GENERAL RECIPROCITY PARAMETER

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General Reciprocity Parameter

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The reciprocity parameter used in the reciprocity calibration of electroacoustic transducers is derived for the general case of arbitrary boundary conditions and arbitrary definitions of responses. A general reciprocity parameter is defined as the ratio of the volume velocity emanating from a surface defined in the transmitting response to the resulting pressure averaged over a surface defined in the receiving response. It is shown how the general parameter concept leads directly and simply to the various special parameters for the cases of spherical waves, cylindrical waves, plane waves, diffuse sound, couplers, and tubes. Application of the concept to in situ and nearfield conditions is also described.

INTRODUCTION

The reciprocity parameter $J$ used in the reciprocity calibration of electroacoustic transducers is defined by $J = M/S$, where $M$ is the receiving sensitivity and $S$ is the transmitting response of a reciprocal transducer. Obviously, $J$ depends on how $M$ and $S$ are defined—that is, on what electrical and acoustical parameters are chosen to describe the input and output of the transducer and on what the boundary conditions are on the medium are.

Since MacLean and Cook first applied the reciprocity principle to the calibration of electroacoustic transducers in 1940, there has been a continuing development of reciprocity parameters to fit special conditions. MacLean's original reciprocity calibration was under far-field-free-field conditions and, although it is not usually identified as such, his parameter should be called the spherical-wave reciprocity parameter. Cook's work pertained to what is now generally called coupler reciprocity. Beranek extended the coupler method to include standing-wave tubes. In 1949, Simmons and Urick developed a plane-wave reciprocity parameter. In 1961, Bobber and Sabin contributed a cylindrical-wave reciprocity and Diestel a diffuse-sound reciprocity. Most recently, Beatty reports on two parameters used in tube reciprocity. His tube reciprocity differs from Beranek's in that Beatty uses plane, progressive waves rather than standing waves.

The development of each of these parameters has, for the most part, been independent of the others. There have been some exceptions. Sabin, in one of the two methods used to derive the cylindrical-wave parameter, used the spherical-wave parameter. Trotty has also shown how the plane-wave and cylindrical-wave parameters can be derived from power relationships if the spherical-wave parameter is known.

Actually, all the reciprocity parameters have a common meaning and physical definition as acoustic transfer admittances. Wathen-Dunn identified $J$ as the transfer admittance between two points in an acoustic medium. Although he allowed arbitrary boundary conditions of the medium, Wathen-Dunn did assume that the reference pressures in the definitions $M = E/p_w$ and $S = p/1$ were pressures at a point, thus limiting $J$ to a transfer admittance between points. This author developed the cylindrical-wave reciprocity parameter in terms of the acoustic transfer admittance between two parallel lines. Among the various reciprocity methods,
the sound pressures \( p_m \) and \( p_A \) in different cases are pressures at a point, along a line, over a plane, and the average pressure in a room or tank.

A unifying concept for all reciprocity parameters is derived in terms of a general reciprocity parameter, where the boundary conditions of the medium, the reference pressures used in defining \( M \) and \( S \), and the transducer configuration are all arbitrary. It is also shown how a general parameter can be used to derive special parameters—in some cases with considerable savings in analytical labor—and how the general parameter concept is used to measure \( J \) for boundary conditions that preclude computation.

I. DERIVATION OF THE GENERAL RECIPROCITY PARAMETER

Consider a reciprocal, electroacoustic transducer \( T \) of arbitrary shape in a medium with arbitrary boundaries as shown in Fig. 1. The current through and the voltage across the transducer are \( I \) and \( E \), respectively. The receiving sensitivity of \( T \) in the most general case is the ratio of an output voltage or current to an input pressure or velocity. Although any of the four combinations of these output/input parameters can be used, we are interested only in the voltage/pressure ratio that is usually used to express the sensitivity of a microphone or hydrophone. For both theoretical and practical reasons, the output voltage \( E \) is always an open-circuit voltage \( E_o \). The input pressure may be defined in any of the several ways mentioned in the Introduction—that is, at a point, along a line, etc. In some cases, the reference pressure is the pressure that exists when \( T \) is absent; in other cases, it is the real applied pressure \( p_A \) at the transducer diaphragm.

