FA-TR-76028

STRESS ANALYSIS OF PALLET LEVER SHAFT

by

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Fee Men Lee
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March 1976

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Erratum Sheet for FA Report TR-76028 (March 1976)

TITLE: Stress Analysis of Pallet Lever Shaft

AUTHORS: Paul F. Gordon, Fee M. Lee, Ramesh Kajaria
INTRODUCTION

The effect of the load, \( F_w \), after being transferred from the pin to the shaft, consists of a force of magnitude \( F_w \) and a couple (see Fig 4, page 13). This force, \( F_w \), acts on the shaft at the center of the pallet, and its distance \( M \), from point A should be .29 in. instead of the .26 in. used in the subject report (see top of page 10). The revision in the results which this change introduces are given below.

REVISED RESULTS

1. The term \( M \) should be replaced by \( N \) in equations 9, 10, 15, 16, 21, 22, 27 and 28, and equations 11, 12, 17, 18, 23, 24, 29, 30 should be deleted.

2. The corrected stress calculations show that the maximum combined stresses (table 4 and 5) still occur at the exterior boundary points. In both phase I and II, (see table 1, page 10 and Fig 4 and 5, page 13 and 14) the maximum combined stress occurs at point D for all six cases. The value 95, 91, 89, 141, 121 and 91 ksi replace, in sequence, the values 103, 98, 93, 101, 73 and 49 ksi which were originally given (see table 4 and 5). The net result is that in phase I the maximum combined stresses decrease slightly for all three cases. In phase II the maximum combined stresses increase for all three cases.

3. All graphs showing shear force and moment diagrams in the original report should be deleted.

DISCUSSION AND CONCLUSIONS

The maximum stress found in the elastic analysis with no stress concentration factor was 141 ksi, which exceeded the 120 ksi yield stress of the shaft material. It is concluded that the shaft will fail plastically. Thus the conclusions reached on page 34 of the original report are still completely valid, and on that page the value of the maximum stress of 103 ksi is replaced by 141 ksi. In addition the maximum combined stress is now found in case 1 of phase II, rather than in case 1 of phase I, as given in the original report.
A stress analysis of the pallet lever shaft in the M125A1 Booster Runaway Assembly has been performed. The loading was such that bending and shear stress calculations in two orthogonal planes were required. Both elastic and plastic flow calculations were performed for the bending analysis. Stress concentrations due to the introduction of the "D" cut, which was machined on the originally circular section, were estimated. The mode of failure was shown to be a ductile, plastic weakening and loss of load carrying capacity.
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GLOSSARY

A - Cross section area, \( \text{in}^2 \)

\( C_X \) - Distance from the neutral axis, \( X' \), \( \text{in.} \)

\( C_Y \) - Distance from the neutral axis, \( Y' \), \( \text{in.} \)

D - Diameter of shaft, \( \text{in.} \)

d - Distance between centerline of pallet lever shaft to location where \( F_W \) acts, \( \text{in.} \)

d' - Remaining height of slotted cross section of shaft, \( \text{in.} \)

d'' - Diameter of grooved cross section of shaft, \( \text{in.} \)

\( F_C \) - Centrifugal force acting on pallet lever shaft, \( \text{lb}_f \)

\( F_W \) - External force acting on pallet lever shaft, \( \text{lb}_f \)

\( F_{CX} \) - Component of \( F_C \) acting in the \( Y \) direction, \( \text{lb}_f \)

\( F_{WX} \) - Component of \( F_W \) acting in the \( X \) direction, \( \text{lb}_f \)

\( F_{WY} \) - Component of \( F_W \) acting in the \( Y \) direction, \( \text{lb}_f \)

\( I \) - Moment of inertia, \( \text{in}^4 \)

\( I_{X'} \) - Moment of inertia acting about the neutral axis, \( X' \), \( \text{in.}^4 \)

\( I_{Y'} \) - Moment of inertia acting about the neutral axis, \( Y' \), \( \text{in.}^4 \)

\( K_{t'} \) - Stress concentration factor for bi-axial bending with Von-Mises theory of failure

\( k \) - Yield stress in simple shear, \( \text{psi} \)

L - Length of shaft, \( \text{in.} \)

