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A METHOD FOR THREE-DIMENSIONAL FLOW ANALYSIS IN A ROTOR USING A HIGH SPEED DIGITAL COMPUTER

DONALD L. FELT
A METHOD FOR THREE - DIMENSIONAL FLOW ANALYSIS IN A ROTOR USING A HIGH SPEED DIGITAL COMPUTER

* * * * *

Donald L. Felt
A METHOD FOR THREE - DIMENSIONAL
FLOW ANALYSIS IN A ROTOR
USING A HIGH SPEED DIGITAL COMPUTER

by

Donal d L. Felt
Lieutenant Commander, United States Navy

Submitted in partial fulfillment of
the requirements for the degree of
AERONAUTICAL ENGINEER

United States Naval Postgraduate School
Monterey, California

1963
A METHOD FOR THREE - DIMENSIONAL FLOW ANALYSIS IN A ROTOR USING A HIGH SPEED DIGITAL COMPUTER

by

Donald L. Felt

This work is accepted as fulfilling the thesis requirements for the degree of AERONAUTICAL ENGINEER

from the United States Naval Postgraduate School
ABSTRACT

Theoretical analyses of flow with rotating passages of turbo-machinery have become necessary for the proper design of turbo-pump elements in liquid fuel boosters and power conversion units. One such theory is presented, and a numerical solution derived. This theory develops a method for the analysis of steady, inviscid, adiabatic flow through arbitrary rotors. A detailed analysis in a meridional plane is given, assuming axial symmetry. A simplified approach to the blade to blade solution is also presented. The merits of these theories are compared with other proposed methods. The inverse, or design, approach is considered, and found to be unnecessary.

A numerical solution for incompressible flow is derived and applied to the flow solution in the impeller of a mixed flow compressor with backwards-bent blades of arbitrary shape. Meridional streamlines and relative velocity distributions are progressively calculated on a CDC 1604 computer, using FORTRAN program language. Data are measured from a detailed presentation of the blade shape in a meridional plane. Blade to blade relative velocity distributions are calculated from the meridional plane analysis.

It is concluded that the results completely define the flow and are sufficiently accurate for engineering applications. Validation is based upon the reliability of the theory, and upon comparisons with results of other methods. Extensions of the scope of this approach are recommended, which include the compressible solution and the solution of flows in unbladed passages.

The writer wished to express his appreciation for the assistance and encouragement given him by Professor M. H. Vavra of the U. S. Naval Postgraduate School. His guidance in the development of this solution was invaluable.
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<tr>
<td>A</td>
<td>Area</td>
<td>sq. in.</td>
</tr>
<tr>
<td>a</td>
<td>Coefficient</td>
<td></td>
</tr>
<tr>
<td>b</td>
<td>Coefficient</td>
<td></td>
</tr>
<tr>
<td>B</td>
<td>Blade thickness factor</td>
<td></td>
</tr>
<tr>
<td>C</td>
<td>Characteristic number</td>
<td></td>
</tr>
<tr>
<td>c</td>
<td>Coefficient</td>
<td></td>
</tr>
<tr>
<td>D</td>
<td>Grouping of terms</td>
<td></td>
</tr>
<tr>
<td>$E(x)$</td>
<td>Product of function on a characteristic</td>
<td></td>
</tr>
<tr>
<td>$\bar{F}$</td>
<td>Blade force</td>
<td>lb./slug</td>
</tr>
<tr>
<td>$F(L)$</td>
<td>Leading edge function</td>
<td></td>
</tr>
<tr>
<td>$\bar{f}$</td>
<td>Friction force</td>
<td>lb./slug</td>
</tr>
<tr>
<td>H</td>
<td>Total enthalpy</td>
<td>ft.lb./slug</td>
</tr>
<tr>
<td>h</td>
<td>Static enthalpy</td>
<td>ft.lb./slug</td>
</tr>
<tr>
<td>K</td>
<td>Separation parameter</td>
<td></td>
</tr>
<tr>
<td>$K(n)$</td>
<td>Entrance function</td>
<td></td>
</tr>
<tr>
<td>k</td>
<td>Curvature</td>
<td>in. $^{-1}$</td>
</tr>
<tr>
<td>L</td>
<td>leading edge distance</td>
<td>in.</td>
</tr>
<tr>
<td>l</td>
<td>$\Theta$ = constant curve distance</td>
<td>in.</td>
</tr>
<tr>
<td>M</td>
<td>Streamline number</td>
<td></td>
</tr>
<tr>
<td>$\bar{M}$</td>
<td>Moment about axis</td>
<td>lb./ft.</td>
</tr>
<tr>
<td>m</td>
<td>Streamline distance</td>
<td>in.</td>
</tr>
<tr>
<td>N</td>
<td>Number of blades</td>
<td></td>
</tr>
<tr>
<td>$dN$, $\Delta N$, $\delta N$, $dn^{*}$</td>
<td>Incremental distances along streamline</td>
<td>in.</td>
</tr>
<tr>
<td>n</td>
<td>Normal distance</td>
<td>in.</td>
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<th>Symbol</th>
<th>Definition</th>
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<tr>
<td>P</td>
<td>Arbitrary point</td>
<td></td>
</tr>
<tr>
<td>$P^*$</td>
<td>Point on Characteristic</td>
<td></td>
</tr>
<tr>
<td>p</td>
<td>Static pressure</td>
<td>lb./sq. in.</td>
</tr>
<tr>
<td>Q</td>
<td>Volumetric flow rate</td>
<td>cu. ft./sec.</td>
</tr>
<tr>
<td>R</td>
<td>Radius</td>
<td>in.</td>
</tr>
<tr>
<td>$R_e$</td>
<td>Reynold's Number</td>
<td></td>
</tr>
<tr>
<td>s</td>
<td>Entropy</td>
<td>ft. lb. / (slug °R)</td>
</tr>
<tr>
<td>T</td>
<td>Temperature</td>
<td>deg. R</td>
</tr>
<tr>
<td>t</td>
<td>Time</td>
<td>sec.</td>
</tr>
<tr>
<td>$\Delta t$</td>
<td>Blade thickness</td>
<td>in.</td>
</tr>
<tr>
<td>$\Delta t'$</td>
<td>Equivalent blade thickness</td>
<td>in.</td>
</tr>
<tr>
<td>V</td>
<td>Absolute velocity</td>
<td>ft./sec.</td>
</tr>
<tr>
<td>W</td>
<td>Relative velocity</td>
<td>ft./sec.</td>
</tr>
<tr>
<td>X</td>
<td>Coefficient</td>
<td></td>
</tr>
<tr>
<td>x</td>
<td>Distance along characteristic</td>
<td>in.</td>
</tr>
<tr>
<td>Z</td>
<td>Axial distance</td>
<td>in.</td>
</tr>
<tr>
<td>$\hat{u}, \hat{w}, \hat{n}$</td>
<td>Unit vectors in axisymmetric coordinate system</td>
<td></td>
</tr>
<tr>
<td>$\alpha$</td>
<td>Slope of leading edge</td>
<td>deg.</td>
</tr>
<tr>
<td>$\beta$</td>
<td>Blade or flow angle</td>
<td>deg.</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>Angular inclination of characteristic from normal</td>
<td>deg.</td>
</tr>
<tr>
<td>$\delta$</td>
<td>Angular inclination of $\theta$ = constant curve from normal</td>
<td>deg.</td>
</tr>
<tr>
<td>Symbol</td>
<td>Definition</td>
<td>Units</td>
</tr>
<tr>
<td>--------</td>
<td>------------</td>
<td>-------</td>
</tr>
<tr>
<td>$\varepsilon$</td>
<td>Angular deviation of blade from radial direction</td>
<td>deg.</td>
</tr>
<tr>
<td>$\Theta$</td>
<td>Circumferential reference angle</td>
<td>deg.</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>Slope of streamline</td>
<td>deg.</td>
</tr>
<tr>
<td>$\nu$</td>
<td>Kinematic viscosity</td>
<td>sq. ft./sec.</td>
</tr>
<tr>
<td>$\rho$</td>
<td>Density</td>
<td>slugs/cu. ft.</td>
</tr>
<tr>
<td>$\omega$</td>
<td>Angular velocity</td>
<td>per sec.</td>
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Subscripts

- **B**: Blade
- **e**: Entrance
- **H**: Hub
- **i**: Point on streamline
- **j**: Point on normal
- **k**: Point on characteristic
- **L**: Leading edge
- **l**: $\Theta = \text{constant curve}$
- **m**: Stream direction
- **n**: Normal
- **p**: Pressure side of blade
- **R**: Relative
- **s**: Suction side of blade
- **T**: Tip
- **u**: Circumferential direction
- **x**: Characteristic direction
- **0,1,2,3**: Sequential indices
A METHOD FOR THREE-DIMENSIONAL FLOW ANALYSIS IN A ROTOR USING A HIGH SPEED DIGITAL COMPUTER

INTRODUCTION

There is an increasing demand for compact, high speed, high power output turbomachines for use in liquid fuel rocket engines and power conversion units. These units are being designed to work with such media as cryogenics and liquid metals. The proper design of such machinery largely depends upon the accuracy of the theoretical analysis, used prior to fabrication. The method used should reasonably predict aerodynamic forces and tendencies toward flow separation and cavitation.

The more simplified approaches, using conditions ahead of and after the rotor, ignore conditions within the rotor passage itself, and therefore, are unsatisfactory. Potential flow analyses are useful for stationary cascades, but cannot be accurately applied to flows in rotating passages. The need for more precise methods, required for the proper analysis of modern rotor designs, was anticipated. Several three-dimensional theories have been postulated. In general, these theories are quite complex and are difficult to apply.

One such theory was developed by the NACA's Lewis Laboratory in the early 1950's. The three dimensional problem was reduced to an iterative process between two-
dimensional solutions on hub to tip, and blade to blade stream surfaces. Ref. 1 presents an analysis on a meridional, or hub to tip, surface. A similar approach is developed in Ref. 2. A blade to blade analysis is described in Ref. 3. These treatments were combined into a general theory in Ref. 4. Subsequent efforts were directed towards applications of this theory to specific examples. The complex nature of the theory required the introduction of certain simplifying assumptions. The development of the high speed digital computer made solutions more practical, as demonstrated in Refs. 5 through 7.

Prior to the NACA's work, a method of solution in a meridional plane, similar to that of Ref. 1, was developed by Meyer in Ref. 8. This method uses an iterative, graphical process to solve two simultaneous, linear differential equations along the characteristics of the equations. The equations are derived from the Eulerian equations of motion, and the characteristics are defined by the geometry of the flow channel. In Ref. 9, Vavra reorganized Meyer's scheme into a more general theory, reducing the equations of motion to one non-linear equation which is also solved along characteristics. In addition, a simplified blade-to-blade analysis was developed.

The purpose of this thesis is to transform the theoretical development of Ref. 9 into a method of solution for arbitrary rotors, using the CDC 1604 digital computer. A completely contained computer solution was presumed to
be quite long. It was anticipated that the amount of input data, required for acceptable accuracy, would exceed computer capacity and that long preparation and computer run time would be required. It was decided to use a series of short computations, which could be repeated as often, or at such intervals, as required to obtain the desired accuracy.

The theoretical development may be applied to both the design and inverse problems. The major portion of this thesis is devoted to the latter application; the analysis of flow in a given rotor. A design attempt is made to provide a physical model for the evaluation of the analytical methods. This attempt is not completed because of time considerations, and an actual rotor is used for the model. This impeller is a part of a compressor test rig located at the U. S. Naval Postgraduate School. Details of this machine are enumerated in Ref. 10. The rotor is of the mixed flow type, with non-radial blades. The blades have a constant thickness, and are of the deloaded type, with a reversal in curvature over the rear section. This configuration presents an arbitrary design which does not conform to standard impeller types.

The methods developed in this thesis are applied to this model, using simplified initial conditions, which do not reflect actual operating conditions, but are within the compressor's operating range. No correlation is made between theoretical and test results, however theoretical
results are presented for validation. Both the theory and the results of this analysis are compared with those of Refs. 1 through 7, to substantiate the applicability of this method.
II. THEORY

A complete derivation of the theory is presented in Ref. 9. This section contains those equations and developments that are considered necessary for clarity and continuity, in following the subsequent transformation from theory to numerical methods.

A. Meridional Plane Analysis

1. The following assumptions are made to establish a model for the hub to tip analysis. A more thorough treatment of these assumptions is conducted in Section IV.
   a. The rotor cascade contains an infinite number of infinitely thin blades. Thus, stream surfaces and fluid motion are axisymmetric.
   b. Flow is inviscid, steady, and isentropic.
   c. Entropy changes due to discontinuities at the leading and trailing edges are acknowledged but ignored.
   d. Flow is incompressible.

2. The solution of the equation of motion is based upon complete definition of the geometry of the blade surface. A set of meridional streamlines, \( m \), are assumed and the normals, \( n \), are drawn, establishing an orthogonal, axisymmetric coordinate system. This system is corrected by successive approximations. The blade surface is represented by the circular projection on the meridional plane of the lines of intersection of the blade surface with planes \( \theta = \text{constant} \). \( \theta \) is the angle measured in the
peripheral direction. The $\Theta$ constant planes are planes extending in a radial direction from the axis of rotation, perpendicular to that axis. The peripheral angle, $\Theta$, is referenced to an arbitrary point on the blade surface, usually on the leading edge. The $\Theta$=constant curves are shown in Fig. 1. Assumed coordinate systems are illustrated in Fig. 4.

The angles defined by this family of curves, at an arbitrary point, $P$, are shown in Figs. 2 and 3. The angle $\delta$ is the inclination of a $\Theta$=constant curve from the normal. The angle $\lambda$ is the inclination of a meridional streamline from the axial direction, $Z$. The angle $\beta$ is the flow angle of the relative velocity, $\bar{W}$, on the stream surface.

$$\tan \beta = R \frac{\Theta}{dm}$$

(1)

The deviation of a blade section, $\varepsilon$, from the radial direction, $R$, is:

$$\tan \varepsilon = \frac{\tan \beta \sin (\lambda - \delta)}{\cos \delta}$$

(2)

Thus, the system of streamlines and $\Theta$=constant curves are sufficient to completely define the blade shape.

The relative velocity on a streamline may be expressed vectorially as:

$$\bar{W} = \hat{u} \bar{W}_m \tan \beta + \hat{m} \bar{W}_m$$

(3)

where: $\hat{u}$ = unit vector in peripheral direction

$\hat{m}$ = unit vector in stream direction

The flow problem is reduced to a solution for the meridional component of the relative velocity, $\bar{W}_m$. 


3. The Eulerian equation of motion is:

\[ \frac{\partial \hat{\mathbf{w}}}{\partial t} + \nabla H = \hat{\mathbf{v}} \times (\nabla \times \hat{\mathbf{v}}) + \mathbf{T} \times \mathbf{s} + \hat{f} \]  

(4)

For steady, isentropic, relative flows:

\[ \nabla H_R = \hat{\mathbf{w}} \times (\nabla \times \hat{\mathbf{w}} + 2 \hat{\omega}) + \hat{f} \]  

(5)

where,

\[ H_R = h + \frac{w^2}{2} - \frac{\omega^2 R^2}{2} \]  

(6)

For inviscid flow, the friction force, \( \hat{f} \), is zero. However, the effect of infinitesimal pressure changes across an infinite number of blades is accounted for by introducing the blade force, \( \hat{F}_B \), which is normal to a blade element. Thus:

\[ \nabla H_R = \hat{\mathbf{w}} \times (\nabla \times \hat{\mathbf{w}} + 2 \hat{\omega}) + \hat{F}_B \]  

(7)

Eq. (7) is reduced to its scalar components, using:

\[ \frac{\partial \hat{\mathbf{w}}}{\partial \hat{\omega}} = 0 \]  

(8a)

\[ \hat{F}_B = F_u \left( \hat{\mathbf{u}} - \hat{\mathbf{n}} \tan \beta + \hat{\mathbf{m}} \tan \beta \tan \delta \right) \]  

(8b)

where: \( \hat{\mathbf{n}} = \) unit vector in normal direction

The \( \hat{\mathbf{u}} \) component yields:

\[ RF_u = W_m \frac{\partial (RW_u + \omega R^2)}{\partial m} \]  

(9a)

The \( \hat{\mathbf{m}} \) component, with Eq. (9a) gives:

\[ \frac{\partial H_R}{\partial m} = 0 \]  

(9b)

This relation only holds within the rotor for the assumed theoretical model. Flows outside the rotor are unaffected by such a model.
For all but design conditions, there is a flow discontinuity at the leading edge, since flows ahead of the rotor will not meet the rotor at blade entry angles. It has been assumed that entropy changes caused by these discontinuities are neglected by ignoring the changes in total enthalpy across the leading edge. Conditions ahead of the rotor are derived from Eq. (4) for steady, isentropic flow.

\[ \frac{\partial H}{\partial m} = \frac{V}{R} \frac{\partial (RV)}{\partial m} = 0 \]  

(10)

A relation between conditions on a streamline ahead of the rotor and within the rotor is established as:

\[ H_R = H_e - \omega R_L (W_{uL} + \omega R_L) \]  

(11)

where \( e \) and \( L \) denote entrance and leading edge stations.

The change of \( H_R \) along a normal is:

\[ \frac{\partial H_R}{\partial n} = \frac{\partial H_e}{\partial n} \frac{\partial n_e}{\partial n} - \omega \frac{\partial (R_L W_{uL} + \omega R_L^2)}{\partial L} \frac{dL}{dn} = K(n) \]  

(12)

The \( \hat{n} \) component of Eq. (7) becomes:

\[ W_m \frac{\partial W_m}{\partial n} + W_m^2 k_m + \frac{W}{R} \frac{\partial (RW_{uL} + \omega R^2)}{\partial n} \]

\[ + \frac{W_m}{R} \frac{\partial (RW_{uL} + \omega R^2)}{\partial m} \tan \beta \tan \delta = K(n) \]  

(9c)

where \( k_m \) is the curvature of the meridional streamline.