The ratio \( E_o/p_m \) is called a pressure sensitivity. The pressure sensitivity usually is measured and used only when the dimensions of the transducer are small as compared with a wavelength and the transducer has an acoustic impedance equal to or greater than the characteristic impedance of the medium. Under these conditions, the difference between the applied pressure and the pressure in the absence of the transducer is negligible.

Let \( p_m \) be defined as the average input or received pressure at \( A_m \) when the transducer is either absent or present. For specific cases, the definition of \( M \) will state or imply which condition applies. Then \( M = E_o/p_m \). The place \( A_m \) at which the pressure acts can be a point, a line, or a surface, and may be at an arbitrary location. In practice, of course, \( A_m \) is usually a point and is called the acoustic center of \( T \), but this is only a practice and not a requirement. There is not necessarily any relation between \( A_m \) and the actual size or shape of \( T \). When the medium is unbounded, \( p_m \) may be a free-field pressure, but not necessarily a far-field pressure, as is illustrated later in a nearfield case.

The transmitting response \( S \) is defined as the ratio \( p_A/I \), where \( p_A \) is the output or transmitted pressure and \( I \) is the input current when \( T \) is the only source in the medium. Again, we could use output velocity and input voltage, but choose pressure and current for simplicity and conformity with common practice. The pressure \( p_A \) is the pressure at some arbitrary place \( A_s \) in the medium averaged over \( A_s \). As with \( A_m \), \( A_s \) can be a point, a line, or a surface.

In the analysis to follow, both \( A_m \) and \( A_s \) will be understood to be a continuous closed surface. When either is referred to as a point, it is intended to mean an infinitesimally small spherical surface. Likewise, a line is a cylindrical surface of infinitesimal diameter and a plane is actually two parallel planes separated by an infinitesimal distance. The ends of the lines and the edges of the planes are part of the closed surface but are of negligible area.

Having defined \( M \) and \( S \) for general boundary conditions, we can now find a general reciprocity parameter \( J \), where

\[
J = M/S = (E_o/p_m)/(p_A/I).
\]
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Fig. 2. Network representation of the electroacoustic system; I is current, E is voltage, \( \phi \) is the pressure at \( A_e \), \( U \) is the volume velocity from \( A_v \), \( Z_e \) is the electrical impedance when \( U = 0 \), \( Z_a \) is the acoustic impedance when \( I = 0 \) or \( \phi \) is the electroacoustic transfer impedance.

Foldy and Primakoff\(^{10}\) have proved that the reciprocity theorem applies for the general case of a linear, passive, reversible electroacoustic transducer immersed in a bounded or unbounded medium where the medium itself is reciprocal. Therefore, a system as shown in Fig. 1 can be depicted by a network as shown in Fig. 2 and described by the two equations

\[
\bar{p} = Z_e U + \phi I, \tag{2}
\]

\[
E = \phi' U + Z_a I, \tag{3}
\]

where \( \bar{p} \) is the average pressure over \( A_v \) and \( U \) is the net volume velocity emanating from \( A_e \) or \( \int A_e \text{d}A_v \), where \( \alpha \) is the linear velocity normal to the surface. The coefficients \( \phi \) and \( \phi' \) are the electroacoustic transfer impedances of the system and \( \phi = \phi' \) because the system is reciprocal. A restriction should be noted at this point. The transducer \( T \) cannot have both electrostatic and electromagnetic couplings. Foldy and Primakoff included this restriction in their proof, and others\(^{11,12}\) have demonstrated that a combination system is not reciprocal.

The coefficient \( Z_e \) in Eq. 3 is the electrical input impedance of the transducer when \( U = 0 \) or when the system is driven only electrically.

From the definition, \( U \) has a positive value when a source is located inside \( A_v \) and sound emanates outward, and it has a negative value when a net velocity flows inward to an energy sink. The volume velocity \( U_e \) is zero when sound merely passes through \( A_e \). The coefficient \( Z_a \) is the acoustic impedance at \( A_v \) when \( I = 0 \), or when the system is driven only acoustically by a source at \( A_e \) and the electrical terminals of transducer \( T \) are open. If \( A_v \) is visualized as an imaginary transducer, \( Z_a \) is the acoustical radiation impedance of \( A_v \).

