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ATMOSPHERIC EFFECTS FOR GROUND TARGET
SIGNATURE MODELING

I. Atmospheric Transmission at 1.06 Micrometers

By

Richard B. Gomez

June 1972

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# Atmospheric Effects for Ground Target Signature Modeling

## I. Atmospheric Transmission at 1.06 Micrometers

### 1. Literature Search and Theoretical Analysis

The results of a literature search and subsequent theoretical analysis conducted to determine the characteristics of atmospheric transmission at 1.06 micrometers wavelength are presented. The effects of molecular scattering, molecular absorption, aerosol scattering, and aerosol absorption are considered. Atmospheric transmission at 1.54 micrometers is compared with the transmission at 1.06 micrometers. In addition, problem areas which must be resolved to enable one to make adequate transmission predictions are brought out in this report. It is concluded that aerosol scattering is the primary attenuating mechanism on 1.06 micrometers radiation; for all practical purposes, losses due to molecular absorption, molecular scattering, and aerosol absorption seem small and negligible compared to the loss due to aerosol scattering. For horizontal paths at sea level with good visibility (>10 km) the total extinction coefficient lies in the range of $2 \times 10^{-2}$ to $2 \times 10^{-1}$ km$^{-1}$. Attenuation due to rain over short paths (<5 km) and for rain rates less than 10 mm/hr is not severe; however, cloud, fog, and haze will have a considerable effect on the transmission. Atmospheric transmission at 1.06 μm and 1.54 μm is higher than at most of the other laser wavelengths available; however, spectral measurements are not currently available with high enough resolution to decide which of these two wavelengths has a higher transmission.
<table>
<thead>
<tr>
<th>KEY WORDS</th>
<th>LINK A</th>
<th>LINK B</th>
<th>LINK C</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>ROLE</td>
<td>WT</td>
<td>ROLE</td>
</tr>
<tr>
<td>1. Optics</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2. Electromagnetics</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3. Lasers</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4. Transmittance</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5. Attenuation</td>
<td></td>
<td></td>
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Technical Report ECOM-5445

ATMOSPHERIC EFFECTS FOR GROUND TARGET SIGNATURE MODELING

1. Atmospheric Transmission at 1.06 Micrometers

By

Richard B. Gomez

Atmospheric Sciences Laboratory
White Sands Missile Range, New Mexico

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U. S. Army Electronics Command
Fort Monmouth, New Jersey
6. Atmospheric absorption lines between 10,532.2Å and 10,585.1Å
(from reference [49]) .................................................. 20
7. Atmospheric absorption lines between 10,585.1Å and 10,627.6Å
(from reference [49]) .................................................. 21
8. Atmospheric absorption lines between 10,627.6Å and 10,661.0Å
(from reference [49]) .................................................. 22
9. Atmospheric absorption lines between 10,661.0Å and 10,707.4Å
(from reference [49]) .................................................. 23
10. Scattering coefficients and optical densities for the case of haze (from reference [63]) ....................... 28
11. Scattering coefficients and optical densities for the case of fog (from reference [63]) ....................... 30
12. Rainfall rate (mm/hr) versus attenuation (dB/km) .................. 33
13. Atmospheric transmission spectra obtained by Taylor and Yates (from reference [51]) ....................... 36

TABLES

I. Molecular scattering coefficients reported by McClatchey et al. [17] for 1.06 μm wavelength for five different atmospheric models .................................................. 16
II. Extinction coefficients versus wavelength for eight specific cloud types (from reference [70]) .................. 31
III. Magnitudes of atmospheric effects at 1.06 μm .................. 39
I. INTRODUCTION

This is the first of a series of reports to be prepared in support of the atmospheric modeling portion of a comprehensive Ground Target Signature (GTS) modeling program. The aim of the atmospheric modeling project is to develop the capability of predicting atmospheric effects on ground target signatures for a wide range of meteorological conditions. Accomplishment of this objective will provide the information required for the design and operation of terminal homing, target acquisition, and surveillance systems. It will also influence the choice of operating wavelengths for artificial sources used in conjunction with these systems [1]. Moreover, it will provide the knowledge needed to discriminate between target and environmental effects [1].

The neodymium (Nd\(^{3+}\)) laser wavelength of 1.06 \(\mu\)m was chosen for this initial investigation because the Nd\(^{3+}\) laser is currently being employed in laser guided terminal homing missile systems [2]. The purpose of this report is to present the results of a literature search (through January 1972) and theoretical analysis conducted to determine the characteristics of atmospheric transmission at the 1.06 \(\mu\)m wavelength. The last literature survey on the subject was conducted by Roy and Emmons [3] in 1965, but analysis of atmosphere effects on the propagation of 1.06 \(\mu\)m Nd\(^{3+}\) laser radiation has been treated more recently [4-6].

Results of experimental and theoretical transmission studies by various investigators are used to estimate the transmission characteristics for 1.06 \(\mu\)m radiation. The atmospheric effects of molecular and aerosol scattering and absorption are treated. Other effects, such as turbulence, multiple scattering, nonlinearity, and quantum mechanical corrections are neglected, although under certain experimental conditions these effects may be significant (e.g., transmission through a heavy cloud layer where multiple scattering becomes significant or high beam intensity where nonlinear effects are important). Transmittance models which include some of these effects at various wavelengths including 1.06 \(\mu\)m will be treated in subsequent reports in this series.

Section 2 is a discussion of Nd\(^{3+}\) laser emission and a quantitative description of atmospheric effects on laser radiation. Problem areas which need to be resolved to enable one to make reliable transmission predictions are brought out in this section.

Section 3 is a discussion and analysis of the results of both experimental and theoretical transmission studies made by various investigators in the region of interest.

Section 4 is a comparison between atmospheric transmission at 1.06 \(\mu\)m and 1.54 \(\mu\)m, since transmission at these two wavelengths is higher than at most other laser wavelengths available [6].
Section 5 is a summary of the report, includes some concluding remarks, and provides the results of Section 3 in tabular form.

2. BACKGROUND

2.1 Neodymium Laser Emission Spectral Characteristics

Neodymium (Nd) lasers are receiving much attention for use in atmospheric laser systems because of their emission spectral characteristics that lie in a region for which the atmosphere is relatively transparent, and because they can be operated at ambient temperature with high efficiency. The trivalent neodymium ion (Nd$^{3+}$) is the active entity of these lasers that operate at or near 1.06 µm wavelength, with some finite linewidth. In describing their spectral characteristics, it is necessary to differentiate between the gross and fine structure of the emission bands [7]. The gross structure of the emission bands (the generation wavelength) is dependent on the host material and on the concentration of the doping material [8]. The fine structure of the emission bands is mainly dependent on the resonator properties and on the width and character of the luminescence line broadening [7]. The important types of neodymium lasers commonly being used in atmospheric laser systems are Nd:YAG and Nd:glass. These two lasers are briefly discussed below.

An Nd:YAG laser requires relatively low threshold pumping power and can be operated in either a continuous wave (CW) or pulsed mode with reasonably high powers. Ytterium aluminum garnet (YAG) as a host material is hard, has a high thermal conductivity, and can be grown with good optical quality [8]. The laser generation wavelength is at 1.065 µm with line-widths of about 10 Å [8]. Models emitting up to one kilowatt continuous power at 1.06 µm are commercially available [9].

Characteristics of Nd:glass lasers are discussed in great detail in the literature [10-14]. The major disadvantage of glass as a host material is its low thermal conductivity [10]. This imposes limitations on the diameter that can be used for CW and high repetition rate operations because the glass host cannot dissipate heat quickly. An important factor which strongly influences the generation spectrum is the character of the luminescence line broadening in the active medium [7]. For an inhomogeneously broadened luminescence, the width of the laser emission spectrum can be quite large. Due to the nature of the glass host, line broadening in neodymium glass is inhomogeneous [7,10]. Snitzer [15] reports that the Nd$^{3+}$ 1.06 µm glass laser emission envelope just above threshold is approximately $3 \times 10^{-4}$ µm wide but can be increased to approximately $1.3 \times 10^{-2}$ µm by increasing the pump power. He further reports that individual laser modes of widths less than $10^{-5}$ µm can be obtained anywhere within this $1.3 \times 10^{-2}$ µm wide emission envelope. Hence, the
spectral composition of the Nd:glass laser varies within a single flash [16]. Since the Nd:glass laser has a high energy storage per unit volume and the glass host material affords considerable flexibility in size and shape, very high output powers are realizable from the Nd:glass laser [10,11].