From Fig. 3:

\[ W_u = W_m \tan \beta \]  

(13)
Eq. (9c) is reduced to a relation in $W_m$:

$$\frac{\partial W_m^2}{\partial n} (1 + \tan \alpha) + \frac{\partial W_m^2}{\partial m} (\tan^2 \beta \tan \delta) + W_m^2 (2 k_m + 2 \frac{\tan \beta}{R} \left[ \frac{\partial (R \tan \beta)}{\partial n} + \tan \delta \frac{\partial (R \tan \beta)}{\partial m} \right]) (14)$$

$$+ W_m (4 \omega \tan \beta \left[ \frac{\partial R}{\partial n} + \tan \delta \frac{\partial R}{\partial m} \right])$$

$$= 2 K(n)$$

The partial derivatives in brackets are reduced to a total derivative along a $\Theta =$-constant curve by:

$$\frac{d}{dl} = \sin \delta \frac{d}{dm} + \cos \delta \frac{d}{dn}$$

Eq. (14) becomes:

$$\frac{\partial W_m^2}{\partial n} + \sin^2 \beta \tan \delta \frac{\partial W_m^2}{\partial m} + W_m^2 \left( 2 k_m \cos^2 \beta \right)$$

$$+ \frac{\sin (2 \beta)}{R \cos \delta} \frac{d}{dl} (R \tan \beta) + W_m \omega \left( \frac{2 \sin (2 \beta)}{\cos \delta} \frac{dR}{dl} \right)$$

$$= 2 \cos^2 \beta \ K(n)$$

Eq. (16) is reduced to an ordinary differential equation along a characteristic, whose tangents at any point satisfy the relation:

$$\tan \gamma = \sin^2 \beta + \tan \delta$$

(17)

According to Ref. 8, these characteristics are regarded as circular projections on a meridional plane of unique spatial lines lying on the blade surface. Introducing Eq. (17) into Eq. (16):

$$\frac{dW_m^2}{dx} + W_m \gamma_1 + W_m \omega \gamma_2 = \gamma_3$$

(18)
where $x$ denotes distance along a characteristic, and:

$$Y_1 = \cos \gamma \left[ 2 R_m \cos^2 \beta + \frac{\sin(2\beta)}{R \cos \delta} \frac{d(R \tan \beta)}{dl} \right]$$  \hspace{1cm} (19a)$$

$$Y_2 = 2 \cos \gamma \frac{\sin(2\beta)}{\cos \delta} \frac{dR}{dl}$$  \hspace{1cm} (19b)$$

$$Y_3 = 2 \cos \gamma \cos^2 \beta \ k(n)$$  \hspace{1cm} (19c)$$

4. The value of $k(n)$ is dependent upon conditions ahead of the rotor, as shown by Eq. (12). The normal component of the equation of motion for steady, isentropic flows ahead of the rotor blading is:

$$V_m \frac{\partial V_m}{\partial n} + V_m \frac{\partial^2}{\partial n^2} - \frac{\partial H}{\partial n} = 0 \hspace{1cm} (20)$$

Eq. (10) shows that for isentropic conditions at the entrance, the total enthalpy and the product $R V_u$ are constant along a meridional streamline. This condition is proved from the $\hat{u}$ and $\hat{m}$ components of Eq. (4). Thus:

$$\frac{\partial V_m^2}{\partial n} + V_m \frac{\partial V_m}{\partial n} X_1 + X_2 = 0 \hspace{1cm} (21)$$

$$X_1 = 2 R_m \hspace{1cm} (22a)$$

$$X_2 = \frac{V_u}{R} \frac{\partial (RV_u)}{\partial n} - \frac{\partial H}{\partial n}$$

$$= V_u e \left[ \frac{\partial (RV_u e)}{\partial n} - \frac{\partial H e}{\partial n} \right] \frac{dne}{dn} \hspace{1cm} (22b)$$

The solution of Eq. (21) is:

$$V_m^2 = e^{-\int X_1 dn} \left[ V_{mH}^2 - \int X_2 e^{\int X_1 dn} dn \right] \hspace{1cm} (23)$$
This solution is solved for given entrance conditions and the volumetric flow rate, \( Q \), by iterating the hub velocity, \( V_{\text{mH}} \), until the flow rate is satisfied by:

\[
Q = 2\pi \int_{H}^{T} RV_{\text{m}} \tan \beta \, d\eta
\]  

(24)

At the leading edge:

\[
W_{\text{UL}} = V_{\text{m}} \tan \beta
\]  

(25)

Thus, \( K(n) \) is solved for given entrance conditions.

5. The remaining terms of Eqs. (19) are determined from blade geometry and the orientation of the meridional streamlines within the rotor. These streamlines must be assumed and corrected by successive approximations. The location of the streamlines at the leading edge are determined from entrance conditions. Eq. (18) is solved along a characteristic until the flow rate is satisfied by:

\[
Q = 2\pi \int_{0}^{\chi_{T}} R W_{\text{m}} \cos \chi \, d\chi
\]  

(26)

B. **Blade to Blade Analysis**

1. It is assumed that the relative velocity varies linearly across the blade channel. This assumption is taken from thin airfoil theory, where blade profiles are replaced by bound vortices. The relative velocity from the axisymmetric solution is considered to be the mean velocity along the periphery at any point in the meridional plane. These assumptions lead to:

\[
W_{P} = W - \Delta W
\]  

(27a)

\[
W_{3} = W + \Delta W
\]  

(27b)
where \( p \) and \( s \) refer to the pressure and suction sides of the blade.

2. The difference between relative velocities across the blade is related to the static pressure difference by:

\[
\rho + \frac{c}{2} \omega^2 = \text{constant}\]

(28)

Thus:

\[
\Delta \omega = \frac{\Delta p}{2 \rho \omega}
\]

(29)

The pressure difference across a blade element, which is projected onto a meridional plane, is related to the moment about the axis of rotation, exerted by the flow on that element, by:

\[
\Delta \vec{M} = -\frac{\sigma}{\omega} (R \Delta p \, dn \, dm)
\]

(30)

This moment is also derived from the momentum theorem and Eq. (9a):

\[
\Delta \vec{M} = -\frac{\sigma}{\omega} \left[ R \Delta \Theta \, dn \, dm \, \omega \left( RW_n + \omega R^2 \right) \right]
\]

(31)

The minus sign indicates that the moment opposes the rotation of the rotor. The arc, \( \Delta \Theta \), is expressed in terms of an equivalent blade thickness, \( \Delta t' \), which is measured perpendicular to the meridional plane.

\[
\Delta t' = \frac{\Delta t}{\cos \beta} \sqrt{1 + \sin^2 \beta \cos \delta}
\]

(32)

\[
\Delta \Theta = \frac{2 \pi}{N} - \frac{\Delta t'}{R}
\]

(33)

where: \( N \) = number of blades

\( \Delta t = \) blade thickness
Equating Eqs. (30) and (31) and combining with Eqs. (29) and (33):

\[ \Delta W = \left( \frac{2\pi}{N} - \frac{\Delta t}{R} \right) \cos \frac{\beta}{2} \frac{\partial (R W_m \tan (\beta + \omega R^2))}{\partial m} \]
III. NUMERICAL SOLUTIONS

A. Design or Inverse Solution

1. The application of the preceding theory to impeller design was investigated in an attempt to produce a physical model for the direct solution, or flow analysis. Overall dimensions of an axial entry, mixed flow pump impeller were provided by Professor Vavra, which included:
   a. Hub and tip profiles of meridional contour
   b. Leading and trailing edge contours in a meridional plane
   c. Blade entry and exit angles

The problem was reduced to that of determining blade shapes, which would not only satisfy these boundary conditions, but would conform to practical structural and aerodynamic limitations.

2. A drawing was made of the meridional plane and a series of approximate normals were constructed. A meridional streamline was constructed, dividing the rotor annulus in half.

\[ A_{1/2} = \pi (R_m + R_H) \eta_m \]  

(35a)

Iterations were made on \( R_m \) along a normal until:

\[ A_{1/2} = \frac{\pi}{2} (R_T + R_H) \eta_T \]  

(35b)

The slope of this streamline, \( \lambda \), was measured, plotted, smoothed, and the streamline reconstructed. Normals were corrected.

The distribution of the flow angle, \( \Theta \), along the mean streamline was assumed in the form:
\[ \beta = A + B m^2 \]  

(36)

A and B were evaluated from initial conditions at the leading and trailing edges. Values of \( \Theta \) were calculated by numerical integrations (Ref. 11). From Eq. (1):

\[ \Theta_i = \Theta_{i-1} + \int_{i-1}^i \frac{\tan \beta}{R} \, dl \]  

(37)

where:

\[ \Theta_L = 0 \]

The slope of the \( \Theta = \text{constant} \) curves at any point on a streamline may be calculated by Eq. (2), if \( \varepsilon \) is known.

The choice of an \( \varepsilon \) distribution is governed by:

a. Maximum \( \varepsilon \) is limited by structural considerations

b. \( \varepsilon \) distribution must be compatible with fabrication tooling practices. An example is given in Ref. 9.

The design problem could have been simplified by using radial blades, where \( \varepsilon = 0 \). However, this is contrary to the intent of this thesis in presenting methods applicable to arbitrary designs. Therefore, several \( \varepsilon \) distributions were assumed, and the angles, \( \delta \), computed on the mean streamline.

3. The problem of analytically generating a complete family of \( \Theta = \text{constant} \) curves was as yet unsolved. The \( \beta \) and \( \varepsilon \) distributions on streamlines other than the mean are not independent of the mean distributions. Arbitrary choice of these distributions would, in all probability,
generate impractical blade shapes. These distributions should be assumed as:

\[ \beta = \beta(m,n) \]

\[ \epsilon = \epsilon(m,n) \]

It appeared that the design problem had become more complex than originally anticipated. It was decided that a complete treatment would detract from the main objective of this thesis. Therefore, the design analysis was discontinued.

B. Meridional Plane Analysis

1. The approach used to solve Eq. (18) along a chosen number of characteristics is, briefly:

   a. Assume meridional streamlines in the vicinity of the leading edge which divide the flow into approximately equal increments.

   b. Construct normals, thus establishing a coordinate grid system.

   c. Measure the necessary blade physical characteristics at each grid point.

   d. Generate a characteristic curve within the grid system.

   e. Compute the coefficients, \( Y \), of Eqs. (19).

   f. Solve Eq. (18) for \( \overline{W}_m \) at the intersections of the characteristic with the streamlines, iterating \( \overline{W}_{mH} \) until the flow rate is satisfied.

   g. Correct these intersections until the streamlines divide the flow rate into the prescribed increments.

   h. Recompute \( \overline{W}_m \) at the new intersections.
i. Project the corrected streamlines farther into the rotor channel, and repeat the process for a new characteristic.

Thus, the meridional streamlines are generated from leading to trailing edge, and the distribution of the relative velocity on a meridional plane of the rotor is computed. Steps a, b, c, and i are solved by the computer. The remaining steps are carried out by graphical means.

2. There are two categories of initial data required. The first is a complete physical description of the rotor. Finally, flow conditions ahead of the rotor must be prescribed. Normally, sufficient data are available from drawings of the impeller to construct a meridional plane. The $\Theta =$constant curves are best produced by orthogonal projections from a three-view drawing. The meridional plane for the impeller used in this analysis is shown in Fig. 1.

The flow conditions at an entrance station must either be prescribed from an analysis of the machine installation, or assumed. The specific data required are:

a. Thermodynamic data for the fluid
b. Velocity distribution
c. Flow rate
d. Inlet channel contours
e. Impeller RPM

Conditions for this analysis are simplified by assuming:
This flow is somewhat impractical since it does not reflect actual velocity and energy distributions imposed by intake ducting or guide vanes. However, these distributions do present a definite off-design condition at the leading edge. Design RPM, and a flow rate compatible with actual machine operating conditions, are used. Initial data are listed in Table I. The meridional velocity at the leading edge was computed by:

$$V_m = \frac{Q}{A_L}$$  \hspace{1cm} (38)

$A_L$ was computed along the leading edge by Eq. (35b).

3. Streamlines are extended from initial points on the leading edge, such that the flow rate is divided into equal increments. Eight divisions were used for this analysis, as shown in Fig. 4.

A grid system is constructed in the vicinity of the leading edge. A point on the hub streamline is chosen as the starting point of the first characteristic. This point is determined by predicting the approximate alignment of the characteristic. Eq. (17) indicates that the slope of the characteristic, $\gamma$, is proportional to, but less than, the slope of the $\Theta=$constant curve which originates from the starting point. $\gamma$ also has the same sign as $\delta$. These guidelines fix the characteristic within a desired region. These considerations also assist in estimating...
the proper grid width. A "starting normal" is constructed from the starting point on the hub to the tip streamline. A second normal is constructed adjacent to the first, in the predicted direction of the characteristic. The distance between the two normals on each streamline is used to fix the remaining grid points. These points do not coincide with true normals, however equal grid spacing on streamlines is used to good advantage in subsequent calculations.

The values of $\lambda$, $R$, and $Z$ are measured at each grid point. The values of $\Theta$ were read at the intersections of the $\Theta$=constant curves and the streamlines, plotted, and $\Theta$ at the grid points found by interpolation. The angles $\delta$ are determined in a similar manner. The deviations of the $\Theta$=constant curves from the radial direction, $\delta-\lambda$, are measured. $\lambda$ is added to the interpolated results to obtain $\delta$.

4. Each point on a characteristic must satisfy Eq. (17), therefore, the angles $\beta$ and $\delta$ must be calculated for any point on a streamline. $\beta$ is defined by Eq. (1). The derivative of $\Theta$ at a grid point on the $j^{th}$ streamline is approximated by five-point difference formulas from Ref. 12. Forward Differences

$$\frac{d\Theta}{d\gamma_j} = \frac{-25\Theta_i + 48\Theta_{i+1} - 3\Theta_{i+2} + 16\Theta_{i+3} - 3\Theta_{i+4}}{12 \Delta N_j}$$
Central Differences

\[ \frac{d\Theta_i}{dm_j} = \frac{(\Theta_{i-2} - \Theta_{i+2}) - 8(\Theta_{i-1} - \Theta_{i+1})}{12 \Delta N_j} \]  

(39b)

Backward Differences

\[ \frac{d\Theta_i}{dm_j} = \frac{3 \Theta_{i-4} - 16 \Theta_{i-3} + 36 \Theta_{i-2} - 48 \Theta_{i-1} + 25 \Theta_i}{12 \Delta N_j} \]  

(39c)

\( \Delta N_j \) is the grid spacing on the \( j \)th streamline. The derivative of \( \Theta \) at points other than grid points, are calculated by interpolating linearly between adjacent normals.

\[ \frac{d\Theta^*}{dm_j} = \frac{d\Theta_i}{dm_j} + \left( \frac{d\Theta_{i+1}}{dm_j} - \frac{d\Theta_i}{dm_j} \right) \frac{dN}{\Delta N_j} \]  

(40)

\( dN \) is the distance from the \( i \)th grid point to the point \( P^* \).

A consequence of Eqs. (39) and (40) is that the minimum width of the coordinate lattice is six grid points.

The values of \( R, \lambda, \) and \( \delta \) at a point \( P^* \) are also calculated by linear interpolation. \( \beta \) and \( \gamma \) are calculated by Eqs. (1) and (17).

5. A characteristic is approximated by a polygon with each side terminated by adjacent streamlines. Each intersection, \( P^* \), is located from information calculated at the preceding intersection. In this derivation, the lines between grid points are assumed to be straight. The derivation is shown graphically in Fig. 5.

Assume that \( P_0 \) is established, and the angle \( \gamma \), known. A straight line from \( P_0 \) to \( P' \) on the next streamline at the angle \( \gamma \). The distance, \( dN' \) is:

\[ dN' = dM \tan \gamma \]  

(41)
where:
\[ dM = \frac{\frac{dR}{\cos \lambda}}{\cos \lambda} \]  
(42a)

or:
\[ dM = \frac{\frac{d\varphi}{\sin \lambda}}{\sin \lambda} \]  
(42b)

Eq. (42b) is used for \( \lambda \) greater than 45 degrees. The angle \( \gamma' \) is calculated by the methods of paragraph 4. A line is extended from \( P_0 \) to \( P'' \) at this angle. The point \( P^* \) is established by:
\[ dN = dN' + \frac{\delta N}{2} \]  
(43)

\( P^* \) is the reference point for the extension of the characteristic to the next streamline. The polygonal approximation of the completed characteristic is smoothed through the points \( P^* \). (Fig. 4)

There are a number of considerations that must be accounted for in generalizing this method for computer programming. \( dN^* \) originates at the starting normal. The sign of \( dN' \) is the same as that of \( \gamma \). The sign of \( \delta N \) depends on the difference between \( \gamma \) and \( \gamma' \). The sign of \( dN^* \) may be plus or minus, and its magnitude may be greater or less than that of \( dN' \). The value of \( dN \) in Eq. (40) for a positive \( dN^* \) is:
\[ dN = dN^* \]  
(44a)

while, for negative \( dN^* \):
\[ dN = \Delta N - dN^* \]  
(44b)

6. The coefficients, \( Y \), of Eq. (18) contain four elements which are, as yet, undetermined.

a. \( k_m \)
The curvature, $k$, of a given curve is extremely difficult to calculate. If the curve can be expressed analytically:

$$k = \frac{R''}{[1 + (R')^2]^{3/2}}$$

(45)

where $R'$ and $R''$ are the first and second derivatives, respectively, of the function $R = f(Z)$.

An attempt was made to determine the equations of the hub and tip contours in cartesian coordinates: $R = f(Z)$. Two polynomial approximations of these curves were made using CDC Cooperative Library routines. The coordinates of the curves at each quarter inch along the axis were introduced as data. Only high order polynomials fit these data points properly. The derivatives of these equations were difficult to obtain without frequent interruptions in computer operation. When calculated, the second derivatives reflected the sinuous nature of polynomial approximations, resulting in inaccurate curvatures which varied in sign along a given curve. These methods were considered to be unacceptable for this study.

The derivatives of the hub and tip contours were calculated with various finite difference equations. (Ref. 12) The three and four point calculations were inaccurate. The higher order solutions resulted in erratic second derivatives. It became apparent that all methods were very sensitive to the accuracy of the data. It was found that
inaccuracies in the third decimal place of radius data were sufficient to introduce gross errors in the second derivative.

A semi-graphical approach was used to determine the derivatives. The first derivative was calculated by finite differences, and the results plotted and smoothed. This process was repeated to calculate the second derivative, using the plot of the first derivative for input. Data taken from the two plots were used to calculate the curvature in Eq. (45). Hub and tip curvatures are plotted in Fig. 6.

This procedure is obviously incompatible with continuous computer operations. The computation of the streamline curvatures, $k_m$, at points $P^*$, would be quite tedious using this method. Therefore, $k_m$ is approximated within the flow passage by linearly interpolating between hub and tip, using the data of Fig. 6. $k_m$ is assumed to vary in equal increments between streamlines:

$$k_{m_j} = k_{m_H} + \left(k_{m_T} - k_{m_H}\right) \frac{M_j}{M_T} \tag{46}$$

Linear interpolation, similar to Eq. (40), is used to calculate $k_m$ between grid points on a streamline.