If we drive the system electrically and \( U = 0 \), Eq. 2 becomes

\[
\bar{p}_a = \phi I. \tag{4}
\]

If we drive it acoustically with an imaginary source at

\[ A_v \] and open-circuit the electrical terminals, \( I = 0 \) and Eq. 3 becomes

\[
E_a = \phi U, \tag{5}
\]

and

\[
\phi = \bar{p}_a / I = E_a / U. \tag{6}
\]

Multiplying the right hand member of Eq. 6 by \( (\bar{p}_m / \bar{p}_a) \) produces

\[
\bar{p}_a / I = (E_a / \bar{p}_a)(\bar{p}_m / U). \tag{7}
\]

From Eqs. 1 and 7,

\[
M/S = U / \bar{p}_m = J. \tag{8}
\]

Equation 8 becomes the definition of the general reciprocity parameter. It is the ratio of the volume velocity emanating from a surface \( A_v \) (defined by \( S \)) to the resulting pressure \( \bar{p}_m \) at \( A_m \) (defined by \( M \)). Thus, it is an acoustic transfer admittance, but in a reverse sense. That is, although associated with the transducer \( T \), the parameter \( J \) describes a transfer function of a wave starting at \( A_v \) and traveling to \( T \). If \( \bar{p}_m \) is defined as a pressure in the absence of \( T \), then \( J \) can have an alternate meaning. If \( U' \) is the velocity emanating from an imaginary source at \( A_m \), then \( \bar{p}' = \bar{p}_m \) is the resulting pressure at \( A_v \), then, according to the acoustical reciprocity theorem,

\[
U' / \bar{p}' = U / \bar{p}_m = J. \tag{9}
\]

Thus, \( J \) can also be given by the transfer admittance \( U' / \bar{p}' \). As we shall see, this alternate definition of \( J \) can be useful.

II. DERIVATION OF SPECIAL RECIPROCITY PARAMETERS

Given Eq. 8, the derivation of all the special parameters becomes relatively straightforward. Although Wathen-Dunn\(^9\) has used a similar approach for the spherical-wave case, it is reexamined here to justify the use of point transducers. The author\(^4\) has already used the general parameter concept in deriving the cylindrical-wave parameter, and it is not repeated here.

A. Spherical Waves

The case of the conventional spherical-wave parameter \( J_{m/k} \) is shown schematically in Fig. 3. The trans-
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**Fig. 4. Schematic representation of Fig. 1 for the plane-wave case.**

\[ U/P_m = 4\pi d/pc^2 = 2d/pf = J_{ph}, \]

where \(d\) is the distance between points, \(p\) is the density of the medium, \(c\) is the speed of sound, \(k\) is the wave-number, and \(f\) is the frequency. In some derivations of \(J_{ph}\) in the literature, a point transducer is substituted for the real transducer and the conclusion is drawn that \(J_{ph} = 2d/pf\) is valid only for small transducers. Here, we see that substituting a point transducer for \(T\) means only that we use the alternate concept of \(J\) as given by Eq. 9 and the substitution in no way limits the shape or size of \(T\). A point is used because \(p_m\) is defined as the pressure at a point.

**B. Plane Waves**

The plane-wave or one-dimensional case is shown schematically in Fig. 4. Here, \(p_m\) is averaged over a plane \(A\) equal in area to the diaphragm of the transducer and parallel to the diaphragm. Boundary conditions are chosen so that only plane waves are propagated. The pressure and volume velocity amplitude will then be the same at all points and the ratio, or acoustic-wave impedance, will be \(pc/A\). However, the volume velocity in the wave moving to the left in Fig. 4 contains only half of the total velocity \(U\) emanating from the imaginary source at \(A\). Now, \(p_m\) is the pressure in the plane of the transducer and in the absence of the transducer. Thus,

\[ p_m/\frac{1}{2}U = pc/A, \] (11)

or

\[ J_{ph} = U/p_m = 2A/pc. \] (12)

For the ideal case, \(p_m\) and \(p_s\) would be uniform over \(A\). In practice, however, \(J_{ph}\) may be used in nearfield measurements of large piston transducers, and average values \(p_m\) and \(p_s\) are actually measured.