2.2 Transmittance

In this report the simplified model [17] of an atmosphere composed of $N$ plane parallel homogeneous layers, each characterized by an extinction coefficient, $\gamma_j$, will be adopted but not applied to the 1.06 $\mu$m wavelength because of lack of experimental data concerning aerosol and molecular extinction coefficients versus altitude at this wavelength. The application of this model, which considerably reduces the complexity of the problem of calculating the atmospheric transmittance of radiation will be the subject of subsequent reports in this series. The complexity of the problem is due to the dependence of the extinction coefficient on a number of different physical properties of the atmosphere [18]. In essence, this plane stratified atmospheric model requires that the physical properties of the atmosphere change with elevation, but not laterally and in addition requires that the curvature of the earth be neglected.

Consider a beam of monochromatic collimated laser radiation propagating along the path $\Delta l_j$ in the $j$th layer of the assumed plane stratified atmosphere. The transmittance $\tau_j$ is given by

$$\tau_j = \exp(-\gamma_j \Delta l_j)$$

(1)

where

$$\Delta l_j = \Delta Z_j \sec \theta.$$  

(2)

Here $\Delta Z_j$ represents the increment of vertical distance and $\theta$ is the angle between the vertical and the direction of propagation. The total transmittance of this model atmosphere is given by

$$\tau = \prod_{j=1}^{N} \tau_j$$

(3)

or

$$\tau = \exp(-\sum_{j=1}^{N} \gamma_j \Delta l_j).$$

(4)

The extinction coefficient $\gamma_j$ can be expressed as the sum of the scattering coefficient $\sigma_j$ and the absorption coefficient $k_j$, i.e.,
\[
\gamma_j = \sigma_j + k_j.
\]  
(5)

The quantities \( \sigma_j \) and \( k_j \) depend on the kind and number of molecules and aerosols in the atmospheric path (see section 2.6), so one can write

\[
\sigma_j = \sigma_{mj} + \sigma_{aj}
\]  
(6)

and

\[
k_j = k_{mj} + k_{aj}
\]  
(7)

where

\[
\begin{align*}
\sigma_m &= \text{molecular scattering coefficient} \\
\sigma_a &= \text{aerosol scattering coefficient} \\
k_m &= \text{molecular absorption coefficient} \\
k_a &= \text{aerosol absorption coefficient}.
\end{align*}
\]

All of the above coefficients, \( \gamma \), \( \sigma \), and \( k \), are defined in \( \text{km}^{-1} \) if \( \Delta l \) is in kilometers (km).

2.3 Molecular Scattering

The molecular scattering (Rayleigh) coefficient, \( \sigma_m \), as a function of altitude for each wavelength, is expressed by

\[
\sigma_m(h, \lambda) = \sigma_R(\lambda)N(h)
\]  
(8)

where

\[
\begin{align*}
\sigma_R(\lambda) &= \text{Rayleigh cross section at wavelength } \lambda \\
N(h) &= \text{molecular number density at altitude } h.
\end{align*}
\]

Equation (8) is used to compute the Rayleigh coefficient, \( \sigma_m \), characterizing the \( j \)th layer located at an altitude \( h \). The Rayleigh cross sections for anisotropic air molecules is computed from \( [19] \)

\[
\sigma_R(\lambda) = \frac{8\pi^3}{3 \lambda^4 N^2} \cdot f
\]  
(9)

where \( f = 3(2+\delta)/(6-76) \), \( \delta \) is the so-called depolarization factor, \( n \) is the index of refraction of air, and \( N \) is the molecular number density at sea level.
The factor \( f \) is included in Equation (9) to compensate for the degree of molecular anisotropy. Gucker and Basu [20] report a value of \( 0.035 \) for \( \delta \).

The index of refraction for "standard air," viz., dry air containing 0.03 percent by volume of \( \text{CO}_2 \) at a pressure of 1013.25 mb and a temperature of 288°K, may be computed from the dispersion formula of Edlen [21],

\[
(n-1) \times 10^6 = 64.328 + \frac{29498.10}{146-(\lambda^{-2})} + \frac{255.40}{41-(\lambda^{-2})}
\]  

where \( \lambda \) is the wavelength in micrometers. In terms of atmospheric pressure \( P(\text{mb}) \) and temperature \( T(°K) \), the refractive modulus \( (n-1) \times 10^6 \) may be given by a less precise but more convenient formula [22], i.e.,

\[
(n-1) \times 10^6 = \frac{77.6P}{T} + \frac{0.584P}{T \lambda^2}.
\]  

Equation (11) is valid for wavelengths from 0.2 \( \mu \text{m} \) to 20 \( \mu \text{m} \).

2.4 Selective Molecular Absorption

The absorption bands of the atmospheric gases constitute a complex superposition of many spectral lines; therefore, one writes

\[
k_{mj}(\nu) = \sum_{i} k_{mi}(\nu)
\]  

where \( k_{mi} \) is the molecular absorption coefficient of the \( i \)th spectral line in the \( j \)th layer. The \( (i) \) summation is over all molecular absorption lines of all absorbing species which are close enough to the wavenumber \( \nu \) to contribute significantly to the total molecular absorption coefficient \( k_{mj}(\nu) \).

The attenuation of laser radiation in the atmosphere is caused in part by the so-called continuum absorption due primarily to the integrated effects of the wings of nearby strong absorption lines. This decomposition of the molecular absorption coefficient, \( k_{mj}(\nu) \), may be expressed in the form

\[
k_{mj}(\nu) = \sum_{r} k_{mr}(\nu) + \sum_{s} k_{msj}(\nu)
\]  

where the "\( r \)" summation is over all spectral lines whose centers are within the spectral width \( \Delta \nu \) of the laser radiation and the "\( s \)" summation extends to all absorbing species beyond the limits of \( \Delta \nu \) which affect
the transmission in $\Delta \nu$. The first term is the total selective molecular absorption coefficient. The second term is the continuum molecular absorption contribution from the wings of the many distant absorption lines on either side of the spectral region under consideration. The definition of the term "total continuum absorption coefficient" is discussed in the following section.

The molecular absorption coefficient $k_{m ij}(\nu)$ for a collision-broadened line can be given to good accuracy in the lower layers of the atmosphere (altitude <50 km) for the pressure range from about $10^3$ mb to about 10 mb by [23]

$$k_{m ij}(\nu) = \frac{S_{ij} \alpha_{ij}}{\pi} \left[ \frac{1}{(\nu - \nu_{0 ij})^2 + \alpha_{ij}^2} \right]$$

(14)

where

$$S_{ij} = \int k_{m ij}(\nu) d\nu.$$  \hspace{1cm} (15)

Here $S_{ij}$ is the normalized line intensity, $\alpha_{ij}$ is the half-width at half maximum, $\nu_{0 ij}$ is the wavenumber determining the position of the center of the $i$th spectral line and $\nu$ is the wavenumber at which the absorption coefficient is required. The Lorentz line shape given by Equation (14) is valid for $\nu$ lying within a few tenths of a cm$^{-1}$ of the line center $\nu_{0 ij}$ [24]. It has been shown [24] that when $(\nu - \nu_{0 ij}) \gg \alpha_{ij}$ the wings of the lines decay much more rapidly than Lorentz lines. Hence, for continuum molecular absorption calculations, a correction factor must be introduced into the Lorentz shape when $\nu$ lies beyond a few tenths of a cm$^{-1}$ from the line center $\nu_{0 ij}$. Line shape studies are needed in order to find the correct form for $k_{m}(\nu)$ that would be valid for all $\nu$.