The following derivation defines $\frac{d}{dl} (R \tan \beta)$ in terms of known quantities. From Eq. (15):

$$\frac{d}{dl} (R \tan \beta) = \sin \delta \frac{\partial (R \tan \beta)}{\partial m} + \cos \delta \frac{\partial (R \tan \beta)}{\partial n} \tag{47}$$

$$= R \left( \sin \delta \frac{\partial \tan \beta}{\partial m} + \cos \delta \frac{\partial \tan \beta}{\partial n} \right) + \tan \beta \frac{dR}{dl}$$
From Fig. 2:
\[
\frac{dR}{dl} = \cos(\delta - \lambda) = D_1
\]  
(48)

From Eq. (1):
\[
\frac{\partial (R \tan \beta)}{\partial m} = R \frac{\partial^2 \theta}{\partial m^2} + \frac{\partial \theta}{\partial m} \cdot \frac{dR}{dm}
\]
\[
\frac{\partial (R \tan \beta)}{\partial n} = R \frac{\partial^2 \theta}{\partial m \partial n} + \frac{\partial \theta}{\partial m} \cdot \frac{dR}{dn}
\]
\[
\frac{d(R \tan \beta)}{dl} = R^2 (\sin \delta \frac{d^2 \theta}{dm^2} + \cos \delta \frac{d^2 \theta}{dm \partial n}) + 2D_1 \tan \beta
\]

Grouping terms of Eq. (19a):
\[
\frac{1}{R \cos \delta} \frac{d(R \tan \beta)}{dl} = D_2 = R \left( \tan \delta \frac{d^2 \theta}{dm^2} + \frac{d^2 \theta}{dm \partial n} \right)
\]
\[
+ \frac{2D_1 \tan \beta}{R \cos \delta}
\]  
(49)

The term \( \frac{d^2 \theta}{dm^2} \) at a point \( P^* \) is computed by assuming a parabolic distribution of \( \frac{d \theta}{dm} \) between grid points.

\[
\frac{d \theta}{dm} = a + bm + cm^2
\]  
(50)

\[
a = \frac{d \theta}{dm} \text{ at } P^* = \frac{\tan \beta}{R}
\]

\[
b = \frac{d^2 \theta}{dm^2} \text{ at } P^*
\]  
(51)

Fig. 7 will assist in following the derivation for \( b \).

\[
m_2 \left( \frac{d \theta}{dm} \right)_1 = \left( a + bm_1 + cm_1^2 \right) m_2^2
\]  
(52a)

\[
m_1 \left( \frac{d \theta}{dm} \right)_2 = \left( a + bm_2 + cm_2^2 \right) m_1^2
\]  
(52b)
Subtracting Eq. (52b) from (52a):

\[ b = m_2 \left[ \left( \frac{de}{d\theta} \right)_1 - \left( \frac{de}{d\theta} \right)_0 \right] - m_1 \left[ \left( \frac{de}{d\theta} \right)_2 - \left( \frac{de}{d\theta} \right)_0 \right] \]

\[ m_1, m_2^2 - m_2 m_1^2 \]  

(53)

\( m_1 \) and \( m_2 \) are defined in Fig. 8.

The function, \( \frac{d^2 \theta}{dm \sigma} \), is calculated by differentiating \( \frac{d\theta}{dm} \) along the normal nearest the point \( P^* \). A parabolic distribution of \( \frac{d\theta}{dm} \) over three streamlines along the normal is assumed. The coefficient, \( b \), is derived in the same manner as that described in the preceding paragraph. In this derivation the two succeeding grid points from the origin are used, instead of adjacent points. Calculations for points on the last two streamlines are made by using the two preceding grid points.

**Forward Differentiation**

\[ b = \frac{n_2^2 \left[ \left( \frac{de}{d\theta} \right)_1 - \left( \frac{de}{d\theta} \right)_0 \right] - n_1^2 \left[ \left( \frac{de}{d\theta} \right)_2 - \left( \frac{de}{d\theta} \right)_0 \right]}{n_1 n_2^2 - n_2 n_1^2} \]  

(54a)

**Backward Differentiation**

\[ b = \frac{n_{-2}^2 \left[ \left( \frac{de}{d\theta} \right)_{-1} - \left( \frac{de}{d\theta} \right)_0 \right] - n_{-1}^2 \left[ \left( \frac{de}{d\theta} \right)_{-2} - \left( \frac{de}{d\theta} \right)_0 \right]}{n_{-1} n_{-2}^2 - n_{-2} n_{-1}^2} \]

(54b)

The increments \( n_j \) are functions of the grid spacing, \( dM \).

The values of \( K(n) \) are required for the calculation of \( Y_3 \). Initial conditions have simplified Eq. (12). With Eq. (25):

\[ K(n) = - \omega \frac{2 \left( R_L V_m \tan \beta_L + \omega R_L^2 \right)}{\partial L} \frac{dL}{dn} \]

(55)

\[ \omega = \frac{\Pi}{30} \cdot RPM \]

(56)

\[ \frac{dL}{dn} = \frac{dL}{dn} \cdot \frac{dR}{dn} = \frac{\cos \lambda}{\sin \alpha} \]

(57)
where $\alpha$ is the slope of the leading edge. $\beta_L$ is calculated, using the forward difference formula of Eq. (54a) in conjunction with Eq. (1). The terms in parentheses in Eq. (55) are grouped, and the derivative calculated using the parabolic distribution methods of Eqs. (54).

\[ F(L) = R_L V_m \tan \beta_L + \omega R_L^2 \]  

In summary, the coefficients, $Y$, are reduced to:

\[ Y_1 = \cos \gamma \left[ 2 k_m \cos^2 \beta + \sin (2 \beta) \cdot D_2 \right] \]  
\[ Y_2 = 2 \cos \gamma \frac{\sin (2 \beta)}{\cos \delta} \cdot D_1 \]  
\[ Y_3 = 2 \cos \gamma \cos^2 \beta \cdot K(n) \]  

7. The equation of motion, Eq. (18), is solved by successive approximations, until the distribution of $W_m$ along the characteristic satisfies the flow rate of Eq. (26).

The steps in this solution are:

a. Assume $W_{mH}$

b. Solve Eq. (18) for $\frac{dW_{mH}^2}{dx}$

c. Let:

\[ W_{m2} = W_{mH} + \frac{dW_{mH}^2}{dx} \, dx \]  

\[ dx = \frac{dM_2}{\cos \gamma_H} \]  

d. Solve Eq. (18) for $\frac{dW_{m2}^1}{dx}$

e. Let:

\[ W_{m2}^1 = W_{mH} + \frac{1}{2} \left( \frac{dW_{mH}^2}{dx} + \frac{dW_{m2}^1}{dx} \right) \, dx \]  

f. Repeat for $W_{m3}$, using $W_{m2}$ in (a).

The variables under the integral sign in Eq. (26) are grouped.
Numerical integrations are performed over two adjacent streamlines at a time, and the results are successively summed. A parabolic distribution is assumed for $E(x)$.

$$E(x) = a + bx + cx^2$$  \hspace{1cm} (64)

The coefficients are derived in the same manner as that used for the development for the difference equations.

$$a = E_0$$  \hspace{1cm} (65a)

$$b = \frac{x_2^2(E_1 - E_0) - x_1^2(E_2 - E_0)}{x_1x_2^2 - x_2x_1^2}$$  \hspace{1cm} (65b)

$$c = \frac{x_2(E_1 - E_0) - x_1(E_2 - E_0)}{x_1^2x_2 - x_2^2x_1}$$  \hspace{1cm} (65c)

where:

$$x_1 = \int dx_i$$

$$x_2 = \int dx_1 + \int dx_2$$

The integral of $E(x)$ is:

$$\int_{k}^{k+2} E(x) dx = a(x_{k+2} - x_k) + \frac{b}{2}(x_{k+2}^2 - x_k^2)$$

$$+ \frac{c}{3}(x_{k+2}^3 - x_k^3)$$  \hspace{1cm} (66)

where:

$$x_k = \sum_{i=2}^{k} dx_i$$  \hspace{1cm} (67)

In case there exists an odd number of streamtubes, the final integral is calculated by:

$$E(x) = a + bx$$  \hspace{1cm} (68)

$$a = E_0$$  \hspace{1cm} (69a)
\[ b = \frac{E_i - E_o}{dX_i} \quad (69b) \]

\[ \int_{k}^{k+1} E(x) \, dx = d\left(x_{k+1} - x_k\right) + \frac{b}{2} \left(x_{k+1}^2 - x_k^2\right) \quad (70) \]

8. The intersection of the characteristic with each streamline, excluding hub and tip, is connected until adjacent streamlines divide the flow rate into M-1 equal increments. Calculations progress from streamline M-1 to streamline 2. Each calculation iterates the increment \( \delta x \) until:

\[ Q \left(\frac{K}{M}\right) = 2\pi \int_{T}^{K} E(x+\delta x) \, (dx+\delta x) \quad (71) \]

\[ K = M-1, M-2, \ldots \ldots 2 \]

The variables in \( E(x) \) are corrected by \( \delta x \).

\[ R_K = R_i + \left(\frac{dR}{dx}\right)_i \delta x \]
\[ = R_i + \delta x \cos (\gamma_i - \lambda_i) \quad (72) \]

\[ W_{mk} = W_{mi} + \left(\frac{dW_m}{dx}\right)_i \delta x \]
\[ = W_{mi} + \frac{\delta x}{2W_{mi}} \left(\frac{dW_m}{dx}\right)_i \quad (73) \]

\[ \gamma_K = \gamma_i + \left(\gamma_{i+1} - \gamma_i\right) \frac{\delta x}{dX_i} \quad (74) \]

\( K \) indicates the new point of intersection, and i, the original point. Eq. (71) is solved by introducing the proper limits into Eqs. (66) or (70).

9. Preliminary calculations for the blade to blade solution are included in the computer program for the meridional plane analysis. Variables of Eq. (34) are grouped,
and the groupings computed at the corrected intersections of the characteristic and streamlines.

\[ DW_{\text{cos}} = \left( \frac{2\pi}{N} - \frac{A\ell'}{R} \right) \cos \beta \]  

(75a)

\[ DW_{\text{func}} = RW_m \tan \beta + \omega R^2 \]  

(75b)

C. Computer Programs; ROTOR 1 and LEDGE 1

1. The preceding methods are translated into FORTRAN computer language compatible with the CDC 1604 digital computer. Program ROTOR 1 calculates a complete solution for one characteristic, from the location of the characteristic to the correction of assumed streamlines and the relative velocity profile. The solution proceeds in an orderly fashion, much like the development of the preceding section. Subroutines are used for repetitive calculations. Control of decisions, iterations, and progressive development is maintained in the main program. Subroutine PSTAR locates the characteristic, accounting for all signs of $dN^*$. Subroutine DDM calculates the first derivative of $\Theta$, $\frac{d\Theta}{dm}$, by finite differences. Subroutine ANGLE calculates $\beta$ and $\gamma$. Subroutine COY calculates the elements of the coefficients, $Y$, except $K(n)$. The coefficients, $Y$, are calculated in the main program. The relative velocities are calculated in subroutine RELVEL, and the flow rate in subroutine FLOW. Control of the iterations is maintained in the main program. Iterations for streamline corrections are made in the main program, using subroutine FLOW.
2. Entrance conditions are calculated in a separate program, since these computations are not required after the locations of streamlines on the leading edge are determined. Program LEDGE 1 calculates $K(n)$ as defined by Eqs. (55), (56), and (57), with the exception that $\cos \lambda$ is omitted. This variable is a function of position on a streamline, and therefore is included in the calculations for $Y_3$. The results of LEDGE 1 are used as inputs to Rotor 1.

It should be noted that the first term of $K(n)$ in Eq. (12) is omitted, since $\frac{\partial He}{\partial n_e} = 0$ in this analysis. This term is introduced as input (DHEDN) into Rotor 1. It is intended that this term would be calculated separately from given thermodynamic data at the entrance.

3. Definitions, flow diagrams, and program listings are included in the Appendix. Many control, indexing, and grouping names are undefined. Their usage may be interpreted from the developments of the preceding section or from the program listings.

D. **Results of Rotor 1**

This program computed properly, but the results were unacceptable. Streamline corrections were large (up to 1/2 inch), imposing improbable velocity distributions. The characteristics appeared to be properly located, however, the flow angles, $\beta$, were somewhat arbitrarily distributed along normals and characteristics.
A number of test print-outs were made in order to locate the inaccuracies. (The listing of Rotor 1 in the Appendix includes test print-out instructions.) It was discovered that the derivatives of $\Theta$, calculated by Eqs. (39), (40), (53), and (54) were inaccurate. The second derivatives were particularly incorrect. The methods used are considered to be sound, however, the degree of accuracy primarily depends on the accuracy of the input data. In this analysis, the $\Theta$ = constant lines were originally plotted from approximations. Errors introduced in plotting were compounded by graphical interpolations (and extrapolations) for $\Theta$ values at grid points. The erroneous $\Theta$ derivatives were introduced in the computations for the coefficients, $Y$, resulting in an improbable flow solution.

E. Alternate Meridional Plane Analysis

1. It was decided to eliminate the derivatives of $\Theta$ from the calculations, therefore, it was necessary to introduce known values of $\beta$. It is reasonable to assume that these data would be available, or could be computed, from detailed drawings of the impeller. For this analysis, $\beta$ distributions along the hub and tip contours were obtained from data used in the original design work. However, $\beta$ cannot be specified on the internal streamlines until the streamline is constructed. A distribution of $\beta$ from hub to tip must be assumed.

2. $\beta$ along the hub and tip contours is shown in Fig. 9.
It is assumed that $\beta$ varies linearly along normals between these contours.

$$\beta_j = \beta_H + \left( \beta_T - \beta_H \right) \frac{M_j}{M_T} \quad (76)$$

The function $D_2$ of Eq. (49) becomes:

$$D_2 = \frac{1}{R \cos \delta} \frac{d}{dl} (R \tan \beta)$$

$$= \tan \delta \left( \frac{\partial \tan \beta}{\partial m} + \frac{\partial \tan \beta}{\partial n} \right) + \frac{D \tan \beta}{R \cos \delta} \quad (77)$$

The distribution of $\tan \beta$ between two grid points on a streamline or normal is assumed to be linear.

$$\frac{\partial \tan \beta}{\partial m_j} = \frac{\tan \beta_{i+1} - \tan \beta_i}{\Delta N_j} \quad (78a)$$

$$\frac{\partial \tan \beta}{\partial n_i} = \frac{\tan \beta_{i+1} - \tan \beta_i}{d M_i} \quad (78b)$$

At the $i$th grid point:

$$\frac{\partial \tan \beta_i}{\partial m_j} = \frac{\tan \beta_{i+1} - \tan \beta_{i-1}}{2 \Delta N_j} \quad (79)$$

At a point, $P^*$:

$$\frac{\partial \tan \beta}{\partial n} = \left( \frac{\partial \tan \beta}{\partial n_{i+1}} - \frac{\partial \tan \beta}{\partial n_i} \right) \frac{\Delta N}{\Delta N_j} \quad (36)$$

The angle $\delta$ is still measured on the $\Theta$-constant curves.

Leading edge calculations are also modified. A linear distribution of $\beta$ along the leading edge is assumed in the same manner as Eq. (76).

F. Computer Programs: Rotor 2 and LEDGE 2

1. Program Rotor 2 is a modification of Rotor 1, with the new calculations for $\beta$ replacing the $\Theta$ derivatives.

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order of some solutions has been changed to simplify the mechanics of the program. Subroutines DTD and ANGLE are eliminated. The values of the angles, $\gamma$, are computed in the main program or in subroutine PSTAR. Subroutine PSTAR is modified to reflect these changes. Subroutine DDL replaces COY, and calculates the derivatives along the $\Theta=$constant curves. Curvatures are calculated in PSTAR. Subroutines RELVEL and FLOW are unchanged. Program LEDGE 2 is a simplification of LEDGE 1, reflecting the introduction of $\beta$ data.

Both programs are diagrammed and listed in the Appendix. Only new or modified variable names are defined.

G. Results of Rotor 2

1. The complete meridional plane analysis was solved by Rotor 2. Nine characteristics were generated. Fig. 4 is a tracing of the actual construction for the first two characteristics. The grid networks for both solutions are indicated. Two modifications are made to the first set of estimated streamlines. The first modification reflects the changes effected by the calculations for characteristic Cl. Each change required recalculations in LEDGE 2. The results of the last calculation were held constant throughout the remaining solutions.

Data for each characteristic are listed in Tables II-1 through II-9. The "starting normal" originates from the "starting point" for each calculation. The "starting point number" indicates the position of the normal in the grid
system for each solution. The intersection of a characteristic with each streamline is located by measuring the distance DNSTAR (dN*) from the intersection of the starting normal with the streamline. Streamlines are corrected by measuring the distance DELTA (δx) along the characteristic from the original intersection, P*. Relative velocities are listed for the final intersection point. Additional data are listed as checks on the calculations.

For example, the calculations for characteristic C8 showed a discrepancy between the correction length, δx, and the computed radius, in locating the new streamlines. Test print-outs revealed errors in the calculated grid lengths, dM. These errors had accumulated, resulting in somewhat radical streamline deviations and questionable velocities. dM had been calculated by Eq. (42a), which, at the time, was used for angles, λ, of 60 degrees or less. This limit was changed to 45 degrees and Eq. (42b) applied. The results were satisfactory.

2. The completed system of computer characteristics and streamlines is shown in Fig. 10. True normals are constructed perpendicular to these streamlines. Streamlines have been faired and extended to the trailing edge. Data points are indicated.

The distributions of relative velocity along odd numbered streamlines are plotted in Fig. 11. Values at the leading edge were hand calculated. Velocities at the trailing edge were extrapolated on a large scale plot. Curves
are faired through data points without smoothing. The relative velocity profiles on the odd numbered normals of Fig. 10 are cross plotted in Fig. 12.

3. Computer run time for one ROTOR 2 solution was approximately two minutes. Construction and data preparation time was about four hours. Total preparation and computer time for LEDGE is approximately two hours.

H. Blade to Blade Analysis

1. Most of the preliminary calculations have been accomplished in the hub to tip solution. The values of $W$, $D_{\text{W coef}}$, and $D_{\text{W func}}$ are plotted from the results in Tables II, and the curves smoothed. Data are read from these curves at equal increments along each streamline. Extrapolated data are used at the leading and trailing edges. An increment of 1/2 inch is used in this solution.

The derivatives of $D_{\text{W func}}$ are computed by the five-point difference formulas of Eqs. (39). The relative velocity difference, $\Delta W$, is computed by a form of Eq. (34):

$$\Delta W = \frac{D_{\text{W coef}}}{2} \frac{d(D_{\text{W func}})}{dm}$$  \hspace{1cm} (81)

The relative velocity distributions on the pressure and suction blade surfaces (driving and trailing surfaces in a compressor) are calculated by Eqs. (27).

2. Program BLADE performs these calculations along each streamline, from leading edge to trailing edge. Computer run time was approximately 30 seconds. Preparation time was about six hours.
3. Results are compiled in Tables III-1 through III-9. The relative velocity distributions along the hub, tip, and mean streamlines are plotted in Figs. 13, 14, and 15. The linear velocity profiles across the blade channel, at various stations along the mean streamline, are shown in Fig. 16.
IV. DISCUSSION

A. Theoretical Assumptions

1. The assumption of axial symmetry is in keeping with sound engineering practice. Although changes in the circumferential direction are ignored, incremental pressure changes across the blades are considered by introducing the blade force, $F_B$. This assumption is also made in Refs. 1 and 2. The general theory, postulated by Wu in Ref. 4, does not admit to axial symmetry. Wu modifies the development of Ref. 2 to allow for deviations from axial symmetry, accounting for these deviations with a thickness factor, $B$. This factor is conveniently used as an integrating parameter in defining a flow function. $B$ is interpreted as being proportional to the thickness of a stream sheet containing an arbitrary stream surface, and to blade thickness distribution.

