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The nuclear quadrupole resonance spectrum was discovered by Dehmelt and Krüger in 1949 and is used in solid state physics and structure chemistry. Nuclear quadrupole resonance was developed based on the following principles:

1. Electromagnetic characteristics of atomic nuclei. Nuclei possess the characteristic of self-spin. When the self-spin $I > 0$, a nuclear magnetic moment $\mu$ is developed. When $I > \frac{3}{2}$ an electric quadrupole moment is developed. The moment $Q$ induced by the nonspherical symmetrical distribution of positive charges in atomic nuclei is expressed by the following equation:

$$Q = \frac{1}{c} \int \rho(\vec{r}, r)(3 \cos^2 \varphi - 1)r^2 d\tau$$

$$= z(3z^2 - r^2)_{av}$$  \hspace{1cm} (1)

2. Energy levels and the corresponding energy of $Q$ in an inhomogeneous electric field. In an axially symmetric field

$$E_M = \frac{cqQ}{4I(2I - 1)} \left[ 3M^2 - I(I + 1) \right]$$  \hspace{1cm} (3)

where $q$ = electric field gradient at the nucleus, $cqQ$ = the coupling constant of nuclear quadrupole moment and $M_1 = I, I - 1, \ldots, -I - 1, -I$. If the induced frequency $\nu$ in an inhomogeneous field satisfies the condition

$$\hbar \nu = \Delta E = cqQ \left[ \frac{3}{4I(2I - 1)} \right] \left[ 2 |M_1| - 1 \right]$$  \hspace{1cm} (4)

transitions from one energy state to another will occur. If the energy state jumps to a higher level, it results in the production of nuclear quadrupole resonances.

3. Zeeman splitting theory. The introduction of an external magnetic field will lead to further splitting of the energy levels. The process is called Zeeman splitting. For simplicity, the energy of interaction of an axially symmetric quadrupole with an axially symmetric electric field gradient is expressed by

$$E_M = \frac{cqQ}{4I(2I - 1)} \left[ 3M^2 - I(I + 1) \right] + \frac{\hbar}{2\pi} M H \cos \varphi$$

The magnetic field in which Zeeman splitting takes place is around $10^2$ gauss with a corresponding increase in frequency of $10^2$ kc/sec. The frequency which satisfies $\Delta M = \pm 1$ at $M > \frac{1}{2}$ and $\pm M \leftrightarrow \pm (M + 1)$ is given as

$$\omega_M = \frac{3cqQ}{\hbar} \frac{1}{4I(2I - 1)} \left[ 2 |M| + 1 \right] \pm \hbar \rho \cos \varphi$$

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(4) Factors affecting the spectral line width of the nuclear quadrupole resonance spectrum are: (1) Static factors. The function of adjacent dipoles between resonance nuclei and nonresonance nuclei will cause splitting in the resonance spectra and will also induce self-spin resulting in further fine splitting. Internal strain and misalignment of the sample and imperfection in the crystal lattice will also increase the width of spectral lines. (2) Kinetic factors. Molecular torsion and rotation are the principal causes. The movement is the result of an interelectronic function between adjacent molecules and can be estimated by means of an infrared detector and a Raman spectrum. Molecular rotation will change the electric field gradient as expressed by the following equation: \[ q' = q \left( \frac{3 \cos^2 \theta - 1}{2} \right) \] which in turn will affect the resonance frequency by the amount \[ \omega_q = \omega_q \left( \frac{3 \cos^2 \theta - 1}{2} \right). \] The latter can be obtained from the resonance frequency-temperature curve. The installation for observation of nuclear quadrupole resonance spectra is similar to the equipment set up for nuclear magnetic resonance observations with the exception that a crystal field within a solid sample replaces the external magnetic field. The basic requirement is to regulate frequency changes and to record the resonance signals. The frequency ranges from a few kHz to 1000 kHz. Applications of the nuclear quadrupole resonance spectra are: (1) As a method of crystal analysis. Bray's papers point out that difference resonance spectra will show the existence of "unbalanced" atoms distributed in different parts of a crystal having varying electric field gradients. (2) As a method of ascertaining H bond formation in solids. Harry's experiment on Cl\textsubscript{35} showed that the nuclear quadrupole resonance spectra can be used to determine the formation of H bonds in compounds. (3) As a method of studying phase changes in solids. The processes of phase change in solids can be determined by the temperature change of the nuclear quadrupole spectra. (4) As a method of determining the ratios of nuclear quadrupole moments at different isotope effects. The relation between resonance frequencies is equivalent to the ratio of the nuclear quadrupole moments at different isotopic values. (5) As a method of studying the effects of radiation on matter. When solid matter is exposed to high energy radiations, changes will be induced in the electrons, free radicals, and unstable molecules resulting in the widening of resonance spectral lines. According to Monfils, the relationship satisfies the following equation:

\[ \frac{I}{I_0} \propto \exp^{-\lambda t}. \]

Here, \( I_0 \) and \( I \) are intensities of resonance spectra respectively before and after radiation, \( \lambda \) - the concentration of impurities, and \( \lambda_0 \) - the volumetric parameter relative to the amount of impurities. (6) As a method of studying the characteristics of chemical bonds. Since the electric field gradient can be calculated by the counting constant and asymmetrical parameters of the nuclear quadrupole resonance under given conditions, the distribution of electronic charge and the characteristics of chemical bonds within the molecule can also be determined. The transition of valence electron to \( q \) in atoms is shown as follows:

\[ q = \rho \sum \int |\psi|^2 \left( \frac{3 \cos \theta - 1}{2} \right) \, \text{d}r. \]
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where $\psi_i$ - the wave function of no. 1 p electron; $r_i$, $\varphi_i$, and $\theta_i$ - polar coordinates of no. 1 p electron. The $q$ value at atomic nucleus is determined by the degree of ionization, the degree of heterogeneity, and duplication of bond formation. (7) As a method of measuring internal stress of high polymers during processing operation. In 1960 Gutowsky successfully applied the nuclear quadrupole resonance method in measuring the internal stress of resins during vulcanization. Test results showed that this method excelled the optical and strain resistance methods. At present nuclear quadrupole resonance spectrum is confined to the study of solids. According to Sterzer and Beers, the method is also applicable to the study of highly viscous liquids. The article was written with the assistance of Professors T'ang Yu-ch'i (0781/2589/4381) and Chien Jen-yuan (6929/0086/0337). There are 8 figures and 10 tables. English language references are: T. P. Das, E. I. Haha, "Nuclear Quadrupole Resonance Spectroscopy" 1958; F. Sterzer and Y. Beers, Phys. Rev., 100, 1174 (1955); H. S. Gutowsky, J. Polymer. Sci., 143, 143 (1960); P. L. Bray, Bull. Amer. Phys., 1 (2), 323 (1956).