The line intensities are functions of temperature, the dependence being different for different spectral lines. If $S_o$ is the value of intensity at standard temperature, $T_0$, and pressure, $P_0$, the value of $S$ at other temperatures is given by [25]

$$S(T,p) = S_o p(T_0 / T)^a \exp \left\{ \frac{-E''}{k} \left[ \frac{T}{T_0} \right] \right\}$$

(16)

where

- $E''$ = energy of molecule in the lower state of the transition responsible for the spectral line
- $k$ = Boltzmann's constant
- $p$ = partial pressure of absorbing gas (in atmospheres)
- $T$ = temperature (in degrees Kelvin)
- $a$ = constant depending on absorbing gas.
The half-width of the absorption line is a function of the partial pressure of the absorbing gas, the pressure of the nonabsorbing gas, and the temperature. The temperature and pressure dependence of the half-width is approximately [25]

\[ \alpha = \alpha_0 \left( \frac{P_e}{P_0} \right)^b \left( \frac{T_0}{T} \right). \]  

(17)

Here \( \alpha_0 \) is the half-width of the line in question at a pressure \( P_0 \) and a temperature \( T_0 \). The constant \( b \) depends on the absorbing gas. The effective pressure \( P_e \) is usually determined from the empirical relation [26]

\[ P_e = P + (B-1)p \]  

(18)

where \( P \) is the total atmospheric pressure; \( p \) is the partial pressure of the absorbing gas; and \( B \) is the self-broadening factor defined as the ratio of the self-broadening to the broadening by the nonabsorbing gas present. For small amounts of absorbers under atmospheric conditions \( P >> p \) so that one can write \( P_e \approx P \).

Calculations of the integrated transmittance over the rotational bands of water vapor have shown that the temperature dependence of this quantity is determined mainly by the temperature dependence of the line intensities [27]. The temperature variation of the line intensity may change by several orders of magnitude for the temperature range that occurs in the atmosphere [28]. At 1.06 \( \mu \)m the vibration-rotation bands dominate absorption so a corresponding study of the effects of temperature and pressure on the half-widths and intensities of vibrational-rotational lines is needed in order to predict accurately what these effects will do to radiation propagating through a real atmosphere under any weather conditions.

At present it is difficult to determine experimentally the fine structure of the vibrational-rotational spectrum (such as line positions, their intensities, and half-widths) for the majority of lines [29]. The experimental difficulties are caused by the abundance of absorption lines, their overlapping, and the spectrometer's slit function which makes it impossible to determine the true line contours and masks weak narrow lines. However, line strengths and half-widths may, in principle, be calculated from quantum mechanics, although in practice the calculations are intractable. An attempt to predict the fine structure of vibrational rotational spectra theoretically has been made by Gates et al. [30] for the 2.7 \( \mu \)m band of \( \text{H}_2\text{O} \). Although the authors took the positions of the line centers from experimental data, the intensities and half-widths were calculated by quantum mechanical methods. However, they did not consider the interaction of vibrational and rotational motions of the molecule. Failure to take into account the vibrational-rotation interaction in
water vapor may result in errors amounting from ten to several hundred per cent \[31\]. Zuev et al. \[29,32\] have taken into account the vibration-rotation interaction in calculating the intensities, half-widths, and line centers by quantum mechanical methods. The very high degree of monochromaticity of laser radiation makes this degree of sophistication necessary in calculating absorption of laser radiation in the atmosphere. This is true for the neodymium laser whose emission envelope can be relatively broad (as wide as \(1.3 \times 10^{-2} \mu m\)) because the individual laser modes within the envelope may have widths less than \(10^{-5} \mu m\) \[15\]. Presently, to this author's knowledge, no quantum mechanical calculations for the molecular absorption coefficient at \(\lambda = 1.06 \mu m\) for any absorbing gas have been reported in the literature.

2.5 Total Continuum Absorption

Practically all attempts at experimental investigation of the total continuum absorption have been made in the 8-12 \(\mu m\) window. Even here, the results of the total continuum effect are rather contradictory. The absorption coefficients calculated by various authors for the 8-12 \(\mu m\) spectral region differ by 50 to 100% \[33\]. One of the major problems is that the definition of the total continuum absorption coefficient is vague. That is due to the fact that attenuation in the so called "atmospheric windows" caused by the continuum molecular absorption due to wind effects of nearby strong absorbing lines is just one of the components of the overall continuum attenuation of the radiation. There is also attenuation of radiation due to molecular scattering, aerosol absorption, aerosol scattering, and in the case of highly monochromatic lasers, there may be strong selective molecular absorption by atmospheric gases such as H\(_2\)O, O\(_2\), CO\(_2\), and O\(_3\). Hence, in many cases all of these attenuation factors are lumped into one and the total continuum absorption coefficient \(k_F\) in the spectral width \(\Delta \nu\) is defined by the equation \[33\]

\[
\exp\{-k_F \ell\} = \frac{1}{\Delta \nu} \int \exp\{-\sum_j \gamma_j \Delta \nu\} d\nu 
\]

where

\[
\ell = \sum_j \Delta \nu_j 
\]

is the total path and the extinction coefficient, \(\gamma_j\), includes all the following terms:

\[
\gamma_j = \sigma_m \omega_j + \Sigma_{mr} \kappa_{mrj} + \Sigma_{ms} \kappa_{msj} + \sigma_{aj} + k_{aj} \cdot 
\]

Many authors simply assume that all but the third term of Equation (20) are negligible or that the attenuation effect in the atmospheric window \(\Delta \nu\) is caused solely by the molecular absorption by wings of nearby lines.
The continuum absorption coefficient $k^c_j$ is defined in this report as equivalent to the continuum molecular coefficient given by (See Equation (13))

$$k^c_j = \sum s^r_n s^j.$$  

The total continuum absorption coefficient in the spectral interval for this case is calculated from

$$\exp{-k^c T} = \frac{1}{\Delta \nu} \int \Delta \nu \exp{-\sum s^c_i \Delta \nu_j} d\nu.$$  \hspace{1cm} (21)

The quantity $k^c_j$ is evaluated at a position, far removed from the centers of the absorbing lines, where the line variations with wavenumbers are small in the interval $\Delta \nu$. Hence, the summation

$$\sum s^c_i \Delta \nu_j$$

may be treated to a first approximation as constant in the spectral interval $\Delta \nu$ so that

$$k^c_T = \frac{1}{\Delta \nu} \sum s^c_i \Delta \nu_j.$$  \hspace{1cm} (22)

In order to measure $k^c_T$ as defined by Equation (22), the effects due to the other attenuation components (see Equation (21)) must be considered.

The problem of the temperature dependence of absorption in the continuum is not established [333]. The dependence of $k^c$ on temperature and pressure should be resolved if predictions of continuum effects are to be made for different weather conditions.

2.6 Aerosol Extinction: Attenuation of Radiation at 1.06 μm Wavelength by Dust, Haze, Fog, Cloud, Rain, and Snow

The transmission of near-infrared radiation through the atmosphere is largely dependent on scattering and absorption by the most variable and least investigated atmospheric component, the atmospheric aerosol. The aerosol may consist of dust and combustion products, salt particles, industrial pollutants, minute living organisms and, most important, water droplets.

Mie theory can be used to derive the aerosol absorption ($k_a$) and scattering ($\sigma_a$) coefficients for spherical particles (or some other simple forms), provided the complex index of refraction, number density and size distribution are specified. One should keep in mind, however, that irregu-
larities in particle shape will disrupt the resonance inside the particle causing marked changes in the scattering [34]. Very few studies have been made under controlled conditions to compare the calculated and experimentally measured coefficients of radiation attenuation by the aerosol [35,36].

An assumption which is often made is that absorption by the scattering aerosol particles is negligibly small. Since over most of the spectrum aerosol scattering encountered in the atmosphere is dominant over aerosol absorption, this assumption is reasonable. However, there are exceptions where the scattering particles absorb strongly [37] so that one has to be careful in practice before making this assumption. In what follows, the aerosol absorption coefficient will be assumed negligible and thus the terms "aerosol extinction coefficient" and "aerosol scattering coefficient" may be used interchangeably. Areas where the magnitude of aerosol absorption may be significant will be indicated.

The atmospheric aerosol is present in any stratum in the atmosphere but with a highly variable concentration both in space and time. The aerosol size distribution spans a large range of particle sizes and may have considerable structure as found by Fenn [38], Goetz [39], Kondrat'yev et al. [40], and Rozenburg [41]. Moreover, many of the natural aerosol particles which are mixtures of water-soluble and water-insoluble components will undergo severe size fluctuations as the relative humidity varies [42,43]. The natural aerosol particles vary in size from about $4 \times 10^{-3}$ μm radius to about $10^2$ μm radius and are generally classified as follows:

a. Aitken particles of radius $\sim 10^{-3}$ to $10^{-1}$ μm
b. Large particles of radius $\sim 10^{-1}$ to 1.0 μm
c. Giant particles of radius $\geq 1.0$ μm.

