussed in this report.

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V. WAVE DECAY IN SHALLOW WATER

Values of wind-generated significant wave heights and wave periods as a function of windspeed and water depth are shown in Figures 1 to 12. If the initial significant wave height at the seaward or beginning edge of a segment of fetch exceeds the maximum significant wave height for the given water depth of the segment of fetch and the given windspeed, the effects of the bottom friction may be assumed to exceed the effects of the wind stress. Therefore, the wave is assumed to decay, lose height, and over a long distance to approach a height equal to the maximum significant wave height.

The higher waves at the beginning of the fetch will actually represent a spectrum of waves. Waves of various periods could break at different points approaching the shallow-water fetch area from deep water. As shown in Figure 16, the method used here predicts that the longer period wind waves would decay faster than shorter period waves passing through the shallow water (see Fig. 18). As discussed previously, the effects of vegetation near the surface may have a strong influence on very short-period waves. However, these waves are considered to be less important for design purposes, and this influence is ignored.

![Exponential Growth of Significant Wave](image1)

Figure 18. Exponential wave growth and decay.

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As a first approximation, the wave decay may be assumed to occur exponentially at a rate similar to the rate of wave growth; i.e., the wave height will decay from a maximum stable wave height given by the shallow-water condition

\[ H_m = 0.78 d \]  

(15)

to a height equal to the maximum significant height in a distance approximately equal to the shallow-water fetch length required for a wave to grow from a zero height to the maximum generated significant wave height (the fetch length defined by the long dashlines in Fig. 1).

1. Wave Height.

The means of determining the decayed wave height is shown schematically in Figure 19. Steps to predict the decay of a wave are:

(a) Determine the maximum significant wave height that would be generated for the given windspeed and water depth, assuming an unlimited fetch, and using Figures 1 to 12 or equation (3).

(b) Determine the fractional reduction, \( R_i \), represented by the initial wave at the seaward edge of the segment of fetch under consideration given by

Figure 19. Schematic of wave decay calculations.
\[ R_c = \frac{H_m - H_c}{H_m - H_{sm}} \]  

where \( H_m \) is the maximum stable wave height given by equation (15), \( H_c \) the incident wave height at the seaward edge of the fetch segment, and \( H_{sm} \) the maximum significant wave height.

(c) Determine the equivalent initial wave height, \( H_{i,e} \), for wave growth by

\[ H_{i,e} = R_c \cdot H_{sm} \]  

(d) Determine the equivalent fetch length, \( F_e \), for the wave height, \( H_{i,e} \).

(e) Determine an adjusted fetch length, \( F_{a} \), for the segment length, \( \Delta x \), using equations (12) and (13).

(f) Determine the total fetch, \( F \), from equation (14).

(g) Determine an equivalent wave height, \( H_{e} \), for the total fetch and the given windspeed and water depth.

(h) Calculate the fractional growth by

\[ G_e = \frac{H_{e}}{H_{sm}} \]  

(i) Calculate the decayed wave height at the end of the fetch by

\[ H_D = H_m - G_e (H_m - H_{sm}) \]  

2. Wave Period.

As waves decay over the fetch segment, the significant wave period also changes. Very long waves decay rapidly; shorter waves may decay very little (see Figs. 16 and 18). This means that the significant wave period may be reduced. As a conservative estimate, it will be assumed that the wave period remains constant. This is a conservative estimate since longer period waves would produce higher runup on a structure, all other variables being the same.

* * * * * * * * * * * * * * * * example problem 2 * * * * * * * * * * * * * * * *

**GIVEN:** A coastal area is flooded by a storm surge so that the water depth over the area is 10 feet (3.05 meters). The actual fetch across the area, in the direction of wave travel, is 3,000 feet (914 meters). The area is covered with thick stands of tall grass and a small to moderate amount of brush or low bushy trees in an even distribution.
The windspeed is 90 miles per hour (132 feet or 40.2 meters per second) and the initial wave height at the seaward edge of the area of 6 feet (1.83 meters); the wave period is 4.5 seconds.