This theory is sound, and would produce accurate results if explicitly applied. However, the factor $B$ must be assumed, either arbitrarily or from available data. An example of an assumed distribution of $B$ is found in Ref. 6. A blade to blade analysis is made, using the distribution as input. This report states that such data are obtained from a meridional plane analysis, presumably by the methods of Ref. 4. Yet, Ref. 4 states that $B$ is best calculated from the results of a blade to blade analysis. Wu, in Ref. 13, uses a value of $B$ equal to one, which imposes axial symmetry. He states that methods for estimating $B$ were
unavailable at the time. This reference also shows that the changes effected by this assumption are small. The advantage of using approximate values of B, over the axisymmetric approach, is doubtful.

2. The assumption of a steady, inviscid, adiabatic flow is generally accepted. Exclusion of any one of these factors introduces highly complex theoretical considerations, which are difficult, if not impossible to apply. The assumption of isentropic flow within the rotor is reasonable, since known exceptions are considered. The specific exceptions, included in this theory, are the entropy changes caused by discontinuities of the leading and trailing edges. The analysis of this thesis is based upon the premise that these entropy changes are small and can be ignored. This is also implied in Ref. 1, which analyzes flows which conform to the prescribed blade angles at the leading and trailing edges. The analysis of this thesis is not limited by this implication. Entrance conditions are not restricted to design conditions, and Eq. (25) is generally applicable.

3. An incompressible solution was developed in this thesis in order to simplify the presentation. Compressible solutions can be solved by this method if the volumetric flow rate is replaced by the mass flow rate. Density changes along a characteristic can be computed by thermodynamic relations which equate the equilibrium conditions at any point, $P^*$, to known or computed entrance conditions.

4. A simplified blade to blade solution is used in this
thesis. The assumption of a linear velocity distribution is not unique. Ref. 1 assumes a linear pressure variation across the blade channel. Ref. 6 validates this assumption for design conditions. The results of Ref. 3 show near-linear velocity distributions for both the compressible and incompressible solutions.

B. The Design Analysis

1. The design analysis was discontinued because of time considerations. However, it was shown that the theory could be applied to the design solution as well as the direct solution. Difficulty arose in prescribing practical blade characteristics. One method would be to assume various $\beta$ and $\epsilon$ distributions as functions of streamline and normal directions; then generate a blade shape for each combination, and select the most practical solution. Selection would be contingent upon the results of a direct analysis, similar to the method developed in this thesis. This approach appears to be quite long.

The question is whether or not this development is warranted. A design method, based on the theoretical development of Ref. 1, is presented in Ref. 5. The hub profile is calculated from successive flow solutions. This approach is modified by Ref. 7 to provide for arbitrary entrance and discharge conditions. In effect, the initial conditions establish the $\Theta =$constant curves. The solution provided the upper limit of these curves. The design
problem is practically solved by the initial conditions. All that remains is a system of repetitive calculations, which produces an acceptable tip profile. In comparison, the method proposed in this thesis would generate blade shapes, rather than tip contours. It seems more logical, and perhaps more expeditious, to establish feasible physical contours and analyze the flow under prescribed conditions. The contours could then be altered to eliminate undesirable flow phenomena, and to produce the desired performance. This is precisely what is done in the direct approach. Therefore, the design, or indirect, method is considered to be unnecessary.

C. Methods of Solution
1. The developments of Refs. 8 and 9 present a relatively simple approach to the direct problem when compared to Ref. 4. The establishment of characteristic solutions provides a method, compatible with high speed machine computations. A limited number of applications of Ref. 4 have been presented. None have attempted a solution of the complete theory, but have reduced the problem to solutions for specific applications. Ref. 6 deals with the blade to blade analysis. Refs. 5 and 7 are concerned with the design problem, and consider the methods proposed in Ref. 4 to be impractical for engineering applications. In Ref. 13 the methods of Ref. 4 are simplified by assuming axial symmetry, and an incompressible solution is used as a basis for the compressible solution. It is concluded, therefore,
that the approach presented in this thesis is theoretically sound.

2. The accuracy of the solution of any theoretical analysis depends upon the precision of the numerical methods used in computations, and in the accuracy of the input data. It is difficult to assess the inaccuracies introduced by the numerical approximations in this method. It would be impossible to isolate each error, even if test results were available for comparison. Gross inaccuracies, such as those revealed by ROTOR 1, can be detected. Small errors may cancel, or large errors may ensue from an accumulation of small inaccuracies.

For example, the assumptions of linear distributions of curvature and flow angles are questionable in the vicinity of the axial midpoint of the test impeller. Hub and tip curvatures (Fig. 6) follow different patterns in this region. The odd distribution of hub curvature is difficult to explain. The difference between hub and tip blade angles is a maximum in this region. (Fig. 9) These two quantities are multiplied in the calculations of the coefficient, Y. Difficulties were encountered in obtaining accurate results along characteristics in this region, indicating that the errors introduced by these assumptions may have multiplied. Such reasoning is not conclusive, however, since the results of the complete solution do not indicate excessive errors.

Many interpolations were used in this solution. The accuracy of each depends on the grid spacing. The spacing
of normals was limited to a maximum of .3 inches. Nine streamlines are considered sufficient. A finer network would certainly increase the accuracy of each calculation, however, the process of measuring data would become tedious.

The reliability of all calculations also depends upon the accuracy of the measured data. The meridional plane was drawn to double scale. Lengths were measured to an accuracy of about .05 inches. The angles, \( \lambda \), were measured with a drafting machine to an accuracy of 5 minutes. (.1 degree) This accuracy is reduced to about .3 degrees, since measurements were made on curved lines. Interpolations were made for \( \delta \) to the nearest tenth of a degree, but an accuracy of 1/2 degree is more reasonable.

3. The general approach to the meridional plane solution can be applied to obtain the desired degree of accuracy, within the limits outlined in the preceding discussion. A finer grid will increase accuracy for a particular characteristic solution. A solution can be repeated, using the previous results to establish new initial conditions. The number of characteristic solutions used is arbitrary. Therefore, a detailed investigation can be conducted in discrete regions in a rotor channel, or a complete solution can be rapidly calculated, using a few characteristics.

Theoretically, the method can be used to calculate characteristic solutions outside the rotor channel. In this case the defining angles of the blade are set equal to zero, and the characteristics coincide with normals. In stationary
cascades, the rotational effects are eliminated. These solutions are excluded in the computer solutions of this thesis, because of the schemes adapted in performing numerical interpolations. Solutions can be calculated in close proximity to the leading and trailing edges if fictitious blade characteristics are used outside these boundaries.

D. Results

1. The results of the first method of solution (ROTOR 1) were unacceptable. This was partially due to the numerical methods used in calculating the $\Theta$-derivatives. However, inaccuracies of the $\Theta=$constant curves are considered to be the primary fault. It is believed that accurate $\Theta=$constant curves can be constructed from three-view drawings. Under this assumption, Rotor 1 can be utilized with acceptable accuracy.

2. The results of Rotor 2 are considered valid. Although test results are not available for comparison, the logic of the preceding discussion is sufficient proof, in that:

   a. The theory is sound.

   b. The assumptions are justified for engineering applications.

   c. Numerical methods are designed to minimize inaccuracies in each calculation, so that errors will not accumulate.

   d. Data are accurately measured.

3. The computed system of streamlines is regular and follows
a logical development through the rotor. Fig. 10 is a smooth plot of this system. Deviations from data points are small. Maximum deviations occur in the region of rapid curvature and blade angle changes.

4. The acceptable system of streamlines demonstrates the consistency of the solution. The accuracy of the method is measured by the resultant relative velocity distribution. This distribution completely defines the flow. Both pressure distribution and power delivered, or required, are calculated directly from the velocities. Variations in relative velocity indicate areas of possible flow separation.

The accuracy of the relative velocities at the leading edge are computed directly from entrance conditions, and are accurate. Variations of velocities along selected streamlines are shown in Fig. 11. Proper trends are indicated for a compressor with deloaded type blades. Most of the work input is accomplished in the forward section of the rotor, diminishing towards the trailing edge. It should be noted that the energy level of the fluid is not affected by velocity alone. Eq. (6), together with Eq. (9b), shows that the local enthalpy is also a function of peripheral speed, \(\omega R\). Therefore, the deloaded blade effectively reduces the deceleration of the relative velocity at high radii, so that the work input, thus blade loading, will not become excessive. The irregular nature of the velocity distributions in Fig. 11 might be attributed to inaccuracies in the calculations; however, similar presentations
in Refs. 5, 6, and 13 support the existence of these irregularities. In contrast, the velocity profiles along normals in Fig. 12 are quite regular.

5. The applicability of these results can be illustrated by an investigation of flow separation along a contour. Relative velocity changes along the hub, near the leading edge, appear to be conducive to separation. The rapid decrease in velocity implies an adverse pressure gradient. A separation parameter, K, is derived in Ref. 14. A value of K greater than .045 indicates probable separation.

\[ K = \frac{1}{\rho} \frac{dP}{d\ell} \frac{1}{W^2 R_{\text{eff}}^{1/5}} \]  

Reynold's Number is defined as:

\[ R_e = \frac{W l}{\nu} \]

Let:

\[ l = \frac{m}{\cos \bar{\beta}} \]

where: \( l \) = length along blade from stagnation point
\( \bar{\beta} \) = average blade angle

Along a streamline, from Eqs. (6) and (9b):

\[ \frac{dh}{dm} = -W \frac{dW}{dm} + \omega^2 R \frac{dR}{dm} \]  

For incompressible flow:

\[ dh = \frac{dP}{\rho} \]

\[ K = \frac{m^8 (-W \frac{dW}{dm} + \omega^2 R \frac{dR}{dm}) \cdot (\nu \cos \bar{\beta})^2}{W^{2.7}} \]  

At a point on the hub, \( m = 2 \) inches:

\( W = 106 \) ft./sec.  
\( \frac{dW}{dm} = -216 \) ft./sec.-ft.
\[
\frac{dR}{dm} = \sin \lambda = 0.165 \\
R = 0.5 \text{ ft.} \\
\nu = 0.00016 \text{ ft.}^2/\text{sec. for air} \\
\beta = 49^\circ \text{ from Fig. 9}
\]

Therefore: \( K = 0.0138 \)

Thus, flow at this particular point, which appears to be in one of the more critical regions for separation, should not separate. The relatively high value of \( K \) does indicate possible separation farther along the hub; however, the change of velocity decreases beyond this point. The effects of peripheral speed and curvature on separation are illustrated in Eq. (84). The value of \( K \) is approximately 0.0092 at the point of maximum curvature, at a distance of about 0.4 inches along the tip streamline. The velocity gradient at this point is practically zero. Although the value of \( K \) is low, it can be surmised that a nominal negative velocity gradient might induce separation.

6. The results of the blade to blade analysis are extensions of the more exact meridional plane analysis. The relative velocity distributions along streamlines (Figs. 13, 14, and 15) can also be analyzed for local phenomena, which may be aggravated by the correction, \( \Delta W \). This velocity difference is used to calculate the fluid forces on the blade with the relations of Section II. A presentation of the type shown in Fig. 16 is adequate for these calculations.

An attempt was made to indicate the correlation between the trailing edge velocities in Fig. 14, in order to
establish some initial conditions for a wake analysis. The dashed line indicates a possible velocity distribution, but this is only a guess. Figs. 13 and 15 do not demonstrate this convergence. In addition, the velocities at the trailing edge are calculated from extrapolated data. Therefore, this type of correlation is inconclusive.

E. Extensions of the Method

1. The meridional plane analysis sufficiently describes the flow for an incompressible analysis. The results might be extended to include the calculations of:
   a. Pressure distribution
   b. Power input or power required
   c. Separation parameter
   d. Cavitation parameter
   e. Blade forces

Most of these calculations depend upon the results of several characteristic solutions, and would be included in a separate computer program. Many preliminary calculations of point functions (pressure, enthalpy, etc.) can be included in the main solution.

2. The methods should be modified to include characteristic calculations outside the rotor passage. This would permit continuous solutions through multi-stage machines and in unbladed passages. Major modifications would be required, since a number of decisions would be needed to insure the use of proper blade properties in the vicinity of blade boundaries. Input requirements would necessarily
become more complex.

3. The theory and methods could be modified to use non-dimensional variables. This would be particularly applicable to design studies, where non-dimensional results of preliminary rotor configurations could be directly compared.

4. This method should be extended to include the compressible solution. A method is outlined in Ref. 9.

5. The blade to blade method used in this thesis is practical in its simplicity, and is sufficiently accurate when used in conjunction with the meridional plane analysis. It would be interesting to compare the results of this solution with a more exact approach, such as the method of Ref. 6.

6. The extensions to the meridional plane analysis should also be included in the blade to blade solution.
V. CONCLUSIONS AND RECOMMENDATIONS

A. It is concluded that:

1. Theoretical assumptions are based on practical consideration, and do not impose excessive limitations on the solution.

2. The meridional plane analysis is developed from sound theoretical derivations, which provide a relatively rapid and accurate method of solution.

3. The methods which are applied in solving this problem are good approximations. The degree of accuracy of each characteristic solution depends on the size of the coordinate grid and on the accuracy of data measurements.

4. The progressive method employed in the meridional plane solution can be applied at arbitrary intervals to obtain the desired accuracy.

5. The accuracy of the results, based primarily upon theoretical considerations, is sufficient for engineering purposes.

6. Results are not sufficiently accurate to compute detailed analyses at the trailing edge.

7. The results of this method are sufficient to completely describe the flow within the rotor, and predict the performance of the machine.

8. This solution is restricted to flows within the rotor passage.

9. The computer program, ROTOR 1, can be used if \( \Theta = \text{constant} \) curves are accurately specified.
10. The use of a direct flow analysis is preferable to the inverse method in design studies.

11. The blade to blade analysis is limited by the assumption of a linear velocity distribution, but the results are acceptable for engineering purposes.

B. It is recommended that:

1. The method be non-dimensionalized.

2. Computations be added to describe pressure distribution, blade force, power, and critical flow phenomena.

3. The solution be modified to include compressible flows, and calculations beyond rotor boundaries.

4. A more accurate blade to blade analysis be used in conjunction with this meridional plane solution.
REFERENCES


**TABLE I**

**INITIAL DATA FOR TEST IMPELLER**

<table>
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<tr>
<th>Description</th>
<th>Value</th>
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<tr>
<td>No. of Blades</td>
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<tr>
<td>Blade Thickness, in.</td>
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<tr>
<td>RPM.</td>
<td>1800</td>
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<td>Volumetric Flow Rate, cu. ft./sec.</td>
<td>128.212</td>
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<tr>
<td>Annulus Area at L.E., sq. in.</td>
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<td>Meridional Velocity, $V_{mL}$, ft./sec.</td>
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Air at Standard Temperature and Pressure
### Table II-1

**Data for Characteristic C1**

**Location of Characteristic Curve**

Starting normal no. = 4

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<th>4</th>
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<td></td>
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<tr>
<td>DNSTAR</td>
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**Location of New Streamlines**

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**Velocity Profile**

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<td></td>
<td></td>
</tr>
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<td>90.8116</td>
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TABLE II-2

DATA FOR CHARACTERISTIC C2

LOCATION OF CHARACTERISTIC CURVE

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LOCATION OF NEW STREAMLINES

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VELOCITY PROFILE

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# TABLE II-2

**DATA FOR CHARACTERISTIC C2**

**LOCATION OF CHARACTERISTIC CURVE**

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**LOCATION OF NEW STREAMLINES**

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### TABLE II-3

**DATA FOR CHARACTERISTIC C3**

**LOCATION OF CHARACTERISTIC CURVE**

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**DATA FOR CHARACTERISTIC C3**

**LOCATION OF CHARACTERISTIC CURVE**

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# TABLE II-4

DATA FOR CHARACTERISTIC C4

LOCATION OF CHARACTERISTIC CURVE

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LOCATION OF NEW STREAMLINES

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VELOCITY PROFILE

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### TABLE II-5

**Data for Characteristic C5**

**Location of Characteristic Curve**

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**Location of New Streamlines**

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**Velocity Profile**

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TABLE II-5
DATA FOR CHARACTERISTIC C5

LOCATION OF CHARACTERISTIC CURVE

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LOCATION OF NEW STREAMLINES

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VELOCITY PROFILE

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### Table III-6

Data for Characteristic C6

#### Location of Characteristic Curve

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<td>-27.5695</td>
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#### Location of New Streamlines

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#### Velocity Profile

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### TABLE 3-6

**DATA FOR CHARACTERISTIC C6**

#### LOCATION OF CHARACTERISTIC CURVE

**STARTING NORMAL NO. = 2**

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#### LOCATION OF NEW STREAMLINES

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#### VELOCITY PROFILE

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### TABLE H-7

**DATA FOR CHARACTERISTIC C7**

**LOCATION OF CHARACTERISTIC CURVE**

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**LOCATION OF NEW STREAMLINES**

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**VELOCITY PROFILE**

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### Table II-7

**Data for Characteristic C7**

#### Location of Characteristic Curve

**Starting Normal No. = 2**

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#### Velocity Profile

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### Table II-8

**Data for Characteristic C8**

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DATA FOR CHARACTERISTIC C8

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VELOCITY PROFILE

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**LOCATION OF NEW STREAMLINES**

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**VELOcity PROFILE**

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**TABLE III-9**

**DATA FOR CHARACTERISTIC C9**

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**LOCATION OF NEW STREAMLINES**

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**VELOCITY PROFILE**

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# TABLE III-1

**VELOCITY PROFILE**

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### TABLE III-8

**VELOCITY PROFILE**

**MERIDIONAL STREAMLINE NO. 8**

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Fig. 1
Meridional Plane with
Physical Contours

Radius, R. Lines

Tip Contour

Hub Contour

\( \Theta = \text{const. line} \)

-60°
-30°
-10°
Fig. 2
Definition of Angles on a Meridional Plane

Characteristic

\[ \Theta = \text{const.} \]

\[ \Theta + d\Theta = \text{const} \]

\[ +\delta \]

\[ +\gamma \]

\[ \pm \lambda \]

\[ \pm \lambda \]

\[ \text{dm} \]

\[ \text{dn} \]

\[ \text{d} \]

\[ \text{L} \]

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Fig. 3
Velocity Triangle on the Tangent Plane of a Stream Surface

\[ V_u \]
\[ W_u \]
\[ W_m = V_m \]
Fig. 4

Location of Streamlines

Characteristics Nos. 1 & 2

- Grid Points
- Characteristics
- Assumed Normal
- Final S.L.
- 2nd Estimate
- 1st Estimate
- Starting Normals
Fig 5
Location of a Point $P^*$
on a Characteristic
Fig. 6
Curvature of Hub & Tip Contours

Curvature - /inch

Axial Distance, Z-inches
Parabolic Interpolation for \( \frac{d^2 \theta}{dm^2} \).
Fig. 8
Determination of Increments for Parabolic Interpolation

\[ m_i = -(\Delta N + dN^*) \]
\[ m_2 = -dN^* \]

\[ +dN^* : \]
\[ m_1 = -dN^* \]
\[ m_2 = \Delta N - dN^* \]

\[ \Delta N \]
\[ m_{j+1} \]
\[ m_j \]
\[ m_i \]
\[ m_2 \]

NS - Starting Normal
Fig. 9
Blade Angle, $\beta$
on
Hub & Tip Contours

Blade Angle, $\beta$ - deg

Axial Distance, Z - inches

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Fig. 11

Velocity Distribution on Streamlines

Relative Velocity - W - fps vs Dist. along Streamline - inches
Fig. 12
Velocity Distribution on Normals
Fig. 13
Blade to Blade
Velocity Distribution
along
Hub Streamline

S. L. No. 1

Relative Velocity, W - fps

Distance along Streamline - inches
Fig. 14
Blade to Blade
Velocity Distribution
along
Mean Streamline

S. L. No. 5

Relative Velocity, W - fps

Distance along Streamline - inches

2 4 6 8 10 12 14
Fig. 16

Velocity Distribution across Blade Channel at Various Points, m along Mean Streamline

Direction of Rotation

Relative Velocity, W-fps

P. Side

S. Side
APPENDIX

COMPUTER PROGRAMS
### PROGRAMS LEDGE 1 AND LEDGE 2

#### VARIABLE NAMES

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**Additions for LEDGE 2**

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Program LEDGE I

Read Input

Angles to Radians

Calculate $C_0$

Calculate: $d\theta/dm$

$F(L)$

All S.L.'s?