The Aitken particles have the distinction of having a strongly wavelength-dependent absorption spectrum [41].

If the atmospheric aerosol is treated as spherical particles, the attenuation of radiation by aerosol will depend on the particle composition, the particle size distribution, and the number density. Consider an atmosphere where the aerosol sizes within a unit volume are characterized by a size distribution function $f(r)$. Various size distribution functions have been offered in the literature to describe the real atmosphere (e.g., Junge [44], Fenn [38], Fortzik [45]). The aerosol attenuation coefficient $\gamma_a$ is given by

$$\gamma_a(h, n, r, \lambda) = \int_{r_1}^{r_2} C_s(n, r, \lambda) dN(r) \quad (23)$$
where
\[ dN(r) = N(h)f(r)dr; \int f(r)dr = 1 \] (24)
and \( dN(r) \) = number of particles with radii between \( r \) and \( r+dr \) per unit volume

\( \gamma_a \) = aerosol extinction coefficient
\( n \) = complex index of refraction
\( \lambda \) = wavelength of incident radiation
\( C_s \) = cross section for each particle
\( r_1, r_2 \) = minimum and maximum radii of the aerosol particles
\( N(h) \) = total number of particles with radii between \( r_1 \) and \( r_2 \) per unit volume at height \( h \)
\( f(r) \) = size distribution function
\( N, N_a \) = aerosol number density limits corresponding to the limits \( r_1, r_2 \)

So
\[ \gamma_a(h, n, r, \lambda) = N(h) \int_{r_1}^{r_2} C_s(n, r, \lambda)f(r)dr. \] (25)

This is usually written in terms of the efficiency factor \( Q_{ext} \) defined as the ratio of the aerosol cross section \( C_s \) to the geometrical cross section of a single particle \( \pi r^2 \):

\[ Q_{ext} = \frac{C_s(n, r, \lambda)}{\pi r^2}. \] (26)

Hence, Equation (24) can be given as
\[ \gamma_a = \int_{r_1}^{r_2} Q_{ext}(n, r, \lambda)f(r)dr. \] (27)

From Equation (5) it is seen that \( \gamma_a \) is given by
\[ \gamma_a = \sigma_a + k_a \] (28)
where each of the coefficients \( \gamma_a, \sigma_a, \) and \( k_a \) can be written in terms of the sum of the corresponding \( i \)th particle coefficients:
\[ \gamma_a = \sum_{i=1}^{N} \gamma_{ai} \]
\[ \sigma_a = \sum_{i=1}^{N} \sigma_{ai} \]
\[ k_a = \sum_{i=1}^{N} k_{ai} \]

These definitions of \( \gamma_a \), \( \sigma_a \), and \( k_a \) are rigorous only if multiple scattering is ignored [46]. General expressions for \( Q_{\text{ext}} \) follow from Mie theory.

The widely varying aerosol characteristics which represent a specific atmospheric condition and are needed for the theoretical calculations of the extinction coefficient are difficult to measure in practice. Hence, the most effective method for obtaining the spectral variation of the aerosol extinction coefficients is by direct measurement of aerosol attenuation of radiation at various wavelengths and for different atmospheric conditions [47,48].

3. PUBLISHED DATA

In this section the published results of transmission measurements and theoretical calculations are used to estimate the atmospheric effects on the propagation of 1.06 \( \mu \)m laser radiation. The only available transmission data at this wavelength was obtained with apparatus having limited spectral resolution and therefore the results of this section are first-order approximations. The atmospheric attenuating mechanisms for which data are presented are molecular scattering, molecular line absorption, molecular continuum absorption, and attenuation by the aerosol. Quantitative estimates of the effects of haze, fog, cloud, and rain are provided. Finally, a qualitative estimate of attenuation by snowfall is included.

3.1 Molecular Scattering (\( \sigma_m \))

Elterman [19] has tabulated the theoretical values of molecular scattering coefficients for a clear standard atmospheric model for altitudes up to 50 km. Twenty-two wavelengths between 0.27 and 4.0 \( \mu \)m are considered. The meteorological range at sea level corresponds to about 25 km at 0.55 \( \mu \)m wavelength. The meteorological range or visual range, \( V \), is that distance for which the transmittance falls to 2%, i.e., \( V = 3.1912/\beta \) where \( \beta \) is the total scattering extinction coefficient. Figures 1 and 2 are plots of \( \sigma_m \) versus \( \lambda \) and \( \gamma_a \) versus \( \lambda \) based upon Elterman's data [19]. From these data it is seen that the molecular scattering coefficient for 1.06 \( \mu \)m wavelength radiation should be of the order of \( 8.2 \times 10^{-4} \) km\(^{-1} \) at sea level and approximately \( 6.1 \times 10^{-4} \) km\(^{-1} \) at an altitude of 3 km.
Figure 1. Rayleigh and aerosol scattering coefficients at sea level as a function of wavelength (from data by Elterman [19]).
Figure 2. Rayleigh and aerosol scattering coefficients at 3 km altitude as a function of wavelength (from data by Elterman [19]).
These are of the same order as the values obtained for the molecular scattering coefficient $a_m$ by McClatchey et al. [17] for 1.06 $\mu$m radiation along a path for five different atmospheric models (see Table I). It will be seen that the contribution to the overall attenuation of 1.06 $\mu$m radiation from the Rayleigh component is small and may be ignored for path lengths less than $10^2$ km.

3.2 Selective Molecular Absorption ($k_m$)

The atmosphere is exceptionally free of strong absorption lines in the 1.06 $\mu$m region as is evident from solar spectra [49,50]. Only a few weak O$_2$ and H$_2$O lines and the short-lived [O$_2$]$_2$ and [O$_2$-N$_2$] complexes are active in this region. These lines are difficult to observe in the laboratory even with high resolution and long paths ($\approx$2 km).

Figures 3-9 are facsimiles of plates 26 to 29 from the Mohler Solar Atlas [49]. A scale can be arbitrarily set to indicate relative absorption. No observations were made through cloudy or hazy skies. An upper bound on the absorption coefficient may be obtained for the maximum selective line absorption coefficient by use of these data. The strongest absorption line shown is located at 10585.1$\AA$. If one assumes an equivalent 16 km sea-level path and a minimum transmittance of 35% on the arbitrary scale based on Taylor and Yates data [51], Equation (1) yields for this line (assuming all attenuation is due to line absorption):

$$k_m^{\text{max}} \approx 6.5 \times 10^{-2} \text{ km}^{-1}.$$  

From a superficial examination of the spectrum, it appears that the average baseline transmittance over a 10$\AA$ bandwidth is of the order of 95%. This yields a molecular absorption coefficient for this region of

$$k_m^{\text{base}} \approx 3 \times 10^{-3} \text{ km}^{-1}.$$  

It seems reasonable to expect the line absorption contribution to the total extinction coefficient to fall between these two limits. A statistical analysis by Zuev et al. [52] of atmospheric transparency to laser radiation at various wavelengths reveals that the absorption coefficient $k_m$ is small, not exceeding

$$k_m \approx 4 \times 10^{-2} \text{ km}^{-1}$$  

at 1.06 $\mu$m under the conditions of Temperature $= 283^\circ$K and precipitable-centimeters (pr-cm) of H$_2$O = 0.3 to 0.7.
TABLE I

Molecular scattering coefficients reported by McClatchey et al. [17] for 1.06 μm wavelength for five different atmospheric models.