M - Location from left side of shaft where \( F_W \) acts, \( \text{in.} \)

\( M_C \) - Critical moment, \( \text{in.-lb}_f \)

\( M_f \) - Upper limit of moment for failure, \( \text{in.-lb}_f \)

\( M_X \) - Internal bending moment about the X-axis, \( \text{in.-lb}_f \)

\( M_Y \) - Internal bending moment about the Y-axis, \( \text{in.-lb}_f \)

\( M_{WX} \) - Bending moment about the X-axis at the centerline of the shaft due to \( F_W \), \( \text{in.-lb}_f \)

\( M_{WY} \) - Bending moment about the Y-axis at the centerline of the shaft due to \( F_W \), \( \text{in.-lb}_f \)

N - Location from left side of shaft where \( F_C \) acts, \( \text{in.} \)
<table>
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<th>Symbol</th>
<th>Description</th>
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<tr>
<td>R</td>
<td>Radius of shaft in Figure 1, in.</td>
</tr>
<tr>
<td>R_{AX}</td>
<td>Reaction at end of shaft in the X direction, lb_f</td>
</tr>
<tr>
<td>R_{AY}</td>
<td>Reaction at end of shaft in the Y direction, lb_f</td>
</tr>
<tr>
<td>R_{DX}</td>
<td>Reaction at end of shaft in the X direction, lb_f</td>
</tr>
<tr>
<td>R_{DY}</td>
<td>Reaction at end of shaft in the Y direction, lb_f</td>
</tr>
<tr>
<td>r</td>
<td>Radius of groove in shaft, in.</td>
</tr>
<tr>
<td>r_o</td>
<td>Radius of outer fiber of shaft, in.</td>
</tr>
<tr>
<td>V</td>
<td>Shear force, lb_f</td>
</tr>
<tr>
<td>V_x</td>
<td>X component of shear force, lb_f</td>
</tr>
<tr>
<td>V_y</td>
<td>Y component of shear force, lb_f</td>
</tr>
<tr>
<td>X'</td>
<td>Coordinate as measured from neutral axis in the X direction</td>
</tr>
<tr>
<td>Y</td>
<td>Frame of reference, Y-axis</td>
</tr>
<tr>
<td>Y'</td>
<td>Coordinate as measured from neutral axis in the Y direction</td>
</tr>
<tr>
<td>z</td>
<td>Distance from left end of shaft, in.</td>
</tr>
<tr>
<td>s</td>
<td>Position of plastic interface, in.</td>
</tr>
<tr>
<td>\theta</td>
<td>Angle F_W makes with Y-axis, degree</td>
</tr>
<tr>
<td>\phi</td>
<td>Angle F_C makes with X-axis, degree</td>
</tr>
<tr>
<td>\sigma</td>
<td>Normal stress, psi</td>
</tr>
<tr>
<td>\sigma_1</td>
<td>Bending stress in the Z direction produced by the bending moment about the X-axis, M_X, psi</td>
</tr>
<tr>
<td>\sigma_a</td>
<td>Bending stress in the Z direction produced by the bending moment about the Y-axis, M_Y, psi</td>
</tr>
<tr>
<td>\sigma_{mm}</td>
<td>Combined bending stress of \sigma_1 and \sigma_2, psi</td>
</tr>
<tr>
<td>\sigma_y</td>
<td>Tensile yield strength, psi</td>
</tr>
<tr>
<td>\tau_x</td>
<td>Shear stress, psi</td>
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INTRODUCTION

The work described in this report was performed under D.A. (Fuze) Project GG46106, the M125A1 Booster Program. The objective of this program was to provide engineering support during production of the M125A1 booster runaway escape mechanism. This task dealt with production line failures of the pallet lever shaft of that mechanism. The stress analysis performed under that task in support of the failure analysis is presented in this report.