**C. Coupler**

Coupler reciprocity systems have very small chambers. The chambers are so small, in fact, and the boundaries are of such high impedance, that it is valid to assume that the instantaneous pressure in the chamber is everywhere the same, so that we have a zero-dimensional case. A precise definition of where \(p_m\) and \(p_s\) are measured becomes unnecessary. The pressure resulting from any volume velocity is found from the acoustical compliance of the system—that is, from the parallel combination of the medium and boundaries, including other transducers in the chamber. Thus, \(U/p_m = \omega C\). In most cases, the controlling compliance is the compliance \(C\) of the medium. The reciprocity parameter is then

\[ M/S = J_{ph} = \omega C. \] (13)

The compliance \(C\) must be measured or computed for the chamber with or without the transducers present, depending on how \(M\) and \(S\) are defined. The reciprocal transducer is, or is not, present, depending on whether \(p_m\) is the applied diaphragm pressure or the pressure in the absence of \(T\). The two other transducers of the usual reciprocity trio—that is, the sound source and the hydrophone—are, or are not, present, depending on whether \(p_s\) is defined as the chamber pressure in, or not in, the presence of the two transducers.

**D. Diffuse Sound**

In Diestel's diffuse-sound reciprocity method, the transducers are placed in those parts of a reverberant chamber where a diffuse sound field exists—that is, where the time average of the mean-square sound pressure is everywhere the same and the flow of energy in

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(a) Beatty's tube-reciprocity arrangement (a) when the reciprocal transducer \( T \) is receiving and (b) when \( T \) is transmitting; (c) is a schematic representation of Fig. 1 for the Beatty tube reciprocity case.

Substituting Eq. 17 in Eq. 16, gives Diestel's expression:

\[
J_{dt} = (2.1/r_f)(V/cT)^{1/2}
\]  

E. Tube

In Beatty's tube reciprocity, the transducer diaphragms are not of the same shape and area as the cross section of the tube. Both radial and longitudinal motions are present. The boundary conditions are, therefore, different from and more complex than those for the plane-wave case. It is a three-dimensional case, although the diameter of the tube is restricted to about \( \lambda /3 \).

A simplified picture of tube-reciprocity conditions is given here. The reader is referred to Beatty's paper for more detail. The conditions are shown in Figs. 5(a) and (b). The usual trio of transducers is represented by the source projector \( P \), the reciprocal transducer \( T \), and the hydrophone \( H \). The arrows indicate the directions of sound-energy flow in plane progressive waves. The radial mod.3s are present only near the transducers. Active electroacoustic absorbers terminate the tube and effectively place the terminal boundary an infinite distance away—to the left in Fig. 5(a) and in both directions in Fig. 5(b).

The receiving sensitivity of \( T \) is defined in terms of the plane-wave pressure in the plane \( A_m \) in the absence of, or without the effect of, the presence of \( T \).

The total real pressure at any position in the tube is the sum of the longitudinal plane-wave mode and the...
radial modes that are present only near the transducers. Since the plane-wave mode suffers no attenuation, the position of $A_m$ is arbitrary.

The transmitting response of $T$ is defined in terms of the pressure at the plane $A_s$ of the plane progressive waves traveling toward the right in Fig. 5(b). As with $A_m$, the position of plane $A_s$ is arbitrary. The hydrophone $H$ is assumed so small that it does not disturb the plane waves.

From the general reciprocity-parameter concept, the reciprocity parameter becomes the transfer admittance $U/\tilde{p}_m$ depicted in Fig. 5(c); $U$ is the volume velocity emanating from $A_m$ and $\tilde{p}_m$ is the plane-wave pressure at $A_m$. Figure 5(c) represents conditions that do not differ from those for the plane-wave case. The tube-reciprocity parameter, therefore, is $2A/pc$. We see, then, that the choice of the plane-wave reference pressures at $A_m$ and $A_s$ eliminates the complications introduced by the radial modes.