<table>
<thead>
<tr>
<th>Altitude (km)</th>
<th>Tropical $\sigma_m$ (km$^{-1}$)</th>
<th>Midlatitude Summer $\sigma_m$ (km$^{-1}$)</th>
<th>Midlatitude Winter $\sigma_m$ (km$^{-1}$)</th>
<th>Subarctic Summer $\sigma_m$ (km$^{-1}$)</th>
<th>Subarctic Winter $\sigma_m$ (km$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>8.04E-04</td>
<td>8.20E-04</td>
<td>8.91E-04</td>
<td>8.38E-04</td>
<td>9.39E-04</td>
</tr>
<tr>
<td>0-1</td>
<td>7.68E-04</td>
<td>7.81E-04</td>
<td>8.43E-04</td>
<td>7.98E-04</td>
<td>8.77E-04</td>
</tr>
<tr>
<td>1-2</td>
<td>6.99E-04</td>
<td>7.06E-04</td>
<td>7.52E-04</td>
<td>7.21E-04</td>
<td>7.70E-04</td>
</tr>
<tr>
<td>2-3</td>
<td>6.33E-04</td>
<td>6.38E-04</td>
<td>6.70E-04</td>
<td>6.50E-04</td>
<td>6.82E-04</td>
</tr>
</tbody>
</table>
Figure 3. Atmospheric absorption lines between 10,427.3Å and 10,469.7Å (from reference [49]).
Figure 4. Atmospheric absorption lines between 10,469.7Å and 10,513.0Å (from reference [49]).
Figure 5. Atmospheric absorption lines between 10,513.0 Å and 10,532.2 Å (from reference [49]).
Figure 6. Atmospheric absorption lines between 10,532.2 Å and 10,585.1 Å (from reference [49]).
Figure 7. Atmospheric absorption lines between 10.585 Å and 10.627.6 Å (from reference [49]).
Figure 8. Atmospheric absorption lines between 10,627.6Å and 10,661.0Å (from reference [49]).
Figure 9. Atmospheric absorption lines between 10,661.0Å and 10,707.4Å (from reference [49]).
The contribution by the \([O_2]_2\) and \([O_2-N_2]\) complexes has been under investigation by Dianov-Klokov et al. [53]. They have shown that the role of the band of the \([O_2]_2\) complex at 1.064 \(\mu\)m is dominant over the role of the individual \(O_2\) molecules. Additional data on the bands of the complexes in the near-infrared are needed to account for radiation loss due to these bands.

3.3 Total Continuum Absorption (\(k_C^c\))

There is practically no experimental data concerning the water vapor continuum in the region for \(\lambda<8\mu\)m except at the two points \(\lambda = 3.70\ \mu\)m and \(\lambda = 3.58\ \mu\)m where \(k_C^c = 0.062\ \text{gm}^{-1} \text{cm}^2\) and \(k_C^c = 0.07\ \text{gm}^{-1} \text{cm}^2\), respectively [54]. A quantitative assessment by Andreyev and Gal' tsev [33] of the continuum absorption coefficient for the region \(\lambda<8\mu\)m, based on the numerical analysis of the fine structure data of the water vapor spectrum presently available results in

\[
k_{1.06}^C \sim 2 \times 10^{-3}\ \text{gm}^{-1}\ \text{cm}^2
\]

or

\[
k_{1.06}^C \sim 6 \times 10^{-26}\ \text{molecules}^{-1}\ \text{cm}^2
\]

or

\[
k_{1.06}^C \sim 1.6 \times 10^{-6}\ \text{(atm-cm)}^{-1}\ \text{STP}\.
\]

To evaluate the contribution of \(k_C^c\) to the total extinction coefficient computed from Taylor and Yates' data [51] in a later section of this report, consider the path length to be 16 km, the temperature to be 278°K and the relative humidity (RH) to be 40%, so that one has

\[
k_{1}^C \sim 6 \times 10^{-4}\ \text{km}^{-1}
\]

This is of the order of the Rayleigh coefficient \(\sigma_m\), although at 305°K and 70% relative humidity, \(k_C^c\) will be an order of magnitude greater.

The coefficient of continuum absorption by \(H_2O\) for \(\lambda \sim 1.06\ \mu\)m computed by Kozyrev and Bazhenov [55] from experimental data of Elder and Strong [56] and Streeter [57] on the attenuation of radiation in the water vapor windows results in

\[
k_{1.06}^C \sim 5 \times 10^{-2}\ \text{gm}^{-1}\ \text{cm}^2
\]

or

\[
k_{1.06}^C \sim 1.5 \times 10^{-24}\ \text{molecules}^{-1}\ \text{cm}^2
\]
At 278°K and 48% relative humidity one has
\[ k_c^{1.06} \sim 1.5 \times 10^{-2} \text{ km}^{-1}. \]

This value extrapolated from available experimental data is 25 times greater than the theoretical value.

In the above cases it is not clear how the total continuum absorption coefficient \( k_T \) is defined. This may be the reason for such a large discrepancy between these two values. The largest value \( k_F = 1.5 \times 10^{-2} \text{ km}^{-1} \) seems somewhat of an overestimate but is useful as an upper limit for \( k_T \) at \( T = 278°K \) and \( RH = 48\% \). At \( T = 291°K \) and \( RH = 55\% \), this limit increases to \( k_F = 4 \times 10^{-2} \text{ km}^{-1} \). Thus it is seen that \( k_T \) is a function of temperature and relative humidity.

3.4 Aerosol Extinction: Attenuation of Radiation at 1.06 \( \mu \text{m} \) Wavelength by Dust, Haze, Fog, Cloud, Rain, and Snow

McCormick, Lawrence, and Crownfield [58] calculated backscattering and total cross sections for a Junge [44] size distribution \( f(r) \) of spherical aerosol particles with a refractive index of 1.5. These calculations were made for incident laser radiation at wavelengths of 0.3472 \( \mu \text{m} \), 0.5300 \( \mu \text{m} \), 0.6943 \( \mu \text{m} \), and 1.06 \( \mu \text{m} \), for different values of the size distribution parameter where

\[ f(r) = br^{-(v+1)}; \quad b = \text{constant} \]

and for four sets of particle radius limits \((r_1, r_2)\). Only the aerosol component was considered in their computations. For \( v = 3 \) and \((r_1 = 0.04 \mu \text{m}, r_2 = 10.0 \mu \text{m})\), their results for the average scattering cross sections per particle, \( \langle C_S \rangle \), at the different wavelengths are

\[
\begin{align*}
\langle C_S \rangle (\lambda = 0.3472 \mu \text{m}) &= 2 \times 10^{-10} \text{ cm}^2 \\
\langle C_S \rangle (\lambda = 0.5300 \mu \text{m}) &= 1.32 \times 10^{-10} \text{ cm}^2 \\
\langle C_S \rangle (\lambda = 0.6943 \mu \text{m}) &= 1.01 \times 10^{-10} \text{ cm}^2 \\
\langle C_S \rangle (\lambda = 1.06 \mu \text{m}) &= 6.56 \times 10^{-11} \text{ cm}^2.
\end{align*}
\]

If a "clear" atmosphere (23 km visibility), is assumed, the particle density at sea level is given by McClatchey et al. [17] approximately as \( 2.8 \times 10^3 \) particles \( \text{cm}^{-3} \) so that the average scattering coefficients computed from McCormick et al. [58] data are
\[ \sigma_a(\lambda = 0.3472 \, \mu m) \sim 5.6 \times 10^{-2} \, \text{km}^{-1} \]

\[ \sigma_a(\lambda = 0.5300 \, \mu m) \sim 3.7 \times 10^{-2} \, \text{km}^{-1} \]

\[ \sigma_a(\lambda = 0.6943 \, \mu m) \sim 2.8 \times 10^{-2} \, \text{km}^{-1} \]

\[ \sigma_a(\lambda = 1.06 \, \mu m) \sim 1.8 \times 10^{-2} \, \text{km}^{-1} \]

It is seen that the average scattering coefficient for \( \lambda = 1.06 \, \mu m \) is smaller than the scattering coefficients at the shorter wavelengths. It may be additionally inferred that if aerosol scattering is the dominant mechanism for reducing the transmission, the 1.54 \( \mu m \) wavelength should have a higher transmission.

Curcio, Knestrick, Cosden, and Drummeter [59] have reported on the attenuation of radiation by aerosol scattering. They reached the conclusion that the effective particle-size distribution for a particular day at any location near the coast can generally be approximated by a combination of continental and maritime distributions [60]. A typical measured relationship between the atmospheric aerosol extinction coefficient \( \gamma_a \) and the wavelength for a particular day in the Chesapeake Bay area is shown in their paper [59]. They corrected the data to show only the attenuation due to the atmospheric aerosol. From their data, the aerosol extinction coefficient at \( \lambda = 1.06 \, \mu m \) for a 16 km path and 25 km visibility is approximately given by

\[ \gamma_a \sim 1.13 \times 10^{-1} \, \text{km}^{-1} \]

\[ T = 291^\circ \text{K}; \ RH = 55\% \]

\[ \text{pr-cm of H}_2\text{O} = 4. \]

From Elterman's data [19], it is seen (Figures 1 and 2) that in the 1.06 \( \mu m \) wavelength region, the Rayleigh scattering coefficient \( \sigma_m \) is of no importance as compared with the aerosol extinction coefficient \( \gamma_a \). The value for \( \gamma_a(\lambda = 1.06 \, \mu m) \) as given by Elterman (for meteorological range \( T = 25 \, \text{km} \)) is \( \gamma_a \sim 1.13 \times 10^{-1} \, \text{km}^{-1} \).