The function of the pallet lever assembly, Figure 1, is to delay the arming of the M125A1 Booster, Figure 2, until the fuze is a safe distance away from launch. A previous mechanism modification described in Tech report FA-TR-74045\(^1\) necessitated the use of a pallet shaft containing a "D" cut to insure adequate escapewheel clearance in addition to an efficient torque exchange at the escapewheel-pallet contact point. The structural integrity of the shaft design which resulted was questioned when premature arming of the M125A1 Booster was observed in lot acceptance testing with the 90 mm M41 Gun. The spin environment produced by this weapon is nominally 19,500 rpm and results in a high centrifugal loading on all mechanism components. This also results in a high applied torque on the unbalanced rotor gear which powers the mechanism. This torque is reduced and transmitted to the pallet lever exerting additional force on the pallet shaft.

The magnitude of forces used as input to this stress analysis reflect this 19,500 rpm spin environment, with the rotor gear taken in a maximum output orientation. No gear train losses were assumed anywhere in the device in computing the force applied by the escapewheel on the pallet lever. Since the pallet lever can assume a wide range or orientations with respect to the centrifugal force field, four positions which span the extremes of both entrance and exit engagement positions are analyzed. It was concluded as a result of this study that the pallet lever shaft was on the verge of excessive ductile, plastic bending. The acceptance lot testing failures exhibited the predicted failure mode.

ANALYSIS

Loads and Reactions on the Shaft

The purpose of the analysis is to determine the normal and shearing stresses in the shaft. However, it is necessary first to determine the loads and reactions which generate the stress system.

The right circular beam under consideration is shown in Figures 1 and 3, together with the prescribed loads. The two separate loading conditions for the placement of \( F_W \) are called Phase I (Figure 1) and Phase II (Figure 3). As can be noted,
Figure 1. Pallet Lever Assembly (Prescribed Loads for Phase I.)
Figure 3. Pallet Lever Assembly (Prescribed Load for Phase II.)
the only difference in the nature of the loading between Phase I and II is the pin and inclination on which $F_W$ acts. Within each phase are three possible values of the loads and inclinations. These three possibilities are identified as cases 2 or 3. The beam was loaded in each phase by two forces: an external force, $F_W$, and a centrifugal force, $F_C$. The dimensions $M$, $N$, and $L$ have values of .26 in., .28 in., and .39 in., respectively. Both forces $F_W$ and $F_C$ act in the X-Y plane at inclinations of $\theta$ and $\phi$ with respect to the Y-axis and X-axis, respectively, and are normal to the Z-axis. Numerical values for the loads and angles are found in Table 1. The external force, $F_W$, as shown acts on the pin, thus in addition to the usual shear loading, it also contributes a concentrated bending moment to the shaft about the Z-axis at the centerline of the pallet.

For ease in presentation, the components of each force and bending moment in the X-Z and Y-Z planes are illustrated in Figures 4 and 5. Numerical values are listed in Table 2. The reactions $(R_{AX}, R_{AY}, R_{DX}, \text{ and } R_{DY})$ were found by demanding static equilibrium in the shaft. The following expressions resulted:

<table>
<thead>
<tr>
<th>Case</th>
<th>$F_W$, lb</th>
<th>$\theta$, degrees</th>
<th>$F_C$, lb</th>
<th>$\theta$, degrees</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>5.78</td>
<td>17</td>
<td>7.4</td>
<td>22</td>
</tr>
<tr>
<td>2</td>
<td>4.78</td>
<td>16</td>
<td>7.4</td>
<td>15</td>
</tr>
<tr>
<td>3</td>
<td>3.49</td>
<td>18</td>
<td>7.4</td>
<td>5.5</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Case</th>
<th>$F_W$, lb</th>
<th>$\theta$, degrees</th>
<th>$F_C$, lb</th>
<th>$\theta$, degrees</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>5.69</td>
<td>30</td>
<td>7.4</td>
<td>-10</td>
</tr>
<tr>
<td>2</td>
<td>4.67</td>
<td>39.5</td>
<td>7.4</td>
<td>-5.5</td>
</tr>
<tr>
<td>3</td>
<td>3.61</td>
<td>56</td>
<td>7.4</td>
<td>+4</td>
</tr>
</tbody>
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Table 2. X and Y Components of $F_W$ and $F_C$