No

Yes

Calculate $L$

All S.L.'s?

No

Yes

Calculate DFL

All S.L.'s?

No

Yes

Print Output

END
PROGRAM LEDGE 1
DIMENSION RL(9),ALFA(9),DELN(9),F(9),EL(9),VM(9),
THETA(9,3),AALFA(9),ATHETA(9)
READ 10,MO,RPM
10 FORMAT(110,F10.0)
READ 11,RL
11 FORMAT(6F10.0)
READ 11,ALFA
READ 11,VM
READ 11,(THETA(M,K),K=1,3),M=1,MO
DO 12 M=1,MO
AALFA(M)=ALFA(M)*3.14159/180.
DO 12 K=1,3
ATHETA(M,K)=THETA(M,K)*3.14159/180.
12 CONTINUE
OMEGA=RPM*3.14159/30.
DO 13 M=1,MO
CTDM=(-3.*ATHETA(M,1)+4.*ATHETA(M,2)-ATHETA(M,3))
/(2.*CELN(M))
F(M)=(VM(M)*12.*CTDM+OMEGA)*RL(M)*RL(M)
13 CONTINUE
EL(1)=0.
DO 14 M=2,MO
EL(M)=EL(M-1)+(RL(M)-RL(M-1))*SINF(AALFA(M-1))
14 CONTINUE
PRINT 21.
21 FORMAT(/ICX,21*LEADING EDGE FUNCTION/*/11X1HM11X3DFL)
DO 22 M=1,MO
15 IF(M-1) 15,15,16
15 MA=1
MB=2
MC=3
GO TO 19
16 IF(M-MO) 17,18,18
17 MA=M
MB=M+1
MC=M-1
GO TO 19
18 MA=MO
MB=MC-1
MC=MC-2
GO TO 19
19 XA=EL(MB)-EL(MA)
XB=EL(MC)-EL(MA)
DFL=(XB*XB*(F(MB)-F(MA))-XA*XA*(F(MC)-F(MA)))/
((XA*XB-XA*XA-XA*XB)*12.*SINF(AALFA(M)))
PRINT 20,M,DFL
20 FORMAT(/10X,12,5X,F15.5)
22 CONTINUE
END
END
Program LEDGE 2

1. Read Input
2. Angles to Radians
3. Calculate $\theta$'s
   - If ALL S.L.'s are Yes, go to 4.
   - If ALL S.L.'s are No, go to 2.
4. Calculate $\omega$
5. Calculate $F(L)$
   - If ALL S.L.'s are Yes, go to 6.
   - If ALL S.L.'s are No, go to 5.
6. Calculate $L$
   - If ALL S.L.'s are Yes, stop.
   - If ALL S.L.'s are No, go to 5.
PROGRAM LECGE 2
DIMENSION RL(9),ALFA(9),F(9),EL(9),VM(9),
BETA(9),ABETA(9),AALFA(9)
READ 10,MC,RPM
10 FORMAT(11C,F10.0)
READ 11,RL
11 FORMAT(6F10.0)
READ 11,ALFA
READ 11,VM
READ 32,BETA(1),BETA(9)
32 FORMAT(2F10.0)
ABETA(1) = BETA(1)*2.14159/180.
ABETA(9) = BETA(9)*2.14159/180.
DO 12 M=1,MC
AM = FLOAT(M-1)/FLOAT(MC-1)
AALFA(M) = AALFA(M)*3.14159/180.
12 ABETA(M) = ABETA(1)+(ABETA(M)-ABETA(1))*AM
CMega = RPM*3.14159/30.
DO 91 M=1,MC
BETA(M) = ABETA(M)*180./CMega
91 CONTINUE
DO 13 M=1,MC
F(M) = VM(M)*RL(M)*TAN(ABETA(M))*12.*CMega*RL(M)*RL(M)
13 CONTINUE
EL(1) = 0.
DO 14 M=2,MC
EL(M)=EL(M-1)+(RL(M)-RL(M-1))*.SIN(AALFA(M-1))
14 CONTINUE
PRINT 31
31 FORMAT(11X,M15,15,16
MA = 1
MB = 2
MC = 3
GO TO 19
15 IF(M-MC) 17,18,18
16 MA = M
MB = M+1
MC = M-1
GO TO 19
17 MA = MC
MB = MC-1
GO TO 19
18 XA = EL(MB)-EL(MA)
XB = EL(MC)-EL(MA)
CFL = (XB*XB*(F(MB)-F(MA))-XA*XA*(F(MC)-F(MA)))/
1/((XA*XB)*XB*XA-12.*SIN(AALFA(M))
PRINT 20,M,CFL
20 FORMAT(10X,12.5X,5X,F15.5)
22 CONTINUE
END
## VARIABLE NAMES

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<td>DHEDN</td>
<td>$\partial H_e/\partial n_e$</td>
<td></td>
</tr>
<tr>
<td>DM</td>
<td>$dM$</td>
<td>in.</td>
</tr>
<tr>
<td>DNSTAR</td>
<td>$dn^*$</td>
<td>in.</td>
</tr>
<tr>
<td>DTM, DT1, DT2</td>
<td>$d \theta/dm$</td>
<td></td>
</tr>
<tr>
<td>DWCO</td>
<td>$D^w$ coef.</td>
<td></td>
</tr>
</tbody>
</table>

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<table>
<thead>
<tr>
<th>Name</th>
<th>Equivalent to</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>DWFUNC</td>
<td>(D\omega\func) (\delta N/2)</td>
<td>in.</td>
</tr>
<tr>
<td>DX</td>
<td>(dx)</td>
<td>in.</td>
</tr>
<tr>
<td>EN</td>
<td>(\beta(x))</td>
<td></td>
</tr>
<tr>
<td>FX</td>
<td>(\gamma) at (P^*)</td>
<td>deg.</td>
</tr>
<tr>
<td>GAMMA</td>
<td>(\gamma) at ((P^*+\delta x))</td>
<td>deg.</td>
</tr>
<tr>
<td>GAMX</td>
<td>(\gamma) at (P^*)</td>
<td>rad.</td>
</tr>
<tr>
<td>PGAMMA</td>
<td>(\tan\gamma)</td>
<td></td>
</tr>
<tr>
<td>TGAMMA</td>
<td>(\gamma) at ((P^*+\delta x))</td>
<td>rad.</td>
</tr>
<tr>
<td>XGAMMA</td>
<td>(\gamma) at ((P^*+\delta x))</td>
<td>rad.</td>
</tr>
<tr>
<td>ALAM</td>
<td>(\lambda)</td>
<td>rad.</td>
</tr>
<tr>
<td>DLAM</td>
<td>(\lambda)</td>
<td>deg.</td>
</tr>
<tr>
<td>PLAM</td>
<td>(\lambda) at (P^*)</td>
<td>rad.</td>
</tr>
<tr>
<td>XLAM</td>
<td>(\lambda) at ((P^*+\delta x))</td>
<td>rad.</td>
</tr>
<tr>
<td>OMEGA</td>
<td>(\omega)</td>
<td>per sec.</td>
</tr>
<tr>
<td>QA</td>
<td>(Q) (actual)</td>
<td>cu. ft./sec.</td>
</tr>
<tr>
<td>QC</td>
<td>(Q) (calculated)</td>
<td>cu. ft./sec.</td>
</tr>
<tr>
<td>QDEL</td>
<td>(\Delta Q)</td>
<td>cu. ft./sec.</td>
</tr>
<tr>
<td>DQ</td>
<td>(\int E(x)dx)</td>
<td>cu. ft./sec.</td>
</tr>
<tr>
<td>R</td>
<td>(R)</td>
<td>in.</td>
</tr>
<tr>
<td>AR</td>
<td>(R) at (P^*)</td>
<td>in.</td>
</tr>
<tr>
<td>RX</td>
<td>(R) at ((P^*+\delta x))</td>
<td>in.</td>
</tr>
<tr>
<td>THETA</td>
<td>(\Theta)</td>
<td>deg.</td>
</tr>
<tr>
<td>ATHETA</td>
<td>(\Theta)</td>
<td>rad.</td>
</tr>
<tr>
<td>THICK</td>
<td>(\Delta t)</td>
<td>in.</td>
</tr>
<tr>
<td>TKEQV</td>
<td>(\Delta t')</td>
<td>in.</td>
</tr>
<tr>
<td>Name</td>
<td>Equivalent to</td>
<td>Units</td>
</tr>
<tr>
<td>--------------</td>
<td>--------------------------------</td>
<td>----------------</td>
</tr>
<tr>
<td>W</td>
<td>W</td>
<td>ft./sec.</td>
</tr>
<tr>
<td>WDEL</td>
<td>dw</td>
<td>ft./sec.</td>
</tr>
<tr>
<td>WM</td>
<td>$W_m$ at $P^*$</td>
<td>ft./sec.</td>
</tr>
<tr>
<td>WX</td>
<td>$W_m$ at $(P^* + \delta x)$</td>
<td>ft./sec.</td>
</tr>
<tr>
<td>WSQ</td>
<td>$W_m^2$ at $P^*$</td>
<td>ft.$^2$/sec.$^2$</td>
</tr>
<tr>
<td>DWSQ</td>
<td>$dW_m^2/dx$</td>
<td>ft.$^2$/sec.$^2$-in.</td>
</tr>
<tr>
<td>X, AX</td>
<td>$x$</td>
<td>in.</td>
</tr>
<tr>
<td>XDEL</td>
<td>$\delta x$</td>
<td>in.</td>
</tr>
<tr>
<td>Y1, Y2, Y3</td>
<td>$Y_1$, $Y_2$, $Y_3$</td>
<td>in.</td>
</tr>
<tr>
<td>Z</td>
<td>$Z$</td>
<td>in.</td>
</tr>
</tbody>
</table>

**INDEX NAMES**

N, NN, etc. = Normal number  
M, MM, etc. = Streamline number  
MO = Total number of streamlines  
NO = Total number of normals  
NS = Starting normal

**Changes and additions for Rotor 2**

- **ABETA**  
  \[ \beta \]  
  rad.
- **APBETA**  
  \[ \beta \text{ at } P^* \]  
  deg.
- **DTBN**  
  \[ d(\tan \beta)/dn \]
- **DTBM**  
  \[ d(\tan \beta)/dm \]
Program Rotor 1

Main Program

Read Input

Angles to Radians

Calculation at Initial Point:

\[
\begin{align*}
R & \quad \lambda \\
\beta & \quad \delta \\
dN^* & = 0 \\
DM & = 0
\end{align*}
\]

Calculate DM

Calculate dN^*

S.R. PSTAR for +dN^*

S.R. PSTAR for -dN^*

Calculations for dN^* = 0

S.R. DTD
S.R. ANGLE

S.R. PSTAR for +\gamma'

S.R. PSTAR for -\gamma'

\[
\begin{align*}
\gamma' & = ?
\end{align*}
\]

Sufficient Grid?

Yes

No

END
Initialize to Correct Streamlines
\[ Q_{AF} = Q_A \left( \frac{M_i}{M_T} \right) \]

Calculate QC
\[ (\delta x = 0) \]

\[ |Q_{C-QAF}| - \varepsilon \]

\[ \delta x = 0.2 \]

Calculate QC

\[ Q_{C-QAF} \]

[Decide whether to increase or increment \( \delta x \)]
Calculate \( W \)

Calculations for Blade to Blade

All S.L.'s?

Yes

Print Final Results

END

No

All S.L.'s?

Yes

Calculate \( W \)

No

(0)

(4)

(5)

(6)

(7)

\( \log \cdot OA + k \) - \( v \)

(-) ?

(+) ?