Following is a discussion of results concerning the attenuation of 1.06 \( \mu m \) wavelength radiation by important types of aerosols: humid haze, fog, cloud, rain, and snow. Experimental measurements of attenuation by dry dust and other aerosols not included in the above types are not presented because of lack of data. Realistic theoretical estimates of dry particles such as these (dust, industrial pollutants, etc.) cannot be made because these particles are very irregular in shape. Irregular particles, as mentioned in Section 2.6, do not scatter radiation in entirely the same way that spherical particles do and hence Mie theory is not applicable. The water envelope on aerosols tends to make the spherical shape assumption more realistic, although how realistic is open to question.
Haze is defined as that finely dispersed fraction of the atmospheric aerosol with particle radius sizes lying between 0.1 μm to 0.6 μm. Hazes are formed when the relative humidity is less than 80%. When the relative humidity increases to about 80% or greater, a haze is replaced by a foggy haze, which in turn is replaced by a fog as the saturation point is reached. The essential characteristic of a fog as well as for a foggy haze is the existence, against the background of a continuous particle size distribution, of two stable narrow ranges of average sized particles [48]. For foggy hazes the ranges of particle radii are 1 to 5 μm and 12 to 15 μm, while for fogs, they are 8 to 12 μm and 18 to 25 μm. The radii of the droplets that dominate the scattering characteristics by clouds are between 5 and 20 μm. The average radii for rain droplets exceed 100 μm.

Approximately 90 to 95% of the aerosol formations characterizing the state of the atmosphere under real meteorological conditions are hazes [48]. Rosenberg [48] reports that a Junge size distribution should not be used to calculate extinction coefficients in the case of humid hazes, because of the water envelope. According to Gebbie et al. [61] and Sinclair [62], natural haze is approximately transparent in visible and near-infrared regions, and according to Arnulf et al. [63] the transmission increases markedly with increasing wavelength, from the visible to 10 μm. Arnulf et al. measured the transmittance τ through haze by use of the expression

\[ \tau = 10^{-dx} \]

where \( d \) is the optical density per unit length and \( x \) is the atmospheric path length. The optical densities and extinction coefficients obtained by Arnulf et al. for the case of haze are shown in Figure 10. The optical densities, \( d \), are related to the extinction coefficients by

\[ \gamma = 2.3d. \]

At 1.06 μm the densities fall in the interval 1 km\(^{-1}\) > \( d \) > 0.5 km\(^{-1}\). The extinction coefficient, \( \gamma_{\text{haze}} \), in this case lies in the interval

\[ 2.3 \text{ km}^{-1} > \gamma_{\text{haze}} > 1.15 \text{ km}^{-1} \]

indicating that for a 1 kilometer path, the transmittance \( \tau \) falls in the interval

\[ 10\% < \tau < 32\%. \]

The value for \( \gamma \) computed by Arnulf et al. probably also includes absorption by the haze, because it has been shown by Robinson [64] and Kondratyev [65] that it is likely that haze not only scatters, but also absorbs significantly in the visible and infrared spectral regions.
Figure 10. Scattering coefficients and optical densities for the case of haze (from reference [63]).
Arnulf et al. [63] also investigated the extinction of radiation by fogs. Figure II gives the extinction coefficients and optical densities of several types of fogs as compiled by them. As seen from the figure, a particular stable fog exhibits approximately the same opacity at all wavelengths shown out to 4 μm at which point it becomes more transparent. Moreover, the transmittance of the various fogs at 10 μm is observed to be higher than at all other wavelengths shown in the figure. It should be noted that the mean radii of the droplets of most fog investigated by Arnulf et al. fall in the range 2.3 to 3.0 μm, which is substantially less than the results of other investigators. The maximum measured drop radius never exceeded 15 μm.

Kurnick, Zitter, and Williams [66] measured the transmittance of natural fogs at various wavelengths and found a monotonic decrease of the extinction coefficient with wavelength.

The controversy as to what degree the optical properties of fogs determined experimentally with special chambers containing artificial fogs can be used to predict transmission through natural fogs has not yet been resolved [67,68].

Gates and Shaw [69] measured transmission through various cloud types using the sun as a source. They report that transmission through clouds is always slightly higher in the 8.0 to 12.0 μm wavelength region than in the 0.48 to 5 μm wavelength region. Since calculations of pure scattering by clouds show better transmission at the shorter wavelengths than at the longer wavelengths, the authors conclude that the water vapor bands in the near infrared absorbed sufficiently to reverse the trend.

Carrier, Cato, and Von Essen [70] computed extinction coefficients for eight specific cloud models using the exact Mie theory for incident radiation at wavelengths of 0.488, 0.694, 1.06, 4.0 and 10.6 μm. Their results showed that there is no clear advantage of one wavelength over another for improving through-cloud transmission, although backscattering is markedly reduced at the longer wavelengths. The largest source of uncertainty of their results is the neglect of multiple scattering. Table II is a summary of calculated extinction coefficients versus wavelength for the eight models considered. Wide variations in these values can be expected for cloud models that differ from those used in this investigation.

Scattering by rain is a multiple scattering phenomenon which is difficult to analyze quantitatively. However, an estimate of attenuation by rain can be made by assuming single scattering theory and by taking notice that multiple scattering effects will only lower the measured extinction coefficient. Thus, by Equation (27), i.e.,

\[
\gamma_{\text{rain}} = N \int_{r_1}^{r_2} \frac{2\pi Q_{\text{ext}}(n,r,\lambda)f(r)}{r} dr
\]

(30)
Figure II. Scattering coefficients and optical densities for the case of fog (from reference [63]).
TABLE II

Extinction coefficients versus wavelength for eight specific cloud types (from reference [70]).

<table>
<thead>
<tr>
<th>Cloud Type</th>
<th>0.488 μm</th>
<th>0.694 μm</th>
<th>1.06 μm</th>
<th>4.0 μm</th>
<th>10.6 μm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nimbostratus</td>
<td>128</td>
<td>130</td>
<td>132</td>
<td>147</td>
<td>136</td>
</tr>
<tr>
<td>Altostratus</td>
<td>108</td>
<td>109</td>
<td>112</td>
<td>130</td>
<td>83.9</td>
</tr>
<tr>
<td>Stratus II</td>
<td>100</td>
<td>101</td>
<td>103</td>
<td>114</td>
<td>104</td>
</tr>
<tr>
<td>Cumulus Congestus</td>
<td>69.2</td>
<td>69.8</td>
<td>71.3</td>
<td>81.0</td>
<td>67.6</td>
</tr>
<tr>
<td>Stratus I</td>
<td>66.9</td>
<td>67.9</td>
<td>69.7</td>
<td>90.1</td>
<td>42.8</td>
</tr>
<tr>
<td>Cumulonimbus</td>
<td>43.5</td>
<td>43.8</td>
<td>44.4</td>
<td>48.2</td>
<td>50.9</td>
</tr>
<tr>
<td>Stratocumulus</td>
<td>45.3</td>
<td>46.0</td>
<td>47.1</td>
<td>59.6</td>
<td>24.8</td>
</tr>
<tr>
<td>Fair Wx Cumulus</td>
<td>21.0</td>
<td>21.3</td>
<td>21.9</td>
<td>27.6</td>
<td>11.7</td>
</tr>
</tbody>
</table>
an approximate upper bound for the extinction coefficient for rain can be found for a given concentration N. Now at wavelengths between 0.4 \( \mu m \) and 15 \( \mu m \), the rain drops can be considered as large droplets with \( Q_{\text{ext}} \) virtually equal to two.