<table>
<thead>
<tr>
<th>Case</th>
<th>$F_{WY}$ lb</th>
<th>$F_{CY}$ lb</th>
<th>$F_{WX}$ lb</th>
<th>$F_{CX}$ lb</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>5.27</td>
<td>2.77</td>
<td>1.69</td>
<td>6.86</td>
</tr>
<tr>
<td>2</td>
<td>4.59</td>
<td>1.98</td>
<td>1.32</td>
<td>7.13</td>
</tr>
<tr>
<td>3</td>
<td>3.32</td>
<td>.71</td>
<td>1.08</td>
<td>7.37</td>
</tr>
</tbody>
</table>

Phase I:

\[
R_{DX} = \frac{(F_{CXN} + F_{WXM} - F_{WXd})}{L} \quad (1)
\]

\[
R_{AX} = F_{WX} + F_{CX} - \left[ \frac{(F_{CXN} + F_{WXM} - F_{WXd})}{L} \right] \quad (2)
\]

\[
R_{DY} = \frac{(F_{WYM} - F_{CYN} - F_{WYd})}{L} \quad (3)
\]

\[
R_{AY} = F_{WY} - F_{CY} - \left[ \frac{(F_{WYM} - F_{CYN} - F_{WYd})}{L} \right] \quad (4)
\]

Phase II:

\[
R_{DX} = \frac{(F_{WXM} + F_{CYN} - F_{WXd})}{L} \quad (5)
\]

\[
R_{AX} = F_{WX} + F_{CY} - \left[ \frac{(F_{WXM} + F_{CYN} - F_{WXd})}{L} \right] \quad (6)
\]

\[
R_{DY} = \frac{(F_{WYM} - F_{CYN} - F_{WYd})}{L} \quad (7)
\]

\[
R_{AY} = F_{WY} - F_{CY} - \left[ \frac{(F_{WYM} - F_{CYN} - F_{WYd})}{L} \right] \quad (8)
\]
Tables 1 and 2 and Figures 1, 3, 4 completely define the system of prescribed loads and resulting reactions. Subsequently, a stress and failure analysis, presented below, was performed using these loads.

The results of this study include (a) an elastic stress analysis, and (b) a plastic stress and failure analysis. The first step in both analyses was the determination of the shear and bending moment diagrams.

Shear and Moment Diagrams

The shear force and bending moment were found to be for Phase I, (Figure 4):

X Component:

\[
\begin{align*}
O<Z<M & : V_X = -R_{AX} & (9) \\
M<Z<N & : V_X = F_{WX} - R_{AX} & (11) \\
N<Z<L & : V_X = F_{CX} + F_{WX} - R_{AX} & (13)
\end{align*}
\]

\[
\begin{align*}
M_Y &= R_{AX}Z - F_{WX}(Z - M) - F_{CX}(Z - N) - M_{WX} & (14)
\end{align*}
\]

Y Component:

\[
\begin{align*}
O<Z<M & : V_Y = R_{AY} & (15) \\
M<Z<N & : V_Y = R_{AY} - F_{WY} & (17) \\
N<Z<L & : V_Y = R_{AY} - F_{WY} + F_{CY} & (19)
\end{align*}
\]

\[
\begin{align*}
M_X &= -R_{AY}Z + F_{WY}(Z - M) & (18) \\
M_X &= -R_{AY}Z + F_{WY}(Z - M) - F_{CY}(Z - N) + M_{WY} & (20)
\end{align*}
\]

For Phase II (Figure 5), the internal shearing force and bending moment were found to be:

X Component:

\[
\begin{align*}
O<Z<M & : V_X = -R_{AX} & (21) \\
M_Y &= R_{AX}Z & (22)
\end{align*}
\]
Figure 4. Loads and Reaction of Phase I: (a) Top View and (b) Side View. T and C Denote Regions of Tension and Compression, Respectively.
Figure 5. Loads and Reactions for Phase II: (a) Top View and (b) Side View. T and C Denote Regions of Tension and Compression, Respectively.
\[
\begin{align*}
M < Z < N & \quad V_X = F_{WX} - R_{AX} \quad (23) \\
& \quad M_Y = R_{AX}Z - F_{WX}(Z - M) \quad (24) \\
N < Z < L & \quad V_X = F_{WX} + F_{CX} - R_{AX} \quad (25) \\
& \quad M_Y = R_{AX}Z - F_{WX}(Z - M) - F_{CX}(Z - N) - M_{WY} \quad (26)
\end{align*}
\]