No
PROGRAM ROTC1
C DIMENSION CLAM(9,10),R(9,10),Z(9,10),THETA(9,10),
1 ALAM(9,10),DELTA(9,10),DDELTA(9,10),
2 PR(9),PLAM(9),GAMMA(9),PGAMMA(9),PRETA(9),DELN(9),
3 ADDELTA(9),DNSTAR(9),DL(9),DZ(9),CF(9),CURV(9,10),
4 PCURV(9),VY(9),Y2(9),Y3(9),DELX(9),DFL(9),WX(9),
5 DWSQ(9),IX(9),AX(9),FX(9),PTA(9),DDELTA(9),XLAM(9),
6 RX(9),WX(9),KXAMMA(9),XDELA(9),GAMX(9),WX(9),KCEL(9),
7 ZBETA(9),GML(9),YDELTA(9),DKCC(9),DDELTA(9),TKEG(9),
8 COMMON M,DELM,ATHTA,NC,CTEM,PTETA,PDELTA,PGAMMA,PLAM,
9 AR,RC,DNSTAR,DELTA,NDCO,ALAM,NS,D1,D2,CURV,PCURV,MC,
10 X1,X2,X3,N,NCDEL,DWSQ,OMEGA,CX,AX,QA,QC,
11 X111,X222,X333,PLAM,M,N=1,NC
READ 10,MC,NC,NS
11 FORMAT(6F10.0)
10 FORMAT(3I10)
READ 11,(DELM(M),M=1,MC)
READ 11,(R(P,N),N=1,NO),M=1,MC)
READ 11,(Z(P,N),N=1,NO),M=1,MC)
READ 11,(PLAM(M,N),N=1,NO),M=1,MC)
READ 11,(THETA(N,N),N=1,NO),M=1,MC)
READ 11,(DELTA(M,N),N=1,NO),M=1,MC)
READ 11,CF(1,N),N=1,NC)
READ 11,(CURV(N,N),N=1,NC)
READ 90,CM,OMEGA,QA
90 FORMAT(2F15.0)
READ 11,(DELM(M),M=1,MC)
READ 11,(DELM(M),M=1,MC)
READ 11,THICK,RLNC
DO 12 M=1,MC
CO 12 N=1,NO
C = 3.1415925/180.
ALAM(M,N) = PLAM(M,N) * C.
ATHTA(M,N) = THETA(M,N) * C.
ADELA(M,N) = DELTA(M,N) * C.
12 CONTINUE
M = 1
CALL LETC(NS)
AR(M) = R(M,NS)
PDDELTA(M) = ADDELTA(M,NS)
CALL ANGLE
GAMMA(M) = PGAMMA(M) / C
DNSTAR(M) = C.
DM(1) = C.
PLAM(M) = ALAM(M,NS)
PTETA(M) = PRETA(M) / C.
DDELTA(M) = PDELTA(M) / C.
XLAM(M) = PLAM(M) / C.
PRINT 929
929 FORMAT(1H1)
13 FORMAT(10X39HLOCATION OF POINTS ON CHARACTERISTIC ///)
PRINT 13
14 FORMAT(2H,M8X5HGAMMA1CX6HONSTAR9X4HBETA11X5HDELTA10X5HLANDA
1 12X11=12X2HON///)
PRINT 15,M,GAMMA(M),DNSTAR(M),PTETA(M),CELTA(M),XLAM(M),AR(M),
1 DM(M)
15 FORMAT(12,7F15.4///)
DO 16 M=2,MC
NDCO = C.
NP = DNSTAR(M-1) / DELN(M-1)
NE = NS+NP
IF(PLAM(N-1. .7854) 17,17,18
17 ADM = (R(M,NE)-R(M-1,NE)) / CCSF(PLAM(M-1))
DM(M) = ABSF(ADM)
GO TO 19
18 ADM = (Z(M,NE)-Z(M-1,NE)) / SINF(PLAM(M-1))
DM(M) = ABSF(ADM)
16 DNSTAR(M) = DNSTAR(M-1)+DM(M)*TANF(PGAMMA(M-1))
17 IF(DNSTAR(M)) 20,21,22
20 CALL PSTAR(NS,-1,-1,)
GO TO 23
22 CALL PSTAR(NS-NS,1,1.)
111
GO TO 23
21 CALL 'CTD(NS)
PLAM(M) = ALAM(M,NS)
PDELA(M) = ADELA(M,NS)
AR(M) = R(M,NS)
CALL ANGLE
IF (PGAMMA(M)) 24, 23, 25
24 CALL PSTAR(NS,-1,-1.)
GO TO 23
25 CALL PSTAR(NS-NS, 1, 1.)
23 CONTINUE
IF(I-NCGO) 26, 26, 28
26 PRINT 27,M
27 FORMAT(27HINSUFFICIENT GRID WIDTH M=, I2)
GO TO 55
28 GAMMA(M) = PGAMMA(M)/C
BETA(M) = PBETA(M)/C
DDELTA(M) = PDELTA(M)/C
XLAM(M) = PLAM(M)/C
PRINT 15,M,GAMMA(M),DNSTAR(M),BETA(M),DDELTA(M),XLAM(M),AR(M),
1 DM(M)
16 CONTINUE
PRINT
951 FORMAT(1H1,20X12HTEST FOR COY//)
PRINT 952
952 FORMAT(2H M3X2HNX8X6HD2TCH29X6HD2TDN11X2HD113X2HD212X4HCURV///)
CALL COY
CONTINUE
PRINT 97C
97C FORMAT(1H1,5X,6HY TEST /////)
DO 31 M=1,MO
Y1(M) = COSF(PGAMMA(M))*2.0*PCURV(M)*(COSF(PBETA(M)))**2
1+SIGN(2.0*PBETA(M)*D2(M))**12.
Y2(M) = 2.0*COSF(PGAMMA(M))*SINF(2.0*PBETA(M))*C1(M)
1/COSF(PDELTA(M))
Y3(M) = (DHC(HM)-OMEGA*DFL(M))*COSF(PLAM(M))*2.
1*COSF(PGAMMA(M))*CPCF(PBETA(M))***2
PRINT 971,M,Y1(M),Y2(M),Y3(M)
31 CONTINUE
PRINT 972
972 FORMAT(1H1,5X,8HVEL TEST ///)
EE = .001.
WM1) = '0.'
I = 1
32 WDEL = 100.0*(-.1**(I-1))
WM1I) = WM1(1)+WDEL
CALL RELVEL
IF (ABS(FDEL)•EE) 38, 38, 33
33 IF (QDEL) 32, 38, 34
34 I = I+1
35 WDEL = 100.0*(-.1**(I-1))
WM1(1) = WM1(1)+WDEL
CALL RELVEL
IF (ABS(FDEL)•EE) 38, 38, 36
36 IF (QDEL) 37, 38, 35
37 I = I+1
GO TO 32
28 CONTINUE
PRINT 981
981 FORMAT(1H1,13HTEST FOR XDEL///)
PRINT 982
982 FORMAT(3H M,3H J,15H FLOW FRACTION ,15H CAL FLOW RATE ,
15H DLLTA X ,4))/
983 FORMAT(3X,F15.4)
WX(1) = WM1(1)
WX(MO) = WM1(MO)
RX(1) = AR1)
RX(MO) = AR(MO)
XR1A(1) = PBETA(1)
XR1A(MO) = PBETA(MO)
XGAMMA(1) = PGAMMA(1)
XGAMMA(MAX) = PGAMMA(MAX)
YDELTA(1) = PDELTA(1)
YDELTA(MO) = PDELTA(MO)
M01 = MO - 1
DO 950 K = 2, MO1
KK = MO1 - K
F = FLOATF(MO - K) / FLOATF(MO - 1)
QAF = CA*F
EE = .001
CALL FLOW(KK, 0.)
IF (ABS(QC - QAF) - EE) 50, 5C, 140
40 XDEL(KK) = .2
PRINT 983, XCEL(KK)
DDD = XDEL(KK)
41 CALL FLOW(KK, DDD)
IF (QC - QAF) 42, 50, 43
42 XDEL(KK) = XDEL(KK) + .1
DDD = XDEL(KK)
PRINT 983, XDEL(KK)
C ... DRIVES CC GREATER THAN QA TO START
GO TO 41
43 J = 1
44 XDEL(KK) = XDEL(KK) + 1* (-1** (J - 1))
DDD = XDEL(KK)
PRINT 983, XCEL(KK)
45 IF (QC - QAF) 46, 50, 44
46 J = J + 1
47 XDEL(KK) = XDEL(KK) + 1* (-1** (J - 1))
DDD = XCEL(KK)
PRINT 983, XCEL(KK)
48 IF (QC - QAF) 47, 50, 49
49 J = J + 1
GO TO 44
50 CONTINUE
PRINT 980, KK, J, F, QC, XDEL(KK)
980 FORMAT(2I3, 3F15.4)
950 CONTINUE
984 FORMAT(1H1, 16HVELOCITY PROFILE//)
PRINT 985
985 FORMAT(2H M8X6HRACIUS4X1CHBLADE ANGLE8X5H GAMMA9X2HWM
11H REL VELOCITY W ///)
DO 51 M = 1, MO
ZPETA(M) = XBETA(M) / C
GAMX(M) = PGAMMA(M) / C
W(M) = W(X(M))**SRTF(1.+ (TANF(XBETA(M))**2))
PRINT 986, M, RX(M), PETA(M), GAMX(M), WX(M), W(M)
986 FORMAT(12, 5F15.4)
TKEQV(M) = (THICK/COSF(XBETA(M)))**SRTF(1.+ (SINF(I(XBETA(M))**2))**2))
DWCO(M) = (6.2332/SLNC-TKEQV(M)/RX(M))**COSF(XBETA(M))
DWFUNC(M) = RX(M)**(KXM)*TANF(XBETA(M))**12.+OMEGA**RX(M)
1RXM(M)
51 CONTINUE
PRINT 880
880 FORMAT(1H1 /////////// 25X9H TABLE ///17X
127H DATA FOR CHARACTERISTIC CI///)
C CHANGE CHAR. NO. FOR EACH COMPUTATION
982 FORMAT(6H M = 9X2H 19X1H2 9X1H3 9X1H4 9X1H5///)
PRINT 883
883 FORMAT(13X33H LOCATION OF CHARACTERISTIC CURVE///)
PRINT 884, NS
884 FORMAT(23H STARTING NORMAL NO. = ,12//)
PRINT 882
885 FORMAT(10H GAMMA = ,5F10.4)
PRINT 897, (GML(M), M = 1, 5)
897 FORMAT(10H GAM-LAM = ,5F10.4)
PRINT 896, (DNSTAR(M), M = 1, 5)
886 FORMAT(10H DNSTAR = ,5F10.4)
PRINT 887, (BETA(M), M=1,5)
887 FORMAT (1CH BETA(P) =, 5F10.4)
PRINT 888, (AR(M), M=1,5)
888 FORMAT (1CH RADIUS =, 5F10.4)
PRINT 889
889 FORMAT (16X28H LOCATION OF NEW STREAMLINES//)
PRINT 882
PRINT 882, XDEL(1)=C.
XDEL(MC)=0.
PRINT 890, (XDEL(M), M=1,5)
890 FORMAT (10H DELTA X =, 5F10.4)
PRINT 891, (ZBETA(M), M=1,5)
891 FORMAT (1CH BETA(X) =, 5F10.4)
PRINT 892, (RX(M), M=1,5)
892 PRINT 892
892 FORMAT (2)X17H VELOCITY PROFILE//)
PRINT 892
PRINT 893, (WM(M), M=1,5)
893 FORMAT (1CH WM(P) =, 5F10.4)
PRINT 894, (WX(M), M=1,5)
894 FORMAT (1CH WX(X) =, 5F10.4)
PRINT 895, (W(M), M=1,5)
895 FORMAT (1CH REL VEL =, 5F10.4)
PRINT 895, (CWCO(M), M=1,5)
895 FORMAT (1CH CW COEF =, 5F10.4)
PRINT 895, (CWFUNC(M), M=1,5)
895 PRINT 896
896 FORMAT (6H M = B8X2H 69X1H7 9X1H8 9X1H9//)
PRINT 896
PRINT 896
PRINT 896
PRINT 896
PRINT 896
PRINT 896, NS
PRINT 896
PRINT 896, (GAMMA(M), M=6,9)
PRINT 897, (GML(M), M=6,9)
PRINT 898, (DNSTAR(M), M=6,9)
PRINT 899, (BETA(M), M=6,9)
PRINT 899, (AR(M), M=6,9)
899 FORMAT (10H RADIUS =, 4F10.4)
PRINT 899
PRINT 899
PRINT 899
PRINT 899
PRINT 899
PRINT 899, (XDEL(M), M=6,9)
PRINT 899, (ZBETA(M), M=6,9)
PRINT 899, (RX(M), M=6,9)
PRINT 902
PRINT 902
PRINT 902
PRINT 902
PRINT 902, (WM(M), M=6,9)
PRINT 903, (WX(M), M=6,9)
PRINT 903, (W(M), M=6,9)
PRINT 906, (CWCO(M), M=6,9)
PRINT 907, (CWFUNC(M), M=6,9)
PRINT 907
PRINT 907
PRINT 907
PRINT 907
PRINT 907
PRINT 907
PRINT 907
PRINT 907
PRINT 907
PRINT 907
PRINT 907
PRINT 907, (DWFUNC(M), M=6,9)
PRINT 907, (DWFUNC(M), M=6,9)
860 FORMAT (1H1, 4H END)
55 CONTINUE
END
Program Rotor I

Subroutine PSTAR

Initialize for +or- dN^o

Increase ΔN

|ΔN| - ΔN

Calculate dθ/dm at P

Calculate R, δ at P

Calculate β, γ' at P

2nd Loop?

Yes → END

No

Tan γ' = ?

Calculate δN

dN^o = dN^o + δN
SUBROUTINE PSTARI(NN,JO,R)

DIMENSION DLAM(9,10),R(9,10),Z(9,10),THETA(9,10),

1ALAM(5,10),ATHETA(9,10),DELTA(9,10),ADELTA(9,10),

2AR(9),PLAM(9),GAMMA(9),PAMMAM(9),PETA(9),DELN(9),

3PDDELTA(9),NDSTAR(9),CM(9),D1(9),D2(9),CURV(9,10),

4LCURV(9),Y1(9),Y2(9),Y3(9),OHEDN(9),DFL(9),WM(9),

5DWSC(9),DX(9),AX(9),FX(9),EBETA(9),PDDELTA(9),XLAM(9),

6RX(9),WX(9),XGAMMA(9),XETETA(9),GAMX(9),W(9),XCEL(9),

7ZBETA(9),GML(9),YCELTA(9),DWOOG(9),DFWUNG(9),TKECV(9),

COMMON M,DELN,ATHETA,NO,DTRM,PETE,PDDELTA,PGAMMA,PLAM,

1AR,R,CM,NDSTAR,ADDELTA,NOGO,ALAM,NS,D1,D2,CLMT,PCLMT,MC,

2Y1,Y2,Y3,WM,QLAM,WSG,OMEGA,DX,AX,QA,QC,

3WX,RX,XGAMMA,XETETA,YDELTA

CO 30C I=1,2

CEL = DELN(M)

DO 301 K=1,NN

NA=NS+JO*(N-1)

NB = NA+JO*K

X = (CNSTAR(M)-B*CEL)/DELN(M)

IF(ABS(CNSTAR(M))-CEL)302,303,304

304 DEL = DELN(M)*FLOATF(K+1)

GO TO 301

302 CALL CTD(NR)

DT1 = DT0M

CALL CTD(NA)

DT2 = C1M

DT0M = DT1-B*(DT2-CT1)*X

AR(M) = R(M,NA)-B*(R(M,NA)-R(M,NB))*X

PDDELTA(M) = ADELTA(M,NB)-B*(ADELTA(M,NA)-ADELTA(M,NB))*X

GO TO 305

303 CALL CTD(NR)

AR(M) = R(M,NB)

PDDELTA(M) = ADELTA(M,NB)

305 CALL ANGLE

PLAM(M) = ALAM(M,NR)-B*(ALAM(M,NA)-ALAM(M,NB))*X

IF(I-1)306,306,300

306 TGAMD = TANF(PGAMMA(M))-TANF(PGAMMA(M-1))

IF(TGAMD)307,300,300

307 EN = (DM(M)*TGAMD)/2.

ONSTAR(M) = CNSTAR(M)*EN

GO TO 300

301 CONTINUE

NOGO = 1

300 CONTINUE

END
SUBROLTINE DTD(N)
DIMENSION DLAM(9, 10), R(9, 10), Z(9, 10), THERMA(9, 10),
  DLAM(9, 10), ATHETA(9, 10), DELTA(9, 10), ADELTA(9, 10),
  2R(9), PLAM(9), GAMMA(9), PGAMMA(9), PRETA(9), CELN(9),
  3PDELTA(9), ONSTAR(9), CM(9), D1(9), D2(9), CURV(9, 10),
  4PCURV(9), Y1(9), Y2(9), Y3(9), DHEON(9), DL(9), WM(9),
  5GWSC(9), CX(9), AX(9), FX(9), RETA(9), DDELTA(9), XLAM(9),
  6RX(9), WX(9), XGAMMA(9), XETA(9), GMX(9), W(9), XDEL(9),
  7ZBETA(9), GML(9), YDELT(9), DWSC(9), DWFUNC(9), TKECV(9),
  COMMON M, DELN, ATHETA, NO, DTM, PRETA, DDELTA, GAMMA, PLAM,
  AR, R, CM, DELN, ADELTA, NOGO, ALAM, NS, D1, D2, CURV, PCURV, MC,
  2Y1, Y2, Y3, WM, QDEL, DWSC, CMGAM, DX, AX, QA, CC,
  3RX, RX, XGAMMA, XETA, YDELT
DELTA = 12.*DELN(M)
IF(N-2) 100, 100, 1C1
100 DTM = (-25.*ATHETA(M,N)+48.*ATHETA(M,N+1)-36.*
  1ATHETA(M,N+2)+16.*ATHETA(M,N+3)-3.*ATHETA(M,N+4))/DELTA
GO TO 104
101 NREM = NC-N
IF(NREM-1) 102, 102, 163
102 DTM = (3.*ATHETA(M,N-4)-16.*ATHETA(M,N-3)+36.*
  1ATHETA(M,N-2)-48.*ATHETA(M,N-1)+25.*ATHETA(M,N))/DELTA
GO TO 1C4
103 DTM = (ATHETA(M,N-2)-ATHETA(M,N+2) -8.*(ATHETA(M,N-1)
  1-ATHETA(M,N+1))/DELTA
104 CONTINUE
END
SUBROUTINE ANGLE

DIMENSION DLAM(9,1C), R(9,1C), Z(9,10), THETA(9,10),
1ALAM(9,10), ATHETA(9,1C), DELTA(9,10), ADELTA(9,10),
2AR(9), PLAM(9), GAMMA(9), PGAMMA(9), PRETA(9), CELN(9),
3PDELTA(9), CNSTAR(9), DM(9), D1(9), D2(9), CURV(9,10),
4PCURV(9), Y1(9), Y2(9), Y3(9), DHEDN(9), DFL(9), W(9),
5DWSC(9), UX(9), AX(9), FX(9), HETA(9), DDELTA(9), XLAM(9),
6RX(9), WX(9), XGAMMA(9), XBETA(9), GAMX(9), W(9), XCEL(9),
7ZPRETA(9), GLM(9), YDELTA(9), DWD(9), DFLAC(9), TKEQV(9),
COMMON M, DELN, ATHETA, NO, DTM, PRETA, PDELTA, PGAMMA, PLAM, AR, CM, DNSTAR, ADELTA, NOCC, ALAM, NS, D1, D2, CURV, PCURV, M, NO,
2Y1, Y2, Y3, WM, QDEL, DWSC, OMEGA, CX, AX, QA, QC,
3WX, RX, XGAMMA, XPETA, YDELTA

TBETA = AR(M) * DTM
PRETA(M) = ATANF(TPETA)
TGAMMA = (SINF(PRETA(M)) * 2) * TANF(PDELTA(M))
PGAMMA(M) = ATANF(TGAMMA)
END
Subroutine COY

Initialize for $dN^* = +, -, or 0$

Locate Grid Points Adjacent to $P^*$

Calculate $d\theta/dm$ at Grid Points

Calculate $d\theta/dm$ at $P^*$

Calculate $d^2\theta/dm^2$

Locate Adjacent S.L.'s on Normal

Calculate $d\theta/dm$ at Three Grid Points on Normal

Calculate $d^2\theta/dn dm$

Calculate $D_1, D_2$

Calculate $k_m$ at $P^*$

[end]
SUBROUTINE COY

DIMENSION DLAMI9, R(9, 10), Z(9, 10), THETA(9, 10),
1 ALAM(5, 10), ATHEIA(9, 10), DELTA(9, 10), ATHETA(9, 10),
2 AR(9), PLAM(9), GAMMA(9), PGAMMA(9), PBETA(9), DELN(9),
3 PDELTA(9), ONSTAR(9), DM(9), D1(9), D2(9), CURV(9, 10),
4 PCURV(9), Y1(9), Y2(9), Y3(9), DHEDN(9), DFL(9), WM(9),
5 DWSQ(9), YX(9), FX(9), BETA(9), DDELTA(9), XLAM(9),
6 RX(9), WX(9), XGAMMA(9), XBETA(9), GAMX(9), W(9), XCEL(9),
7 ZBETA(9), GML(9), YDELT(9), DELTA(9), CWCO(9),
8 DDELTA(9), DNSTAR(9), DM(9), D1(9), D2(9), CURV, PCURV, MO,
9 2Y1, Y2, Y3, WM, QDEL, DWSQ, OMEGA, DX, AX, QA, CC,
3 NW, RX, XGAMMA, XBETA, YCELTA

DO 400 M = 1, MC
NX = CNSTAR(M)/DELN(M)
IF(NSTAR(M)) 401, 402, 403

401 NA = NS+NX
NB = NA-1
XA = -CNSTAR(M)+FLOAT(NX)*DELN(M)
XB = XA-CELN(M)
JO = -1
R = 1.
GO TO 404

402 NA = NS+NX
NB = NA-1
XA = CELN(M)
XB = -XA
JO = -1
R = 1.
GO TO 404

403 NE = NS+NX
NA = NB+1
XB = -CNSTAR(M)+FLOAT(NX)*DELN(M)
XA = CELN(M)-XB
JO = 1
R = -1.
CALL CTC(NA)

CA = CTCM
CALL CTD(NB)
DB = CTDM
DC = TANF(PBETA(M))/AR(M)
C2TCM2 = (XAXA*(DC-DC)-XB*XB*(DA-DC))/
1(XAXA*XB-XB*XB*XA)
NN = NS+NX
IF(MO-2-M) 405, 406, 406

405 ZA = CM(M)
M2 = M
K = M-1
ZB = ZA-CM(M)
CALL CTD(NN)
DNA = CTCM
M = M-1
CALL CTC(NN)
DNB = DTD(1)
M = M2
GO TO 407

406 M2 = M
M = M+1
ZB = ZB+CM(M)
CALL CTC(NN)
DNA = DTCM
M = M+1
ZB = ZA+CM(M)
CALL CTC(NN)
DNB = DTD(M)
M = M2
GO TO 407

407 CALL DTD(NN)
CNO = DTDM
C2TCNM = (ZB*ZB*(DNA-CNO)-ZA*ZA*(DNB-CNO))/
1(ZP*ZB*ZA-ZA*ZB*ZB)
ALFA = PDELTA(M)-PLAM(M)
D1(M) = CCM(1)
D2(M) = (2.*TANF(PBETA(M))*D1(M))/(AR(M)*CCSF(PDELTA(M))))
1 + AR(Y) * (1 ANF(PELTA(M)) * C2TNM2 + D2TNM) 
IF(M-1) 408, 4CH, 4CS 
408 PCURV(1) = CURV(1, NS) 
954 GO TO 950 
C---REPLACE WITH (GCTC 4CO) 
409 AM = FLOATF(M-1)/FLOATF(M-1) 
CURV(M, NN) = CURV(1, NN) + (CURV(M0, NN) - CURV(1, NN)) * AM 
CURV(M, NN+JO) = CURV(1, NN+JO) + (CURV(M0, NN+JO) - CURV(1, 
1NN+JO)) * AM 
X = UNSTAR(M)/DELN(M) - FLOATF(NX*JO) 
PCURV(M) = CURV(M, NN) - 6 * (CURV(M, NN+JO) - CURV(M, NN)) * X 
950 CONTINUE 
PRINT 953, M, NX, D2TCN2, D2TNM, D1(M), D2(M), PCURV(M) 
953 FORMAT(12, I5, 5F15.4/) 
400 CONTINUE 
END
Subroutine RFLVEL