Hence,

\[
Y_{\text{rain}} = 2N \int_{r_1}^{r_2} \pi r^2 f(r) \, dr = 2G. \tag{31}
\]

Here

\[
G = N \int_{r_1}^{r_2} \pi r^2 f(r) \, dr. \tag{32}
\]

is the geometrical cross section of drops in unit volume. Thus the extinction coefficient for rain given by Equation (31) is independent of wavelength between 0.4 \( \mu m \) and 15 \( \mu m \).

Polyakova [71] has shown from experimental studies that the magnitude of \( Y_{\text{rain}} \) from 0.4 to 15 \( \mu m \) wavelength can be obtained from rainfall intensity data. Polyakova established the empirical relationship

\[
Y_{\text{rain}} = 0.21J^{0.74} \tag{33}
\]

where \( J \) is the rainfall rate in mm/hr and \( Y_{\text{rain}} \) is the magnitude of the extinction coefficient for rain in units of km\(^{-1}\). Figure 12 gives rainfall rate versus attenuation by rain for near infrared wavelengths.

The extinction coefficient for rain can thus be estimated from Equation (31) if the analytical form of the drop size distribution and the drop number density are known or, from Equation (33), if the rainfall intensity is known.

The value for \( Y_{\text{rain}} (\lambda = 1.06 \mu m) \) calculated by Equation (33) for 1 mm/hr rate of rainfall is

\[
Y_{\text{rain}} (\lambda = 1.06 \mu m) = 2.1 \times 10^{-1} \text{ km}^{-1}
\]

and for 10 mm/hr rate of rainfall

\[
Y_{\text{rain}} (\lambda = 1.06 \mu m) = 1.15 \text{ km}^{-1}.
\]

Snow consists of scatterers of very complex form; this makes theoretical predictions of attenuation at different wavelengths extremely difficult. Although the extinction coefficient for rain is independent of wavelength
Figure 12. Rainfall rate (mm/hr) versus attenuation (dB/km).
between 0.4 \( \mu m \) and 15 \( \mu m \), the same is not true of snow. Wilson and Penzias [72] have observed the wavelength dependence of the measured attenuation coefficient in snowfall where they found that the attenuation is greater at 10 \( \mu m \) wavelength than at 0.63 \( \mu m \) or 3.5 \( \mu m \) wavelength. Measurements by Kabanov and Pkhala\(v\)ov [73] indicate that attenuation by snowfall at 10 \( \mu m \) wavelength is greater than at 1 \( \mu m \) wavelength. (Attenuation is still severe at 1 \( \mu m \) wavelength, about between that due to fog and that due to rain for the same amount of equivalent liquid water [74].) This suggests that transmission through snowfall is better at 1.06 \( \mu m \) (Nd\(^{3+}\) laser) than at 10.6 \( \mu m \) (CO\(_2\) laser) wavelength. This inference has not yet been experimentally tested.

There are few experimental data available on the aerosol attenuation coefficient \( \gamma_a(h) \) in the infrared at various altitudes at the present time [75].

4. COMPARISON BETWEEN TRANSMISSION AT 1.06 \( \mu m \) AND 1.54 \( \mu m \)

Berlinguette and Tate [76] have made spectroscopic measurements of absolute transmission for atmospheric paths for the wavelength region 0.9 \( \mu m \) to 5.9 \( \mu m \) with horizontal path lengths of 0.67 km and 1.2 km. Selective window transmissions, in terms of precipitable water vapor, were established for the 0.92 \( \mu m \) to 1.10 \( \mu m \) window and other spectral windows for path lengths of 0.007 km, 0.01 km, 0.27 km, 0.67 km, and 1.2 km. The amounts of precipitable water in the paths considered varied from 0.02 to 7.4 mm. Unfortunately, errors of \( \pm 3\% \) appeared to be involved in the calibration of their apparatus so that little reliance can be placed on the absolute scale of their transmission plots. One can, however, compare the value of the extinction coefficients for 1.06 \( \mu m \) neodymium (Nd\(^{3+}\)) and 1.54 \( \mu m \) erbium (Er\(^{3+}\)) laser radiation from their data. For the longest path (1.2 km) with resolving power of about 200 at 1.06 \( \mu m \) wavelength and 7.4 precipitable millimeters of water vapor in the path, their data show that

\[
\gamma_{1.06} \approx 1.13 \times 10^{-1} \text{ km}^{-1}
\]
\[
\gamma_{1.54} \approx 4.3 \times 10^{-2} \text{ km}^{-1}
\]

That is,

\[
\gamma_{1.06} \approx 2.6 \gamma_{1.54}
\]

In terms of precipitable mm of \( H_2O \):

\[
\gamma_{1.06} \approx 1.8 \times 10^{-2} \text{ mm}^{-1} (H_2O)
\]

34
compared to the erbium case (atmospheric transmission characteristics of Er$^{3+}$ discussed in reference [77])

\[ Y_{1.54} \approx 6.9 \times 10^{-3} \text{ mm}^{-1} (H_2O). \]

Taylor and Yates [51] have made infrared transmission measurements from 0.5 $\mu$m to 15 $\mu$m wavelength over three horizontal sea-level paths of 0.305 km, 5.5 km, and 16.25 km at Chesapeake Bay. Figure 13 displays their results for a relatively clear winter day under the conditions shown. They covered the band 0.5 $\mu$m to 1.8 $\mu$m with a resolving power of 353 at 1.06 $\mu$m. The extinction coefficients calculated from their data for both Nd$^{3+}$ and Er$^{3+}$ laser wavelengths are

a) 5.5 km path: \[ Y_{1.06} \approx 1.15 \times 10^{-1} \text{ km}^{-1} \]
\[ Y_{1.54} \approx 7.8 \times 10^{-2} \text{ km}^{-1} \]

or in terms of precipitable water vapor in the path:

\[ Y_{1.06} \approx 4.63 \times 10^{-2} \text{ mm}^{-1} (H_2O) \]
\[ Y_{1.54} \approx 3.14 \times 10^{-2} \text{ mm}^{-1} (H_2O) \]

b) 16.25 km path: \[ Y_{1.06} \approx 6.3 \times 10^{-2} \text{ km}^{-1} \]
\[ Y_{1.54} \approx 4.7 \times 10^{-2} \text{ km}^{-1} \]

or in terms of precipitable water vapor in the path:

\[ Y_{1.06} \approx 2.0 \times 10^{-2} \text{ mm}^{-1} (H_2O) \]
\[ Y_{1.54} \approx 1.5 \times 10^{-2} \text{ mm}^{-1} (H_2O). \]

R. K. Long [6] has examined transmission measurements made by Streete [57]. At medium resolution, the data indicated that transmission at 1.06 $\mu$m may be higher than that at 1.54 $\mu$m. This is at odds with the results of this report which are based essentially on Taylor and Yates data. However, at higher resolution, Streete's data indicated that the absolute transmittances are comparable and transmission at 1.536 and 1.544 $\mu$m may be higher. The conclusion of the author corroborates that of Long [6] that Streete's data are not any more accurate than those of Taylor and Yates. Thus the problem regarding the transmission at 1.06 $\mu$m vs 1.54 $\mu$m is still unresolved. In any case, it is safe to say, transmission at these two wavelengths is higher than at most of the other laser wavelengths available. The problem of which wavelength has a higher transmission awaits higher resolution experimental studies at these two wavelengths.
<table>
<thead>
<tr>
<th>CURVE</th>
<th>PATH LENGTH</th>
<th>DATE</th>
<th>TIME</th>
<th>TEMP.</th>
<th>R.H.</th>
<th>PRECIPITABLE WATER</th>
<th>VISUAL RANGE</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>1000'</td>
<td>3-20-56</td>
<td>3PM</td>
<td>37°F</td>
<td>62%</td>
<td>1.1MM</td>
<td>22MI.</td>
</tr>
<tr>
<td>B</td>
<td>3.4MI.</td>
<td>3-20-56</td>
<td>10PM</td>
<td>34.5°F</td>
<td>47%</td>
<td>13.7MM</td>
<td>16MI.</td>
</tr>
<tr>
<td>C</td>
<td>10.1MI.</td>
<td>3-21-56</td>
<td>12AM</td>
<td>40.5°F</td>
<td>48%</td>
<td>52.0MM</td>
<td>24MI.</td>
</tr>
</tbody>
</table>