\[
\begin{align*}
Y \text{ Component:} \\
0 < Z < M & \quad V_Y = R_{AY} \quad (27) \\
& \quad M_X = -R_{AY}Z \quad (28) \\
M < Z < N & \quad V_Y = R_{AY} - F_{WY} \quad (29) \\
& \quad M_X = -R_{AY}Z + F_{WX}(Z - M) \quad (30) \\
N < Z < L & \quad V_Y = R_{AY} - F_{WY} + R_{CY} \quad (31) \\
& \quad M_X = -R_{AY}Z + F_{WX}(Z - M) - F_{CY}(Z - N) - M_{WX} \quad (32)
\end{align*}
\]

Due to the loading and reduced area at the "D" section, the maximum stress and failure occur in the "D" section. Attention was therefore restricted to this "D" section, namely, from \( Z = .199 \) in. to \( Z = .279 \) in. Using the equations given above, numerical values of \( V_X, V_Y, M_X, \) and \( M_Y \) were calculated as shown in Table 3 and plotted in Figures 6 to 17. From this table and these figures, the point where the maximum moments occur are \( Z = .239" \) (Phase I) and \( Z = .279" \) (Phase II). Failure, if it occurs, would occur at these points. Therefore, it is these locations on the shaft which are used in the subsequent computation of the bending stresses.

**Unsymmetric Bending**

It follows from the above load analysis that the problem of stress analysis is essentially that of a shaft subjected simultaneously to bending and shear in two planes. The two planes in question are the X-Z and Y-Z planes of Figures 4 and 5.

The approach in the elastic analysis was to consider each of the bending planes separately, and then to combine their effects. \( M_X \) acting alone, will produce a bending stress, \( \sigma_1 \), acting on and normal to the cross-sectional area as shown in Figure 18. \( M_Y \) will produce a bending stress, \( \sigma_2 \) which acts on and is normal to the cross section. As seen in Figure 18, \( \sigma_2 \) is a linear function only of \( X' \) and is independent of \( Y' \). Also, \( \sigma_1 \) is a linear function of \( Y' \) and is independent of \( X' \). The appropriate equations are then:

\[
\begin{align*}
\sigma_1 &= \sigma_1(Y') = \left(\frac{M_X}{I_{XY}}\right) Y' \quad (33) \\
\sigma_2 &= \sigma_2(X') = \left(\frac{M_Y}{I_{X'y}}\right) X' \quad (34)
\end{align*}
\]
Table 3. X and Y Components of Shearing Forces and Bending Moments in Slotted Section

<table>
<thead>
<tr>
<th>Case</th>
<th>Z, in</th>
<th>$V_x$, lb</th>
<th>$V_y$, lb</th>
<th>$M_x$, in-lb</th>
<th>$M_y$, in-lb</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>.199</td>
<td>2.635</td>
<td>-.1489</td>
<td>-.296</td>
<td>.524</td>
</tr>
<tr>
<td></td>
<td>.239</td>
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Figure 6. Shear Diagram for Phase I, Case 1.
\( V_X \) = Shear Force in the X Direction
\( V_Y \) = Shear Force in the Y Direction

Figure 7. Shear Diagram for Phase I, Case 2.
\( V_X \) = Shear Force in the X Direction
\( V_Y \) = Shear Force in the Y Direction.
Figure 8. Shear Diagram for Phase I, Case 3.
\( V_X \) = Shear Force in the X Direction
\( V_Y \) = Shear Force in the Y Direction

Figure 9. Shear Diagram for Phase II, Case 1.
\( V_X \) = Shear Force in the X Direction.
\( V_Y \) = Shear Force in the Y Direction.
Figure 10. Shear Diagram for Phase II, Case 2.
\( V_X \) = Shear Force in the X Direction.
\( V_Y \) = Shear Force in the Y Direction.

Figure 11. Shear Diagram for Phase II, Case 3.
\( V_X \) = Shear Force in the X Direction.
\( V_Y \) = Shear Force in the Y Direction.
Figure 12. Moment Diagram for Phase I, Case 1.
\[ M_X \] = Moment about the X Neutral Axis.
\[ M_Y \] = Moment about the Y Neutral Axis.