Calculate $dx_i$

Calculate $x_i$

Calculate $\left(\frac{dW^2}{dx}\right)_{i-1}$

Calculate $W_{mi}$

Calculate $\frac{dW^2}{dx}$

Calculate $W_{mi}$

Calculate $QC$

$\Delta Q = QC - QA$

$S.R. \ FLOW$

$\text{All S.L.'s?}$

No

Yes

END

122
SUBROUTINE PELVEL

DIMENSION DLAM(9,1C), R(9,1C), Z(9,1C), TFETA(9,1C),
1 ALAM(9,1C), ATFETA(9,1C), CELTA(9,1C),
2 AR(9), PLAM(9), GAMMA(9), PGAMMA(9), PRETA(9), DELN(9),
3 PDELTA(9), DNSTAR(9), DK(9), D1(9), D2(9), CURV(9,1C),
4 PCURV(9), Y1(9), Y2(9), Y3(9), CHEDN(9), DFL(9), WM(9),
5 DWSQ(9), DX(9), AX(9), FX(9), PRTA(9), DDELTA(9), XLAM(9),
6 RX(9), WX(9), XGAMMA(9), XBETA(9), GAMX(9), W(9), XCEL(9),
7 ZBETA(9), GM(9), YDELTA(9), DWCC(9), DWFNC(9), TKECV(9),

COMMON M, CELN, ATHETA, NO, CTCM, PRETA, PDELTA, PGAMMA, PLAM,
1 AR, R, CM, DNSTAR, ALTETA, NOGC, ALAM, NS, D1, C2, CURV, PCURV, MC,
2 Y1, Y2, Y3, WM, QDEL, CWSG, OMEGA, DX, AX, QA, GC,
3 WX, RX, XGAMMA, XBETA, YDELTA

975 FORMAT(1CX, 1HM, 10X, 2HWdM)
AX(1) = 0.
PRINT 973, M, WM(1)
DO 500 M=2, M0

CX(M) =DX(M)/CCSF (PGAMMA(M-1))
AX(M) = AX(M-1) + DX(M)

1-WM(M-1)*OMEGA*Y2(M-1)
WSQ = WM(M-1)**2 + CWSQ(M-1)*DX(M)/12.
WM(M) = SQRTF(WSQ)

DWSQ(M) = Y3(M)*WSQ + Y1(M) - WM(M-1)*OMEGA*Y2(M)
WSQ = WM(M-1)**2 + ((DWSQ(M-1) + DWSQ(M))/2.)*DX(M)/12.
WM(M) = SQRTF(WSQ)
PRINT 973, M, WM(M)

973 FORMAT(I IC, F15.4)
500 CONTINUE
CALL FLCW(M0, C.)
QDEL = CC-CA
PRINT 974, QDEL

974 FORMAT(/SHQC-CA = ,F10.4)
END
Subroutine FLOW

Initialize for sign of $\delta x$

Calculations at $(P^* + x)$:
$w_m, r, \gamma, \beta, \delta, E(x)$

Yes
Odd Number of S.L.'s ?

No

Calculate Coefficients $a, b$

Calculate: $DQ = \int_{m-1}^{m} E(x) \, dx$

Calculate Coefficients $a, b, c$

Calculate:
$DQ = \int_{m-2}^{m} E(x) \, dx$

$QC = QC + DQ$

All Intervals Computed ?

Yes
END

No
SUBROLTINE FLOW(MM, DELTAX)
DIMENSION DLAM(9,10), R(9,10), Z(9,10), THETA(9,10),
 IALAM(9,10), ATHERA(9,10), DELTA(9,10), ADELTA(9,10),
 2AR(9), PLAM(9), GAMMA(9), PGAMMA(9), PBETA(9), DELN(9),
 3PDELTA(9), DNSSTAR(9), CM(9), D1(9), D2(9), CURV(9,10),
 4PCURV(9), Y1(9), Y2(9), Y3(9), DHEDN(9), DFL(9), W(9),
 5DWSO(S), LX(9), AX(9), FX(9), BETA(9), DDELTA(9), XLAN(9),
 6CM(9), DLAM(9), XLAN(9), XHUM(9), CM(9), D1(9), D2(9), CURV(9,10),
 7ZBETA(9), GMUX(9), YCELTA(9), DWCC(9), DWFUNC(9), TKECV(9),
 COMMON M, DELN, ATHERA, NO, DTM, PBETA, PDELTA, PGAMMA, PLAM,
 1AR, R, CM, DNSSTAR, ADELTA, NOC0, ALAM, NS, D1, D2, CURV, PCURV, MO,
 2Y1, Y2, Y3, WM, QDEL, DWSQ, OMEGA, DX, AX, QA, QC,
 3WX, RX, XGAMMA, XBETA, YDELTA
IF (DELTAX) 620, 620, 630
620 JD=0
GO TO 640
630 J=1
640 CONTINUE
RX(MM) = AR(MM) + DELTAX*COSF(PGAMMA(MM) + PLAM(MM))
WX(MM) = WM(MM) + (DELTAX*DSQ(MM))/((24.*WM(MM)))
XGAMMA(MM) = PGAMMA(MM) + DELTAX*(PGAMMA(MM) - PGAMMA
 1(MM-1))/DX(MM+JD)
XBETA(MM) = PBETA(MM) + DELTAX*(PBETA(MM) - PBETA
 1(MM-1))/DX(MM+JD)
YDELTA(MM) = PDELTA(MM) + DELTAX*(PDELTA(MM) - PDELTA
 1(MM-1))/DX(MM+JD)
FX(MM) = RX(MM) + WX(MM)*COSF(XGAMMA(MM))
GO TO 600
CONTINUE
GC = C.
I = 1
606 IQ = I+2
IF (IQ-MM) 601, 607, 6C2
607 AA = FX(I)
X1 = CX(I+1)
X2 = X1+DX(I+2)
PR = (X2*X2*FX(I+1) - X1*X1*FX(I+2) - AA*(X2*X2-X1*X2))/1.
CC = (X2*(FX(I+1)-FX(I)) - X1*(FX(I+2)-FX(I)))/1.
XAX = AX(I+2) + DELTAX
DO = (AA*(XAX-AX(I)) + BB*(XAX*X2-AX(I)X2))/2.
1+CC*(XAX*X2-AX(I)X3)/3.)/144.
GO TO 603
601 AA = FX(I)
X1 = CX(I+1)
X2 = X1+DX(I+2)
RB = (X2*X2*FX(I+1) - X1*X1*FX(I+2) - AA*(X2*X2-X1*X2))/1.
CC = (X2*(FX(I+1)-FX(I)) - X1*(FX(I+2)-FX(I)))/1.
XAX = AX(I+2) + DELTAX
DO = (AA*(AX(I+2)-AX(I)) + BB*(AX(I+2)X2-AX(I)X2))/2.
1+CC*(AX(I+2)X2-AX(I)X3)/3.)/144.
GO TO 603
602 A=FX(I)
XY = CX(I+1)
XX = CX(I+1) + DELTAX
B = (FX(I+1) - FX(I)) / XY
CC = (A*XX + B*(AX(I+1) + DELTAX)) / (2 - (AX(I+1) + DELTAX))/2. /144.
GO TO 603
603 CC = CC+LC*6.25
IF (IQ-MM) 604, 605, 605
604 I = I+2
GO TO 606
605 CONTINUE
END
Program ROTOR 2

Main Program

Read Input

Angles to radians

Calculate all $\beta$'s

Calculation at Initial Point:

- $R$
- $k_m$
- $dN^* = 0$
- $DM^* = 0$

Calculate $DM$

Calculate $dN^*$

S.R. PSTAR for $+dN^*$

$dN^* = ?$

S.R. PSTAR for $-dN^*$
Calculations for $dN^* = 0$

$\gamma' = ?$

S.R. PSTAR for $+\gamma'$

Sufficient Grid? No → END

Yes

All S.L.'s ?

Yes

S.R. DDL

Elements of $Y'$s

Calculate $Y'$s

Yes

All S.L.'s ?

No

127
S.R. RELVEL

Relative velocity Distribution

\[ W_m = W_{mH} + dW \]

\[ dW = 100 \]

\[ W_{mH} = 0 \]

Initial to correct Streamlines

\[ QAF = QA \left( \frac{M_i}{M_f} \right) \]

Calculations At \( P_H^* \) and \( P_T^* \)

Increment \( dW \)

\[ |\Delta Q| - \epsilon \]

\((-\)

\((+)\)

\((0)\)
5

All S.L.'s?

Yes

Calculate W

Calculations for Blade to Blade

All S.L.'s?

Yes

Print Final Results

END
PROGRAM Rotor 2

DIMENSION DLAM(9, 10), R(9, 10), Z(9, 10), ABETA(9, 10),
1 ALAM(9, 10), ETA(9, 10), DELTA(9, 10), ADELTA(9, 10),
2 AR(9), PLAN(9), GAMMA(9), PGAMMA(9), PBETA(9), CELN(9),
3 PDELTA(9), DNSTAR(9), DM(9), D1(9), D2(9), CURV(9, 10),
4 PCURV(9), Y1(9), Y2(9), Y3(9), DHEDE(9), DFL(9), WM(9),
5 CWSQ(9), DX(9), AX(9), FX(9), APBETA(9), ODELTA(9), XLAM(9),
6 RX(9), W(9), XGAMMA(9), XBETA(9), GAPX(9), W(9), XDEL(9),
7 TETA(9), GML(9), YDELTA(9), DWCO(9), DWFUN(9), TKEQV(9),
8 PDELTA(9), ETA(9), PRETA, PDELTA, PGAMMA, PLAN,
1 AR, R, DM, ONSTAR, ADelta, NOGO, ALAM, NS, O1, O2, CURV, PCURV, MO,
2 Y1, Y2, Y3, WM, QDEL, DSOC, OMEGA, EX, AX, QA, CC,
3 WX, RX, XGAMMA, XPETA, YDELTA

READ 10, MC, NC, NS,
10 FORMAT(6F10.0)
READ 11, (DELN(M), M = 1, M0)
READ 11, (R(M, N), N = 1, N0), M = 1, M0)
READ 11, (Z(M, N), N = 1, N0), M = 1, M0)
READ 11, (DLAM(M, N), N = 1, N0), M = 1, M0)
READ 11, (ETA(1, N), N = 1, NO)
READ 11, (ETA(9, N), N = 1, NO)
READ 11, (DELTA(M, N), N = 1, N0), M = 1, M0)
READ 11, (CURV(1, N), N = 1, NO)
READ 11, (CURV(9, N), N = 1, NO)
READ 50, OMEGA, QA
90 FORMAT(2F15.0)
READ 11, (DHEDE(M), M = 1, M0)
READ 11, (DFL(M), M = 1, M0)
READ 50, THICK, RLNO
DO 12 M = 1, M0
CO 12 N = 1, N0
C = 3, 14159/180.
ABETA(M, N) = ETA(M, N) * C
ALAM(M, N) = DLAM(M, N) * C
ADELTA(M, N) = ODELTA(M, N) * C
12 CONTINUE
DO 29 N = 2, M0-1
ABETA(M, N) = ABETA(1, N) + (ABETA(9, N) - ABETA(1, N)) * AM
29 CONTINUE
CO 997 N = 1, N0
CO 997 N = 1, N0
BETA(M, N) = ABETA(M, N) / C
997 CONTINUE
P = 1
AR(M) = R(M, NS)
PCURV(M) = CURV(M, NS)
PDELTA(M) = ADELTA(M, NS)
PBETA(M) = ABETA(M, NS)
TGMMA = (SIN(PBETA(M)) * 2) * TANF(PDELTA(M))
PGAMMA(M) = ATANF(TGMMA)
GAMMA(M) = PGAMMA(M) / C
DNSTAR(1) = 0.
DM(1) = 0.
PLAN(M) = ALAM(M, NS)
APBETA(M) = PBETA(M) / C
QDELTA(M) = PDELTA(M) / C
XLAM(N) = PLAN(M) / C
GLM(M) = GAMMA(M) - XLAM(M)
CO 16 M = 2, M0
NOGO = 0
NP = DNSTAR(M-1, 1) / CELN(M-1)
NE = NS * KP
17 IF (PLAN(M-1) = 7954) 17, 17, 18
AD = (R(M, NE) - R(M-1, NE)) / COSF(PLAN(M-1))
DY(M) = ASIN(AD)
10 TO 16
18 AD = (Z(M, NE) - Z(M-1, NE)) / SINF(PLAN(M-1))
DY(M) = ASIN(AD)
19 DNSTAR(M) = DNSTAR(M-1) + EM(M) * TANF(PGAMMA(M-1))
IF(KPTA(M) = 0) 20, 20, 22
20 CALL PSTAR(NS,-1,-1.)
   GO TO 22
22 CALL PSTAR(NC-NS,1,1.)
   GO TO 23
21 PBETA(M) = APETA(M,NS)
   PLAM(M) = ALAM(M,NS)
   PCURV(M) = CURV(M,NS)
   PDELT(M) = ADELT(M,NS)
   AR(M) = R(M,NS)
   TGAMMA(SINF(PBETA(M))*2) = TANF(PDELT(M))
   PGAMMA(M) = ATANF(TGAMMA)
   IF(PGAMMA(M)) 24,23,25
24 CALL PSTAR(NS,-1,-1.)
   GO TO 23
25 CALL PSTAR(NO-NS,1,1.)
23 CONTINUE
26 PRINT 27,N.
27 FORMAT(27,HINSUFFICIENT GRID WIDTH M=-,I2)
   GO TO 55
28 GAMMA(M) = PGAMMA(M)/C
   PBETA(M) = PBETA(M)/C
   PDDELTA(M) = PDELT(M)/C
   XLAM(M) = PLAM(M)/C
   GML(M) = GAMMA(M)-XLAM(M)
16 CONTINUE
CALL DL
CONTINUE
CONTINUE
DI 31 M=1,MC
Y1(M) = COSF(PGAMMA(M))*(2.*PCURV(M)*(COSF(PBETA(M)))**2
1+SINF(2.*PBETA(M))=C2(M))**12.
Y2(M) = 2.*COSF(PGAMMA(M))=SINF(2.*PBETA(M))=D1(M)
1/COSF(PDELT(M))
Y3(M) = (DHCCN(M)-CMEGA*DFL(M))*COSF(PLAM(M))**2.*
1COSF(PGAMMA(M))*(CCSF(PBETA(M)))**2
31 CONTINUE
EE = .001
WM(1) = 0.
I = 1
32 WDEL = 1CO.*(-1)**(I-1)
   WM(1) = WM(1)+WDEL
   CALL RELVEL
   IF(ABSFX(DFL)-EE ) 30,38,33
33 IF(QDEL) 32,38,34
34 I = I+1
35 WDEL = 1CC.*(-1)**(I-1)
   WM(1) = WM(1)+WDEL
   CALL RELVEL
   IF(ABSFX(QDEL)-EE ) 38,32,36
36 IF(QDEL) 37,38,35
37 I = I+1
   GO TO 32
38 CONTINUE
   WX(1) = WM(1)
   WX(MO) = WM(MO)
   RX(1) = AR(1)
   RX(MO) = AR(MO)
   XPLTA(1) = PDELT(1)
   XHETA(1) = PBETA(1)
   XGAMMA(1) = PGAMMA(1)
   XGAMA(MO) = PGAMMA(MO)
   YDELT(A1) = PDELT(1)
   YDELT(MO) = PDELT(MO)
   MO1=M0-1
   DO SO K=2,M01
   KK = NC+1-K
   F = FLCATF(MO-K)/FLCATF(MC-1)
   QAF = QA=F
   EE = .001
   CALL FLOW(KK,C.)
   IF(ABSFX(C-QAF)-EE ) 38,35,36
40 XDEL(KK) = .2
   CDD = XDEL(KK)

132
CALL FLOW(KK,DDD)

IF(QC-QAF) 42, 50, 43

XDEL(KK) = XDEL(KK)+.1

DDD = XDEL(KK)

C... DRIVES QC GREATER THAN QA TO START

GO TO 41

43 J = 1

XDEL(KK) = XDEL(KK)-.1*(-1***(J-1))

DDD = XDEL(KK)

CALL FLOW(KK,DDD)

IF(ABS(QC-QAF)-EE) 50, 50, 45

44 J = J+1

45 IF(QC-QAF) 146, 50, 44

46 J = J+1

47 XDEL(KK) = XDEL(KK)-.1*(J-1))

48 IF(QC-QAF) 47, 50, 49

GO TO 44

50 CONTINUE

DO 51 M=1,MC

51 CONTINUE

PRINT 880 FORMACT(1H1///////////25X9H TABLE //17X
127H DATA FOR CHARACTERISTIC C9///)

C CHANCE CHAR. NO. FOR EACH COMPUTATION

880 FORMACT(6H M = 8X2H 19X1H2 9X1H3 9X1H4 9X1H5//)

PRINT 880 FORMACT(13X33H LOCATION OF CHARACTERISTIC CURVE///)

PRINT 893, NS

882 FORMACT(23H STARTING NORMAL NO. = 12///)

PRINT 882 PRINT 886, (CNSTAR(M), M=1,5)

884 FORMACT(1CH CNSTAR =, 5F1C.4)

PRINT 896, (GAM-LAM(M), M=1,5)

885 FORMACT(1CH GAMMA =, 5F1C.4)

PRINT 886, (APBETA(M), M=1,5)

887 FORMACT(1CH BETA(P) =, 5F1C.4)

PRINT 887, (AR(M), M=1,5)

888 FORMACT(1CH RADIUS =, 5F1C.4///)

PRINT 889 FORMACT(16X22H LOCATION OF NEW STREAMLINES///)

PRINT 889 PRINT 890, (XDEL(M), M=1,5)

890 FORMACT(1CH DELTA X =, 5F10.4)

PRINT 890, (ZBETA(M), M=1,5)

891 FORMACT(1CH BETA(X) =, 5F10.4)

PRINT 891, (RX(M), M=1,5)

892 FORMACT(21X17H VELOCITY PROFILE///)

PRINT 892 PRINT 892, (WM(p), M=1,5)

893 FORMACT(1CH WM(p) =, 5F1C.4)

PRINT 893, (WM(X), M=1,5)

894 FORMACT(1CH WM(X) =, 5F10.4)

PRINT 894, (W(p), M=1,5)

895 FORMACT(1CH REL VEL =, 5F10.4)

PRINT 895, (DWC01(M), M=1,5)

875 FORMACT(1CH CW COEF =, 5F1C.4)

PRINT 875, (CWFUNC(M), M=1,5)
874 FORMAT(10H CW FUNC =,5F10.0)
896 FORMAT(6H M = 8X2H 69X1H7 9X1H8 9X1H9///)
  PRINT 88C
  PRINT 883
  PRINT 884,NS
  PRINT 896
  PRINT 886,(CNSTAR(M),M=6,9)
  PRINT 897,(GML(M),M=6,9)
  PRINT 885,(GAMMA(M),M=6,9)
  PRINT 887,(APRETA(M),M=6,9)
  PRINT 878,(AR(M),M=6,9)
878 FORMAT(1CH RADIUS =,4F10.4///)
  PRINT 889
  PRINT 896
  PRINT 890,(XDEL(M),M=6,9)
  PRINT 891,(ZBETA(M),M=6,9)
  PRINT 878,(RX(M),M=6,9)
  PRINT 892
  PRINT 896
  PRINT 893,(WM(M),M=6,9)
  PRINT 894,(WX(M),M=6,9)
  PRINT 895,(W(M),M=6,9)
  PRINT 875,(DRAW(M),M=6,9)
  PRINT 874,(DFUNC (M),M=6,9)
  PRINT 86C
860 FORMAT(1H1,4H END)
55 CONTINUE
  END
Program Rotor 2

Subroutine PSTAR

Initialize for
+ or - dN*

Increase ΔN

(dN* - ΔN) ?