Beatty also describes a second (less useful) tube-reciprocity parameter that is applicable when the boundary conditions for $T$ transmitting differ from those for $T$ receiving. The direct approach using the general reciprocity parameter cannot be made under such conditions.

III. MEASURED AND IN SITU PARAMETERS

It follows from the general approach to reciprocity parameters that a reciprocity calibration can be performed under any boundary conditions. The initial assumptions of a linear, passive, reversible system must prevail, but these conditions are the rule rather than the exception. The usual problem is not whether a system is reciprocal, but how to determine the reciprocity parameter. In some cases of complicated or unknown boundary conditions, it is impossible to calculate the parameter. An alternative, then, is to measure $J$. In some special cases, the volume velocity being emitted by a transducer can be determined. The pressure produced at any place in the medium can be measured with a calibrated hydrophone. Thus, the ratio $J = U/\tilde{p}_m$ can be measured.

A second method is to conduct a reciprocity calibration of a hydrophone whose calibration is already known and then solve for the unknown parameter $J$. That is, the roles of $M$ as the unknown and $J$ as a known quantity can be reversed in the familiar equation

$$M = [(E_T/E_H)/(E_P/P_H)]J$$

for determining the sensitivity $M$ of a hydrophone from reciprocity-calibration measurements. The need for a calibrated hydrophone in both methods might seem to eliminate the need for, or usefulness of, a reciprocity calibration. That is, if a calibrated hydrophone is already available, why use a reciprocity calibration? One answer is that sometimes the boundary conditions are more stable over long periods of time (months, or even years) than is a hydrophone calibration. This is true of some ocean-bottom locations, for example. In such cases, an in situ reciprocity parameter can be measured with the aid of a calibrated hydrophone, and thereafter a reciprocity calibration can be made independently of the stability of the hydrophone calibration. A system exploiting the in situ reciprocity technique for calibration on the ocean bottom has been built, but not used.

IV. NEARFIELD CASE

The dependence of the reciprocity parameter on the definitions of $A_m$ and $A_s$ in the receiving and transmitting responses of the reciprocal transducer, and the usefulness of the general parameter concept can be further illustrated by considering a nearfield-free-field case. Suppose that the projector $P$ and hydrophone $H$ are points but the reciprocal transducer $T$ is large. Suppose, further, that the distance $d$ used is of such a magnitude that in the $P \rightarrow H$ measurement $P$ and $H$ are in the far fields of each other, but in the $P \rightarrow T$ and $T \rightarrow H$ measurements each is in the near field of $T$. The situation is depicted in Fig. 6. Now, define the transmitting sensitivity $S_T$ of the reciprocal transducer so that the reference transmitted pressure $\tilde{p}_H$ is the pressure at the position point of $H$ in Fig. 6(c). Also, define the receiving sensitivity $M_T$ of the reciprocal transducer in terms of a free-field pressure $\tilde{p}_m$ in a spherical wave of radius $d$ being emitted from $P$. Thus, both $S_T$ and $M_T$ have very special definitions and are dependent on the distance $d$. From the definitions, both $A_m$ and $A_s$ are points in a free field; therefore $J$ is the same as $J_{ph} = 2d/p_f$. Thus, $H$ can be calibrated in the near field of $T$ using the farfield parameter $J_{ph}$. This is a surprising conclusion, but a valid one. It can be corroborated by considering how $P$, $T$, and $H$ are affected in a conventional trio of farfield calibration measurements when $d$ becomes small. When $d$ is very large, the sensitivity of $H$ is given by

$$M_H = [(E_{TH}/E_{PH}/E_{PT})J_{ph}].$$

where $E$ is the voltage output of the receiving transducer, $I$ is the current into $T$, and the subscripts indicate the transducers used in each of the measurements. Now, if the farfield distance $d$ is reduced so that $P$ and $H$ are in the far field of each other but the near field of $T$, then $E_{PH}$ and $J_{ph}$ would be affected according to the inverse-square law, but the product $E_{TH}/J_{ph}$ would be constant. The voltages $E_{TH}$ and $E_{PT}$ would be affected according to some nearfield function of $d$, the frequency, and the dimensions of $T$. Since both $P$ and $H$ are points, and both transducer pairs ($T$--$H$ and $P$--$T$) constitute reciprocal systems, the function, whatever it is, will affect $E_{TH}$ and $E_{PT}$ equally and the ratio $E_{TH}/E_{PT}$ will be unaffected. Thus, Eq. 20 produces the same $M_H$ in this nearfield arrangement that it does in the far field.