**WINDOW DEFINITIONS**

| I     | 0.72 TO 0.94μ | V    | 1.90 TO 2.70μ |
| II    | 0.94 TO 1.13μ | V1   | 2.70 TO 4.30μ |
| III   | 1.13 TO 1.38μ | VII  | 4.30 TO 6.0 μ |
| IV    | 1.38 TO 1.90μ | V111 | 6.0 TO 15.0 μ |

Figure 13. Atmospheric transmission spectra obtained by Taylor and Yates (from reference [51]).
5. SUMMARY AND CONCLUDING REMARKS

The scattering mechanism is of considerable importance in the propagation of 1.06 μm wavelength radiation because this wavelength lies in the 0.92 to 1.10 μm "atmospheric window" of weak molecular absorption. The usual assumption made under these circumstances is that the total extinction coefficient measured in this region of weak molecular absorption is the total scattering coefficient (Rayleigh plus Mie). The contributions by the continuum absorption, aerosol absorption, and selective line absorption are thus assumed negligible. This atmospheric window nonetheless is filled with numerous weak lines \([O_2, H_2O, [O_2]_2, [O_2-N_2]]\) whose central frequencies readily absorb laser energy, the aerosol may absorb significantly and the magnitude of the continuum is still undecided. For these reasons the assumption that the total extinction coefficient measured in this window region is the total scattering coefficient is unreasonable for the case of atmospheric attenuation of 1.06 μm laser radiation. To resolve this problem (i.e., account for the various attenuation components in the window regions) the characteristics of the aerosol must be specified, the lines in the atmospheric spectra must be specified to no less than 0.1 cm\(^{-1}\) accuracy and the strength of the continuum must be established. For lower accuracy of line positions, errors in the determination of the absorption coefficient may reach tens and hundreds of percent and even higher \([31]\). For low visibilities (< 10 km), however, the aerosol scattering mechanism will dominate the attenuation of 1.06 μm electromagnetic radiation and, hence, molecular scattering and absorption losses will be of minor significance.

It should be noted that selective window transmission calculations by Berlinguette and Tate \([76]\) were not subjected to the calibration error. Their data showed that for amounts of precipitable water less than 7.4 mm in the path, the transmission in the 0.92 μm to 1.10 μm window is greater than 90%. Hence, the total extinction coefficient in the band 0.92 to 1.10 μm is

\[
\gamma_{\text{total}} \approx 10^{-1} \text{ km}^{-1}.
\]

This value seems unreasonably small for total attenuation but appears feasible for the attenuation at the selective wavelength of 1.06 μm.

Also, note that Taylor and Yates state the visual range (see Figure 13) in effect at the time of their measurements. A rough, but useful relationship that can be used to estimate the total scattering extinction coefficient, \(\beta = \alpha_m + \gamma_a\), for their various sets of measurements is \([78]\)

\[
\beta \approx (3.9/V)(0.53/\lambda)^{0.62V^{1/3}}
\]

(34)
where $V$ is the visual range expressed in km and $\lambda$ is the monochromatic beam wavelength in micrometers. The value of $\beta_{1.06}$ for the 5.5 km path length is

$$\beta_{1.06} \approx 4 \times 10^{-2} \text{ km}^{-1}$$

and for the 16.25 km path length is

$$\beta_{1.06} \approx 2 \times 10^{-2} \text{ km}^{-1}.$$  

Hence, one might conclude that the scattering mechanism was not as active during the measurements of Taylor and Yates as it was for the measurements of Curcio, Knestrick, Cosden, and Drummeter [59].

If one removes the total scattering component from Taylor and Yates' value for $\gamma_{\text{total}}$ for the 16.25 km path, the following value of $\gamma'$ results where

$$\gamma'_{1.06} = \gamma_{\text{total}} - \beta = 4.3 \times 10^{-2} \text{ km}^{-1}.$$  

If the total continuum absorption coefficient is of the order of

$$k_T^c = 1.5 \times 10^{-2} \text{ km}^{-1}$$

as discussed previously, then

$$\gamma''_{1.06} = \gamma_{\text{total}} - \beta - k_T^c = 2.8 \times 10^{-2} \text{ km}^{-1}.$$  

Hence, it follows that the selective molecular absorption coefficient from Taylor and Yates data for the wavelength 1.06 $\mu$m falls in the range

$$2.8 \times 10^{-2} \text{ km}^{-1} < k_m < 6.3 \times 10^{-2} \text{ km}^{-1}$$

when all attenuating mechanisms are taken into account.

In section 2 of this report, the factors that contribute to the atmospheric attenuation of laser energy were identified. These factors are listed in the table below along with numerical values as given in section 3. There is little doubt that for all practical purposes the aerosol is the main attenuating mechanism of 1.06 $\mu$m wavelength radiation.
TABLE III MAGNITUDES OF ATMOSPHERIC EFFECTS AT 1.06 μm

<table>
<thead>
<tr>
<th>Attenuating Mechanism</th>
<th>Attenuation Coefficient</th>
<th>Attenuation Loss Upper Bound (dB/km)</th>
<th>Reference</th>
<th>Page No. on this Report</th>
</tr>
</thead>
<tbody>
<tr>
<td>Molecular Scattering, σ_m</td>
<td>0.0008</td>
<td>0.003</td>
<td>[19]</td>
<td>12</td>
</tr>
<tr>
<td>Selective Molecular Absorption, k_m</td>
<td>0.065</td>
<td>0.282</td>
<td>[49,51]</td>
<td>15</td>
</tr>
<tr>
<td>Total Continuum Absorption, k_τ</td>
<td>0.015</td>
<td>0.065</td>
<td>[55]</td>
<td>25</td>
</tr>
<tr>
<td>Aerosol Extinction, γ_a</td>
<td>0.113</td>
<td>0.490</td>
<td>[57]</td>
<td>26</td>
</tr>
<tr>
<td>Total Extinction, γ = σ_m + k_τ + k_m + γ_a</td>
<td>0.2</td>
<td>0.87 (clear day, sea level paths)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Light Rain (1 mm/hr)</td>
<td>0.2</td>
<td>0.87</td>
<td>[71]</td>
<td>32</td>
</tr>
<tr>
<td>Heavy Rain (10 mm/hr)</td>
<td>1.2</td>
<td>5.2</td>
<td>[71]</td>
<td>32</td>
</tr>
<tr>
<td>Cloudburst (100 mm/hr)</td>
<td>6.3</td>
<td>27.5</td>
<td>[71]</td>
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<td>2.3</td>
<td>10</td>
<td>[63]</td>
<td>27</td>
</tr>
<tr>
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The results of this report indicate that the total extinction coefficient at λ = 1.06 μm for horizontal paths at sea level under good visibility (>10 km) should lie in the range

\[ 2 \times 10^{-2} \text{ km}^{-1} < \gamma_{\text{total}} < 2 \times 10^{-1} \text{ km}^{-1}. \]

The attenuation due to rain over short paths (<5 km) and at low rain rates (<10 mm/hr) is not severe, however, cloud, fog and haze will have a considerable effect on the transmission. The problem regarding the transmission of 1.06 μm vs 1.54 μm is still unresolved. The most definitive statement that can be made at this time is that transmission at these two wavelengths is higher than at most of the other laser wavelengths available.

This study has defined the following areas as barrier problems which need to be resolved before adequate predictions of laser systems performance can be made:

1. Effects of temperature and pressure on the half-widths and intensities of vibrational and rotational lines are not adequately known.
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This study has defined the following areas as barrier problems which need to be resolved before adequate predictions of laser systems performance can be made:

1. Effects of temperature and pressure on the half-widths and intensities of vibrational and rotational lines are not adequately known.
2. Vibration-rotation interaction in computing line spectra needs to be accounted for consistently.

3. Magnitude of continuum absorption is unestablished and its definition is vague.

4. Contribution of \([O_2-N_2]\) and \([O_2]\)_2 complexes to the over-all attenuation at 1.06 μm is uncertain.

5. Aerosol attenuation measurements versus theoretically calculated aerosol coefficients need to be investigated for validity. Controlled experimental measurements in aerosol absorption work are seriously lacking, and research into the altitude variation of the aerosol extinction is urgently needed. In addition, the theoretical treatment of irregular particles needs further investigation.
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