**FIND:** The decayed wave height at the end of the fetch.

**SOLUTION:** From the long dashline in Figure 1, for the windspeed of 90 miles per hour and the water depth of 10 feet

\[
\frac{gd}{U^2} = \frac{32.2 \times 10}{(132)^2} = 0.0185
\]

giving (at the intersection of the above line with the long dashline)

\[
\frac{gH}{U^2} = 0.0075
\]

so that the maximum significant wave height

\[
H_{sm} = \frac{0.0075 U^2}{g} = \frac{0.0075 \times (132)^2}{32.2} = 4.1 \text{ feet}.
\]

From equation (15),

\[
H_m = 0.78d = 0.78 \times 10 = 7.8 \text{ feet}
\]

and from equation (16), the fractional reduction is

\[
R_d = \frac{H_{m} - H_e}{H_{m} - H_{sm}} = \frac{7.8 - 6}{7.8 - 4.1} = 0.486.
\]

From equation (17), the equivalent initial wave height

\[
H_{ie} = R_d H_{sm} = 0.486 \times 4.1 = 1.99 \text{ feet}.
\]

From Figure 1, for

\[
\frac{gH}{U^2} = \frac{32.2 (1.99)}{(132)^2} = 0.00368
\]

and

\[
\frac{gd}{U^2} = 0.0185
\]

the fetch is given by

\[
\frac{gf}{U^2} = 1.4
\]
F = 760 feet for the 90-mile per hour windspeed, so that the equivalent fetch is

\[ F_e = 760 \text{ feet} \]

The vegetation does not match any of the curves in Figure 15, but falls between curves B and C. Assuming that a moderate amount of brush will give a friction effect about halfway between the two curves, from curve B, where \( d = 10 \text{ feet} \), \( f_f = 0.20 \), and from curve C, where \( d = 10 \text{ feet} \), \( f_f = 0.485 \). The bottom friction is then taken, in this case, as the average of the two values

\[ f_f = \frac{0.20 + 0.485}{2} = 0.343 \]

For \( f_f = 0.01 \),

\[ \frac{f_f H_i \Delta x}{d^2} = \frac{0.01 \times 6 \times 3000}{10^2} = 1.8 \]

for \( f_f = 0.343 \),

\[ \frac{f_f H_i \Delta x}{d^2} = \frac{0.343 \times 6 \times 3000}{10^2} = 61.7 \]

for \( T = 4.5 \text{ seconds} \) and \( d = 10 \text{ feet} \),

\[ \frac{2\pi d}{gT^2} = \frac{2\pi \times 10}{g \times (4.5)^2} = 0.096 \]

From Figure 16,

\[ K_{f,01} = 0.80 \text{ for } f_f = 0.01 \text{ and } f_f H_i \Delta x/d^2 = 1.8 \]

\[ K_{f,01} = 0.105 \text{ for } f_f = 0.343 \text{ and } f_f H_i \Delta x/d^2 = 61.7 \]

From Equation (13),

\[ \alpha = \frac{1 - K_{f,01}}{1 - K_{f,01}} = \frac{1 - 0.105}{1 - 0.80} = \frac{0.895}{0.20} = 4.48 \]

from equation (12),

\[ F_\alpha = \alpha \Delta x = 4.48 \times 3000 = 13,440 \text{ feet} \]

(i.e., the wave decay over 3,000 feet of tall grass with some brush is equal to the wave decay over 13,440 feet of a sand bottom for this water depth and windspeed).

\[ F = F_e + F_\alpha = 760 + 13,440 = 14,200 \text{ feet} \]
For a windspeed of 90 miles per hour and a fetch of 14,200 feet (from Fig. 1)

\[
\frac{g_d}{U^2} = 0.0185 \text{ (as previously determined)}
\]

\[
\frac{gF}{U^2} = \frac{32.2 \times 14,200}{(132)^2} = 26.24
\]

giving

\[
\frac{gH}{U^2} = 0.0071
\]

From which the equivalent wave height,

\[
H_e = \frac{0.0071 U^2}{g} = \frac{0.0071 (132)^2}{32.2} = 3.84 \text{ feet}
\]

From equation (18), the fractional growth is

\[
G_f = \frac{H_e}{H_{gm}} = \frac{3.84}{4.1} = 0.937
\]

The decayed wave height is then given by equation (19) as

\[
H_D = H_m - G_f (H_m - H_{gm}) = 7.8 - 0.937 (7.8 - 4.1) = 4.33 \text{ feet}
\]

At the end of the fetch segment, the wave height and period are approximated by

\[
H_D = 4.33 \text{ feet}
\]

\[
T = 4.5 \text{ seconds}
\]

VI. SUMMARY AND CONCLUSIONS

The method presented in this report gives a first approximation for estimating wave heights at the end of a fetch with a high value of bottom friction (e.g., a flooded area with dense stands of grass or brush). Only limited data are available for wave height growth or reduction for waves passing over areas with dense bottom vegetation. The method has not been verified.

A substantial amount of data is needed for waves passing over areas of flooded vegetation. The method should be verified and modified as required. The shoaling coefficients (Fig. 16) and the friction factors (Fig. 15) should also be compared with values from actual measurements.
LITERATURE CITED


Camfield, Frederick E.

42 p. : ill. (Technical paper - U.S. Coastal Engineering Research Center ; no. 77-12)
Bibliography: p. 42.
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