pressure over the area of \( T \) produced by a point source at a distance \( d \)." Now, \( A_s \) is still a point, but \( A_m \) is the area of \( T \). In some simple cases, as when \( T \) is a uniform circular piston and \( A_s \) is a point on the axis, it is still easy to find \( J \) from the well-known formula for the axial pressure \( p \) as a function of source velocity \( u \):

\[
1/J = p/u = (2pc/\pi a^2)\left(\sin[k(a^2 + d^2)^{1/2} - d]\right)
\]

Equation 21 also is valid in the reciprocal sense—that is, when the axial point is the source and the piston is the receiver. When the reciprocity-calibration formula for \( M_H \) is derived for these conditions and definitions, we get

\[
M_H = \left[ \alpha(E_{TH}/E_{PT})L \right].
\]

The new factor \( \alpha \) is defined by \( \bar{p} = \alpha \bar{p} \), where \( \bar{p} \) is the average pressure over the area of \( T \) (or \( A_m \)) in Fig. 6(b), and \( p \) is the pressure in the spherical wave of radius \( d \). The difference between \( \bar{p} \) and \( p \) corresponds to the two different definitions of \( AMT \) in this nearfield case. It also corresponds to the difference in the reference sound pressure acting on \( T \) and on \( H \) in Figs. 6(a) and (b), and this is why it appears in Eq. 22. From the definition of \( \alpha \), it is evident that \( \alpha \) is equal to the ratio of Eq. 21 to the reciprocal of Eq. 10. Thus,

\[
\alpha = (1/J_z)/(1/J_{\text{bar}}) \text{ or }\]

\[
\alpha J_z = J_{\text{bar}}.
\]

The relationship in Eq. 24 could have been obtained merely by arguing that \( M_H \) must be independent of the calibration technique so that Eqs. 20 and 22 must be identical. The mathematical argument, however, shows that by choosing \( A_m \) as the area over \( T \), we needlessly complicate the reciprocity calibration. That
is, the right-hand member of Eq. 21 appears in both \( J_s \) and \( \alpha \) but drops out of the product \( \alpha J_s \). Therefore, rather than calculating \( J_s \) and \( \alpha \) separately, and then having the product \( \alpha J_s \) reduce to \( J_{np} \), it is simpler to define \( M_T \) and \( S_T \) such that \( J_{np} \) applies to begin with. This is what was done in the first nearfield case. In any practical case of a reciprocity-calibration technique, all the reference pressures should be defined for equal areas and \( A_s \) should be identical in shape and size to \( A_m \).

VI. SUMMARY

The reciprocity parameter in any reciprocity calibration is the acoustic transfer admittance \( \frac{U}{\bar{p}_m} \), where \( U \) is the volume velocity emanating from the surface \( A_s \), \( \bar{p}_m \) is the average pressure produced by \( U \) over the surface \( A_m \), \( A_s \) is the surface over which the pressure is averaged in the definition of the transmitting response, and \( A_m \) is the surface over which the pressure is averaged in the definition of the receiving sensitivity.
The reciprocity parameter used in the reciprocity calibration of electroacoustic transducers is derived for the general case of arbitrary boundary conditions and arbitrary definitions of responses. A general reciprocity parameter is defined as the ratio of the volume velocity emanating from a surface defined in the transmitting response to the resulting pressure averaged over a surface defined in the receiving response. It is shown how the general parameter concept leads directly and simply to the various special parameters for the cases of spherical waves, cylindrical waves, plane waves, diffuse sound, couplers, and tubes. Application of the concept to in situ and nearfield conditions is also described.
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