Calculations at P:
k, \beta, R, \delta

Calculate γ'

2nd Loop?

Yes END

No

Tan γ' = ?

(+)

(0)

(-)

Calculate δN:
dN* = dN* + δN

135
SUBROLINE PSTAR(NN,JC,B)
DIMENSION CLAM(9,10),R(9,10),Z(9,10),ABETA(9,10),
1ALAM(5,10),BETA(9,10),DELT(9,10),ADELA(9,10),
2AR(9),PLAM(9),GAMMA(9),PGAMMA(9),PBETA(9),DELT(9),
3PCURV(9),DNSTAR(9),GM(9),BM(9),D2(9),CURV(5,10),
4PDCURV(9),Y1(9),Y2(9),Y3(9),DHEDN(9),DEL(9),WM(9),
5SWSC(9),DX(9),AX(9),FX(9),APBETA(9),ODELTA(9),XLAM(9),
6RXY(9),WM(9),XGAMMA(9),XABETA(9),GARX(9),W(9),XDEL(9),
7ZPBTA(9),GNL(9),YDEL(9),CWCC(9),DWFNC(9),TKEQV(9),
8COMMON M,DELT,BETA,NC,PBETA,PDELT,PGAMMA,PLAM,
1ARR,CM,CNSTAR,ADDELTA,NOCO,ALAM,NS,D1,D2,CURV,PCURV,MC,
2Y1,Y2,Y3,WC,DEL,WSG,OMEGA,CX,AX,QA,GC,
3WXY,XYGAMMA,XABETA,YDELTA
DC 30C 1=1,2
DEL = DEXN(M)
DO 310 K=1,NN
   NA=NS+JC*(K-1)
   NB = NS+JC*K
   X = (CNSTAR(M)-B*DEL)/DELT(N)
   IF (ABS(FNSTAR(M))<DEL) 302,303,304
304 CEL = DEXN(M)*DRTF(K+1)
   GO TO 2G
302 AM = DRTF(M-1)/DRTF(MC-1)
   CURV(M,NA) = CURV(1,NA)+CURV(M0,NA)-CURV(1,NA)))*AM
   CURV(M,NB) = CURV(1,NB)+CURV(M0,NB)-CURV(1,NB)))*AM
   PDCURV(M) = CURV(M,NB)-R*(CURV(X,NA)-CURV(M,NA)))*X
   PBETA(M) = ABETA(M,NA)-B*(ABETA(M,NA)-ABETA(M,NB)))*X
   AR(M) = R(M,NB)-B*(R(M,NA)-R(M,NB))*X
   PDELT(M) = ADELA(M,NB)-B*(ADELA(M,NA)-ADELA(M,NB))*X
   GO TO 3G5
303 PBETA(M) = ABETA(M,NB)
   AR(M) = R(M,NB)
   PDELT(M) = ADELA(M,NB)
   AM = DRTF(M-1)/DRTF(MC-1)
   PCURV(M) = CURV(1,NA)+CURV(MC,NB)-CURV(1,NB)))*AM
305 CONTINUE
   TGAMMA=SINF(PBETA(M))*S2)* TANF(PDELT(M))
   PGAMMA(M) = ATANF(TGAMMA)
   PLAM(M) = ALAM(M,NN)-B*(ALAM(M,NA)-ALAM(M,NB))*X
   IF (I-1) 306,306,306,
306 TGMAD = TANF(PGAMMA(M))-TANF(PGAMMA(M-1))
   IF (TGAMAD) 3C7,3C0,3C0
307 END = (CM(M)*TGAMAD)/2.
   CNSTAR(X) = DNSTAR(M) + END
   GO TO 3G0
301 CONTINUE
   NOCO = I
300 CONTINUE
END
Subroutine DDL

Initialize for $dN^o = +,-,\text{ or } 0$

Locate Grid Points Adjacent to $P^o$

Compute $\frac{\partial \tan \theta}{\partial n}$ on Adjacent normals

Compute $\frac{\partial \tan \beta}{\partial n}$
Compute $\frac{\partial \tan \beta}{\partial m}$ at $P^o$

Compute $D_1, D_2$

All S.L.'s ?

No

Yes

END
SUBROUTINE DCL
DIMENSION DLX(9,1C), R(9,10), Z(9,10), APETA(9,1C),
1ALAM(5,1C), BETA(9,1C), DELTA(9,10), ADelta(9,10),
2AR(9), PLAM(9), GAMMA(9), PGAMMA(9), PBETA(9), CELN(9),
3PDELTA(9), CNSTAR(9), CM(9), D1(9), D2(9), CURV(9,1C),
4PCURV(9), Y1(9), Y2(9), Y3(9), DHEDN(9), DFL(9), WM(9),
5DWSQ(9), CX(9), AX(9), FX(9), APETA(9), DDELTA(9), XLAM(9),
6RX(9), WX(9), XGAMMA(9), XBETA(9), GAMX(9), W(9), XD DEL(9),
7ZI(9), GML(9), YDELTA(9), DWCC(9), DWFUNC(9), TKECV(9),
8CMCM, DELM, ABETA, NC, PBETA, PDELTA, PGAMMA, PLAM,
1ARM, CM, CNSTAR, ADELTA, NCCE, ALAM, NS, D1, C2, CLRV, PCLRV, M, 
2Y1, Y2, Z, WM, ODEL, CWSC, CMEGA, DX, AX, QA, LC,
3W, RX, XGAMMA, XBETA, YDELTA
DO 400 M=1,NX
NX=CNSTAR(M)/DELN(M)
IF(M-MC) 401, 402, 403
401 MM=M+1
MX=MM
CP=1
GO TO 403
402 MM=M-1
MX=M
BB=-1.
GO TO 405
403 IF(DNSTAR(M)) 404, 405, 405
404 NA=NS+NX
NB=NA-1
X=-DNST A(M)+FLGATF(NX)*DELN(M)
DEL=1.-X/DELN(M)
GO TO 406
405 NB=NS+NX
NA=NB+1
X=DNST A(M)-FLOATF(NX)*DELN(M)
DEL=X/DELN(M)
406 IF(X) 407, 408, 407
407 ADN=(TANF(ABETA(M,N), NA))-TANF(ABETA(M,N4)))/CM(MX)*BR
BN=(TANF(ABETA(M,N), NB))-TANF(ABETA(M,NB))/CM(MX)*BR
DTBN=BDN+ACN-BDN*DEL
DTBN=(TANF(ABETA(M,NA))-TANF(ABETA(M,NB))/CELN(M)
GO TO 408
408 NC=NS+NX
DTBN=(TANF(ABETA(M,NC))-TANF(ABETA(M,NC))/CM(MX)*BB
NA=NS+NX+1
NB=NS+NX
NB=NS+NX-1
DTBN=(TANF(ABETA(M,NA))-TANF(ABETA(M,NB)))/
1(DELN(M)*BB)
409 CONTINUE
D1(M)=CCSF(PDELTA(TAM), PLAM(M))
D2(M)=TANF(PDELTA(M))*CTBN+(D1(M)*TANF(PBETA
1(M)))/(AR(M)*CCSF(PDELTA(M)))
400 CONTINUE
END
Subroutine RELVEL

1. Calculate $dx_i$
2. Calculate $x_i$
3. Calculate $\left(\frac{dW_m}{dx}\right)_{i-1}$
4. Calculate $W_{mi}$
5. Calculate $\frac{dW_m^2}{dx_i}$
6. Calculate $W_{mi}$
7. Calculate $QC$
8. $\Delta Q = QC - QA$
9. ALL S.L.'s?
   - Yes: END
   - No: S.R. FLOW

139
SUBROUTINE RELVEL

DIMENSION DLAM(9,1C),R(9,1C),Z(9,10),ABETA(9,10),
1ALAM(5,1C),BETA(9,1C),DELTA(9,1C),DELTA(9,1C),
2AR(9),PLAM(9),GAMMA(9),PGAMMA(9),PETA(9),DELN(9),
3PDDELTA(9),CNSTAR(9),DM(9),C1(9),D2(9),CURV(9,1C),
4PCURV(9),Y1(9),Y2(9),Y3(9),DHED(9),NFL(9),WM(9),
5CWSQ(9),Y1(9),AX(9),FX(9),APBETA(9),DDELTA(9),XLAM(9),
6Y1(9),WYX(9),XGAMMA(9),XETA(9),GAMIX(9),W(9),XDEL(9),
7ZBETA(9),CML(9),YDELTA(9),DWCO(9),DKFUC(9),TKEQV(9),
COMMON M,DELN,ABETA,NC,PRETA,PDELTA,PGAMMA,PLAM,1AR,3CM,2NSST,NGO,ALAM,NS,CL1,CL2,CLRV,PCURV,MC,
2Y1,Y2,Y3,WQDEL,CWSC,OMEGA,CX,AX,CA,CC,
3WX,RX,XGAMMA,XYETA,YDELTA

DO 500 M=2,MC

DX(M) = DM(M)/CCSF(PGAMMA(M-1))
AX(M) = AX(M-1)+DX(M)
DWSQ(M-1) = Y3(M-1)-W(M-1)*Y1(M-1)
1-WSQ = W(M-1)**2 + CWSC(M-1)*DX(M)/12.
WM(M) = SQRTF(WSQ)
CWSQ(M) = Y3(M)-WSC*Y1(M)-WM(M)*OMEGA*Y2(M)
WSQ = WM(M-1)**2 + (CWSQ(M-1)+DWSQ(M)/2.)*DX(M)/12.
WM(M) = SQRTF(WSQ)

CONTINUE

CALL FLOX(MC,0.)
QDEL = CC-CA

END
Subroutine FLOW

Initialize for sign of \( \Delta x \)

Calculations at \((P^0 + x)\):
\[ W_m; R, \gamma, \Theta, \delta, E(x) \]

Yes

Odd Number of S.L.'s?

Calculate Coefficients \( a, b, c \)

Calculate:
\[ DQ = \int_{m-2}^{m} E(x) \, dx \]

\[ QC = QC + DQ \]

All Intervals Computed?

Yes

END

No

Calculate Coefficients \( a, b \)

Calculate:
\[ DQ = \int_{m-1}^{m} E(x) \, dx \]
SUBROUTINE FLOW(MM, DELTA)
DIMENSION CLAX(9,10), R(9,10), Z(9,10), ABETA(S,10),
1 ALAX(S,10), DELTA(S,10), DELTA(9,10), DELTA(9,1C),
2 AR(9), PLAM(9), GAMMA(9), PCARRAY(9), DARRAY(9), DELTAN(9),
3 PDELTAN(9), DMAX(9), PCARRAY(9), DARRAY(9), DELTAN(9),
4 PDELTAN(9), DMAX(9), PCARRAY(9), DARRAY(9), DELTAN(9),
5 PDELTAN(9), DMAX(9), PCARRAY(9), DARRAY(9), DELTAN(9),
6 RX(9), WX(9), XGAMMA(9), XBETA(9), GAMX(9), WX(9), XGAMMA(9),
7BETA(9), GML(9), YDELTAN(9), CC(9), PCDFN(9), TKEQV(9),
COMMON M, MM, GUNSTAR, DARRAY, NOSS, GAMMA, NS, D1, D2, CURV, PCURV, MC,
1 XY, ZY, WX, QDEL, CWSQ, OMEGA, EX, AX, QA, CC,
3 WX, RX, XGAMMA, XBETA, YDELTAN
IF (DELTA) 620, 622, 633
620 JG = 0
GO TO 640
630 JG = 1
640 CONTINUE
RX(MM) = AR(MM) + DELTA*COSF(PGAMMA(MM) - PLAN(MM))
WX(MM) = WM(MM) + (DELTA*QWSQ(MM))/(2.4*WM(MM))
XGAMMA(MM) = PCARRAY(MM) + DELTA*(PGAMMA(MM) - PGAMMA
1(MM)) / X/MM + JD
XBETA(MM) = PBETA(MM) + DELTA*(PBETA(MM) - PBETA
1(MM)) / X/MM + JD
YDELTAN(MM) = PDELTAN(MM) + DELTA*(PDELTAN(MM) - PI)*DELTAN
1(MM)) / DOX(MM + JD)
FX(MM) = RX(MM) * WX(MM) * COSF(XGAMMA(MM))
DO 660 CC = 1, MM - 1
FX(M) = AR(M)*WM(M)*COS(PGAMMA(M))
660 CONTINUE
CC = 0.
I = 1
606 IC = I + 2
IF (IC-MM) 601, 607, 602
607 AA = FX(I)
X1 = DX(I + 1)
X2 = X1 + DX(I + 2)
PR = (X2*X2*FX(I+1) - X1*X1*FX(I+2) - AA*(X2**2 - X1**2))
/((X1*X2*X2 - X2*X1*X1)
CC = (X2*FX(I+1) - FX(I)) - X1*(FX(I+2) - FX(I)))/
1*(X1*X2*X2 - X2*X1*X1)
XAX = AX(I+2) + DELTA*X
DQ = (AA*(AXAX - AX(I)) + PR*(XAX**2 - AX(I)**2))/2.
1 + CC*(XAX**3 - AX(I)**3)/3.)))/144.
601 AA = FX(I)
X1 = DX(I + 1)
X2 = X1 + DX(I + 2)
PR = (X2*X2*FX(I+1) - X1*X1*FX(I+2) - AA*(X2**2 - X1**2))
/((X1*X2*X2 - X2*X1*X1)
CC = (X2*FX(I+1) - FX(I)) - X1*(FX(I+2) - FX(I)))/
1*(X1*X2*X2 - X2*X1*X1)
DQ = (AA*(AXAX - AX(I)) + PR*(AXI+2)**2 - AX(I)**2))/2.
1 + CC*(AXI+2)**3 - AX(I)**3)/3.)))/144.
GO TO 606
602 AA = FX(I)
XY = DX(I + 1) + DELTA*X
R = (FX(I+1) - FX(I))/XY
CC = (AXAX + PR*(AXAX + DELTA*X - AX(I))**2)/2.
GO TO 605
603 CC = CC + IC + 6, 83, 18
IF (IC-MM) 604, 605, 607
604 IC = I + 2
GO TO 606
605 CONTINUE
END
END
PROGRAM BLADE

VARIABLE NAMES

<table>
<thead>
<tr>
<th>Name</th>
<th>Equivalent to</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>DELN</td>
<td>(\Delta N)</td>
<td>in.</td>
</tr>
<tr>
<td>DWCO</td>
<td>(DW_{\text{coef}})</td>
<td></td>
</tr>
<tr>
<td>DWFUNC</td>
<td>(DW_{\text{func}})</td>
<td></td>
</tr>
<tr>
<td>DDM</td>
<td>(d(DW_{\text{func}})/dm)</td>
<td></td>
</tr>
<tr>
<td>W</td>
<td>(W)</td>
<td>ft./sec.</td>
</tr>
<tr>
<td>WDEL</td>
<td>(\Delta W)</td>
<td>ft./sec.</td>
</tr>
<tr>
<td>WSUC</td>
<td>(W_s)</td>
<td>ft./sec.</td>
</tr>
<tr>
<td>WPRESS</td>
<td>(W_p)</td>
<td></td>
</tr>
</tbody>
</table>

INDEX NAMES

MO = Number of streamlines
NMAX = Maximum number of data points
NN = Number of data point on a streamline
Program BLADE

Read Input

Initialize:
Increment \( dN \)
No. of Increments \( NN \)

Calculate \( d(DW_{\text{func}}) \)
\( \frac{dm}{dm} \)

Calculate:
\( \Delta W \)
\( W_s \)
\( W_p \)

All Points on S.L.? No

All S.L.'s? No

END

144
PROGRAM BLADE

DIMENSION DWC0C(10,30),DWFUNC(1C,30), W(10,30), NN(10),
1 WDEL(10,30),WSUC(1C,3C),WPRESS(10,30),DELN(10), DDM(30)

READ 10,MO,NMAX
10 FORMAT(6I10)
READ 10, (NN(M), M=1,NC)
READ 20, (DELN(M), M=1,MC)
20 FORMAT(6F10.0)
READ 20, ((DWC0C(M,N), N=1,NMAX), M=1,MO)
READ 20, ((DWFUNC(M,N), N=1,NMAX), M=1,MO)
READ 20, ((W(M,N), N=1,NMAX), M=1,MO)
DO 30 M=1,MO
30 FORMAT(40)
PRINT 40
40 FORMAT(1H1//////////25X9H TABLE ///21X
118H VELOCITY PROFILE ///)
PRINT 50, M
50 FORMAT(16X,26H MERIDIONAL STREAMLINE NO.,12///)
PRINT 60
60 FORMAT(4H, M1C6X1 HW14X2 HDW8X9HW SUCTION4X1 CHW PRESSURE///)
DELTA = 12. * DELN(M)
NM = KN(M)
DO 30 N=1,NM
30 IF (N.NE.2) 41, 42
GO TO 45
42 NREM = NM-N
IF (NREM.NE.1) 43, 43
GO TO 45
44 CDN(M) = (DWFUNC(M,N-2)-DWFUNC(M,N+2)-8. * DWFUNC(M,N-1)) /DELTA
45 CONTINUE
X = DELN(M) * FLOATF(N-1)
WDEL(M,N) = DWC0C(M,N) * DDM(N)/24.
WSUC(M,N) = W(M,N) + WDEL(M,N)
WPRESS(M,N) = W(M,N) - WDEL(M,N)
PRINT 100, X, W(M,N), WDEL(M,N), WSUC(M,N), WPRESS(M,N)
100 CONTINUE
PRINT 70
70 FORMAT(1F6.2,1F14.4)
30 CONTINUE
PRINT 70
END