Figure 13. Moment Diagram for Phase I, Case 2.
\[ M_X \] = Moment about the X Neutral Axis.
\[ M_Y \] = Moment about the Y Neutral Axis.
Figure 14. Moment Diagram for Phase I, Case 3.

\[ M_X = \text{Moment about the X Neutral Axis.} \]
\[ M_Y = \text{Moment about the Y Neutral Axis.} \]

Figure 15. Moment Diagram for Phase II, Case 1.

\[ M_X = \text{Moment about the X Neutral Axis.} \]
\[ M_Y = \text{Moment about the Y Neutral Axis.} \]
Figure 16. Moment Diagram for Phase II, Case 2.
\[ M_X = \text{Moment about the X Neutral Axis.} \]
\[ M_Y = \text{Moment about the Y Neutral Axis.} \]

Figure 17. Moment Diagram for Phase II, Case 3.
\[ M_X = \text{Moment about the X Neutral Axis.} \]
\[ M_Y = \text{Moment about the Y Neutral Axis.} \]
Figure 18. Individual States of Stress: (a) Stress Due to $M_X$ and (b) Stress Due to $M_Y$. 

\( \sigma_1 = \text{CONST. ACROSS IN THE X}^1 \text{DIR.} \)
I_{X'} is the moment of inertia about the neutral axis X', I_{Y'} is the moment of inertia about the neutral axis Y'. With respect to the drawings: 1. Y' is symmetrically located on the section. 2. the X' axis is defined by the dimensions C_1 and C_2 which have values of C_1 = .424 R, C_2 = .576 R. 3. I_{X'} has a value of 0.11 R^4. 4. I_{Y'} was calculated from the definition:

\[ I_{Y'} = \int_A x^2 \, dA \]  

(35)

which resulted in

\[ I_{Y'} = \frac{\pi R^4}{8} \]  

(36)

The total stress is the sum of the individual components, \( \sigma_1 \) and \( \sigma_2 \). Examination of Figure 18 and Equations 33 and 34 show that the total loading, \( \sigma_{\text{nom}} \), will result in a complex stress distribution. This is indicated, schematically, in Figure 19. Figure 19 shows the sum of the two distributions. The stress \( \sigma_1 \) about the X' axis caused a tensile (T) and compressive (C) region. The stress \( \sigma_2 \) about the Y' axis also causes tensile and compressive regions. Upon addition, the four regions can be identified CC, CT, TC, and TT. The symbols denote the contribution from each stress. For example CC denotes that in Region 1 both \( \sigma_1 \) and \( \sigma_2 \) were compressive.

Tables 4 and 5 contain the numerical values of the total stress distribution, \( \sigma_1 + \sigma_2 \), for a large number of interior and boundary points which are identified in Figure 20. Both interior and exterior points were examined for each loading case within each Phase. For all six loading conditions the tables show clearly that:

1. The maximum compressive stress always occurred at point D.
2. The maximum tensile stress was at either point J or M. Note that the maximum stress occurs always at the boundary rather than at the interior. This is intuitively reasonable since it parallels the simpler uni-plane bending of elementary beam theory.
3. The maximum stress occurs in Phase I, case 1, it is compressive, and has a value of 103 ksi. Maxima for all other cases are underlined. The influence of the shear stress on the total stress distribution was considered. The shear stress, \( \tau_{X'Y'} \), is given approximately by

\[ \tau \approx \frac{V}{A} \]  

(37)

where V is the shear force and A the cross sectional area. Table 6 presents these stresses for both (X and Y) components of the shear force. The values of V were taken from Table 3. As can be seen, the maximum shear stress is of the order of 3 ksi and is negligible compared to the bending stresses.

**Plastic Flow and Failure**

Consider the circular beam of Figure 21. The Von-Mises criterion for incipient flow is:

\[ \sigma^2 + 3 \tau^2 = 3k^2 \]  

(37)

where \( \sigma \) is the normal stress, \( \tau \) the shear stress and \( k \) is the yield stress in simple shear.
Figure 19. Combined States of Stress.

a - Bending in the Y-Z Plane.
b - Bending in the X-Z Plane
c - Equivalent Bending Effect of b and c.
Table 4. Combined Bending Stress at Different Points of Cross Section for Phase I

<table>
<thead>
<tr>
<th>Interior Points</th>
<th>Combined Stress ksi</th>
<th>Exterior Points</th>
<th>Combined Stress ksi</th>
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<tr>
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<td>Case 1  2  3</td>
<td></td>
<td>Case 1  2  3</td>
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<tr>
<td>11</td>
<td>25    24  23</td>
<td>A</td>
<td>61    56  51</td>
</tr>
<tr>
<td>12</td>
<td>36    34  31</td>
<td>B</td>
<td>76    71  65</td>
</tr>
<tr>
<td>13</td>
<td>46    43  39</td>
<td>C</td>
<td>90    86  80</td>
</tr>
<tr>
<td>21</td>
<td>40    39  37</td>
<td>D</td>
<td>103   98  93</td>
</tr>
<tr>
<td>22</td>
<td>51    48  46</td>
<td></td>
<td>89    85  81</td>
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<tr>
<td>23</td>
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<td>77    75  72</td>
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<td></td>
<td>52    52  52</td>
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<td>33</td>
<td>76    72  68</td>
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<td>-     -  -</td>
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<tr>
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<td>67    64  62</td>
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<tr>
<td>84</td>
<td>61    59  68</td>
<td></td>
<td>52    52  51</td>
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</table>
Table 5. Combined Stress at Different Points of Cross Section for Phase II

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<th>Points</th>
<th>Combined Stress ksi</th>
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<td>38 29 17</td>
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<td>83 63 36</td>
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<td>13</td>
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<td>C</td>
<td>87 68 43</td>
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<tr>
<td>84</td>
<td>50 44 29</td>
<td>P</td>
<td>16 19 26</td>
</tr>
</tbody>
</table>
Figure 20. Locations of Points used in Calculations

\[
\begin{align*}
X_1^I &= .008 \text{ IN.} \\
X_2^I &= .016 \text{ IN.} \\
X_3^I &= .024 \text{ IN.} \\
X_4^I &= .004 \text{ IN.} \\
X_5^I &= .008 \text{ IN.} \\
X_6^I &= .012 \text{ IN.} \\
X_7^I &= .016 \text{ IN.} \\
X_8^I &= .020 \text{ IN.} \\
X_9^I &= .024 \text{ IN.} \\
Y_1^I &= .003 \text{ IN.} \\
Y_2^I &= .006 \text{ IN.} \\
Y_3^I &= .009 \text{ IN.} \\
Y_4^I &= .007 \text{ IN.} \\
Y_5^I &= .014 \text{ IN.} \\
Y_6^I &= .016 \text{ IN.}
\end{align*}
\]
Table 6. Maximum Average Shearing Stress in the Flat Section

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<th>$T_{XY_2}$, psi</th>
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<td>1272</td>
</tr>
<tr>
<td>3</td>
<td>1070</td>
<td>884</td>
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</table>

$T_{XY_1} = $ Shear stress due to X component of shear force.

$T_{XY_2} = $ Shear stress due to Y component of shear force.
Figure 21. State of Stress
Since the shear stress is much smaller than the normal stress, i.e.,

$$|\tau| \ll |\sigma|$$  \hspace{1cm} (38)

the yield condition, Equation 37 is:

$$\sigma = \pm k \cdot \sqrt{3}$$  \hspace{1cm} (39)

To establish conditions incipient for flow one must consider the elastic behavior just before plasticity commences.

The relation between stress and bending moment for an elastic beam is:

$$\sigma = \frac{M}{X/I}$$  \hspace{1cm} (40)

Since $\frac{M}{I}$ is a constant at a particular section, it follows from Equation 40 that elastic stress is a maximum at the outer fibers. Thus plasticity commences there first.

Thus, using Equations 39 and 40, the critical moment, $M_C$, at which plasticity begins at the outer fiber is:

$$M_C = \sqrt{3}k \frac{I}{r_o}$$  \hspace{1cm} (41)

For moments smaller than $M_C$ the beam is elastic and, disregarding the question of stress concentration, does not fail. It is important to note that $M_C$ is a property inherent to the beam since its value depends only on material and geometric constants.

The value of the shear yield, $k$, is most conservatively related to the Tresca criterion as:

$$k = \frac{1}{2} \sigma_Y$$  \hspace{1cm} (42)

where $\sigma_Y$ is the tensile yield strength of the metal.

Thus the critical moment is:

$$M_C = \left( \sqrt{3}/2 \right) \sigma_Y \frac{I}{r_o} = 0.87 \sigma_Y \frac{I}{r_o}$$  \hspace{1cm} (43)

and since:

$$I = \pi r_0^4/4$$  \hspace{1cm} (44)

$$M_C \approx 0.68 r_0^3 \sigma_Y$$  \hspace{1cm} (45)

It is important to note that while $M_C$ causes plastic flow in the outer fibers, the remainder of the beam is elastic.
Failure occurs when the moment exceeds the critical value by an amount to make part of the crosssection plastic. An upper limit on this value, $M_f$, is found in the analysis below.

Consider the section shown in Figure 21. Plasticity commences, as noted above, when $|\xi| = r_o$, at the outer fibers. As $M$ is increased, more of the beam becomes plastic. This occurs as $|\xi|$ decreases. When $\xi = 0$, and the section is entirely plastic, the beam is permanently deformed and therefore failed.

The state of stress for each region of the beam section is:

\[ \sigma = k \sqrt{3} \quad \text{for} \quad -r_o \leq Z \leq -\xi \]
\[ \sigma = kZ \sqrt{3}/\xi \quad \text{for} \quad -\xi \leq Z \leq \xi \] \hspace{1cm} (46)
\[ \sigma = k \sqrt{3} \quad \text{for} \quad \xi \leq Z \leq r_o \]

By definition the moment caused by the stress system, Equation 46 is:

\[ M = \int_{-r_o}^{r_o} \sigma (Z) Z \, dA = M (\xi) \] \hspace{1cm} (47)

where $dA$ is an area element. Noting the symmetry of deformation about the $Y$-axis, Equation 47 is:

\[ M = 2 \int_{r_\xi}^{r_o} \sigma (Z) Z \, dA + 2 \int_{0}^{\xi} \sigma (Z) Z \, dA, \] \hspace{1cm} (48)

recalling that:

\[ dA = 2 \left( r_o^2 - Z^2 \right)^{1/2} \, dZ, \] \hspace{1cm} (49)

and also the values of $\sigma (Z)$ given by Equation 46, the final integrated result is:

\[ M (\xi)/2 = (2/3) k \sqrt{3} \left[ r_o^2 - \xi^2 \right]^{3/2} \bigg[ + Z k \sqrt{3} \left[ - (r_o^2 - \xi^2)^{3/2}/4 + r_o^2 (r_o^2 - \xi^2)^{1/2}/8 + (50) \right.

\[ + (r_o^4/8 \xi^2) \sin^{-1} (\xi/r_o) \right] \bigg] \]

The value of $M_f$, an upper limit to the moment which causes complete failure, is obtained by allowing $\xi$ to approach zero in Equation 50. The result is:

\[ M_f = 1.155 \sigma_Y r_o^3 \] \hspace{1cm} (51)
Comparing this value to $M_c$ in Equation 45 it is seen that, theoretically, when $M_c$ is exceeded by about 70%, the beam is completely failed. In the present application, however, where virtually no plastic flow and permanent deflection are permitted, this factor of 70% beyond $M_c$ is too great for design allowance. Also, the real cross-section is a half circle and not a complete circle as assumed. While a value for $M_f$ for a half-circle has not been attempted, it is obvious that $M_f$ will certainly not be greater than $M_c$. 
DISCUSSION AND CONCLUSION

The maximum stress found in the elastic analysis with no stress concentration factor was 103 ksi. The yield stress of the beam material is 120 ksi. The right angle formed by the machined flat will introduce a stress concentration factor. Since any stress concentration factors will elevate the stress to well beyond 120 ksi, which is the yield strength of the material, it is concluded that the beam is on the verge of ductile, plastic failure.
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