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Monthly Progress Report

HERO SUPPORTING STUDIES

by

Norman P. Faunce
Paul F. Mohrbach

October 1 to October 31, 1962

Prepared for

U. S. NAVAL WEAPONS LABORATORY
Dahlgren, Virginia

Contract No. N178-8102

THE FRANKLIN INSTITUTE
LABORATORIES FOR RESEARCH AND DEVELOPMENT
PHILADELPHIA PENNSYLVANIA
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ABSTRACT

Preliminary evaluations of protected MARK 7 MOD 0 ignition element plug assemblies indicate losses of 1.43 and 3 db respectively at 80 and 200 mc. These estimates are derived from analysing the component as an equivalent symmetrical T-network; the parameters of the network are derived from measurements of open and short circuit input impedance. Though the resulting estimates appear high, the method warrants further study.

A constant current functioning test of this element shows it to be more sensitive than its unprotected counterpart; it requires only 7.8 amperes compared to 9.2 amperes @ 0.1 msec for 50% functioning. Dynamic resistance which ranges from 55 ohms/second at 3 amperes input to 956 ohm/second at 10 amperes was determined also for the protected MARK 7 element. Its thermal time constant was found to be 11.6 msec.

Additional investigations into means for measuring power to the base of an arbitrary termination proceeded along the line of comparing differential power measurements to measurements derived from detecting the maximum and minimum voltages on a slotted line preceding the load. This latter technique, called the voltage min-max method, appears to be superior to any new technique tried to date.
SUMMARY

Impedance measurements made of the input to the protected
MARK 7 MOD 0 plug assembly have been continued. From determinations
of this impedance with the bridge side of the assembly first shorted
and then opened we obtain data to specify a symmetrical T-network model
of the unit. Including the bridge wire terminations as a pure resistance
(reasonably valid up to 200 mc) we then compute the theoretical terminated
loss. Results indicate essentially no loss up to 30 mc, but at 80 mc
we predict 1.43 db loss and at 200 mc it appears to be 3.0 db. Compared
to the predicted attenuation based upon the lossy material's characteristics these estimates are high. However, we seem to have hit close
enough to warrant additional investigation.

A constant current test was performed with a pulse of 0.1
millisecond duration. For 50% probability of functioning, according to
these test results, only 7.8 amperes are necessary. This indicates the
protected MARK 7 to be more sensitive than the standard, which requires
9.21 amperes for the same response. Measurements were made of the
quantity, dr/dt for the protected plug. At 3 amperes the rate of change
of resistance with time is 55 ohms/per second, over intervals of about
816 microsecond or less. At the other extreme, 10 amperes, the resistance
change with time is 956 ohm/per second, valid under 123 microsecond.
Values between these test endpoints are almost linearly dispersed.
The thermal time constant was determined for this unit and found to be
11.6 millisecond on the average. This is the time for the bridgewire
temperature to drop to 36.8% of its initial value.

Additional studies of better means to measure power to the
base of an arbitrary termination now involve comparing two likely
methods. The differential power method discussed in the previous report
is compared with a new approach, the voltage min-max method. In this
latter method a calibrated voltage probe is used with a slotted line to
determine the maximum and minimum voltage in the line. With these data
and knowledge of the characteristic impedance of the line we readily
determine power from the expression,

\[ P = \frac{V_{\text{max}} - V_{\text{min}}}{Z_0} \]

With the MARK 1 MOD 0 Squib as termination, it appears that
this new method has great possibilities. From the data, we have determined
the loss introduced by the directional coupler to be about 1 db at 3000
mc, and the loss in the base of the plug about 12 db. Using the slotted
line permits the power to be determined at a number of points in the
systems, which may prove valuable in estimating system losses when they
become more significant.
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1. COMPONENT TESTING

Initially, impedance measurements were considered for the primary purpose of specifying the reflection coefficient to be expected when the protected elements were mounted at the end of a 50-ohm transmission line. This information collected last month would give us insight into the problem we might expect in measuring power while performing RF sensitivity evaluations. Work performed this period indicates that we might be able to deduce an estimate of probable firing sensitivity from additional impedance data collected on a minimum number of items.

This period we conducted most of the dc evaluations outlined for the protected MARK 7 MOD 0 ignition element: a constant current test at 0.1 msecond, evaluation of dr/dt and, in addition, determination of thermal time constant. The remaining dc evaluation, a long-time exposure to a non-initiating pulse followed by a dc test to determine if sensitivity is altered, will be conducted when the companion RF test is scheduled.

1.1 RF Evaluation of Protected MARK 7 MOD 0 Ignition Element; Impedance Study

Last month we measured the input impedance of a number of protected MARK 7 MOD 0 ignition elements. These data were collected at a number of frequencies and included measurements on both complete units and bridged plug assemblies. Results indicated that the impedance of the total item was duplicated by the impedance of the plug only, at least up to a frequency of 500 Mc.

While determining these impedances we conceived the idea that we might, by making additional measurements, collect data from which we could predict the RF loss for the assembly. Consequently, we now propose that the plug be represented as an equivalent T-network, in
which form we can calculate the ratio of power dissipated in the plug to that dissipated in the bridge wire.

Any unknown network can be represented as an equivalent T; the transformations of measurements are given in Figure 1-1. Because of its geometry we might best characterize the protected MARK 7 plug as a non-symmetrical T-network. However, to minimize the effort initially we assumed it to be symmetrical. Accordingly, we determined the input impedance of two separate plug assemblies with their outputs alternately open and shorted. Using average values from these measurements we determined the equivalent T network impedances. These data are all included in Table 1-1. The input impedance of the bridge plug (average of 5 units) is also included for comparison.

Assuming the network to be terminated by a 1 ohm bridge wire we computed the ratio of power dissipated in the termination to power dissipated in the total assembly (total power input). The values in Table 1-1 labelled base loss are equal to ten times the logarithm (base 10) of this power ratio. The two results of greater than zero magnitude are plotted in Figure 1-2, which includes a point of 5.73 db at 500 Mc representing the average attenuation evaluated for this lot of protected elements during their development.

These three data points appear to define a straight line. Had the slope of this line been 53° we would have reason to be exceedingly optimistic about the technique used to obtain the data; 53° is the slope of the attenuation-frequency characteristic determined for the attenuating material used in the protected plug development.

The fact that we determined terminated power loss from these data would account in some measure for the seemingly high loss values. By extrapolating the curve we would predict a value of about 0.65 db at 30 Mc; our calculations indicated the loss at this frequency to be exceedingly low, nearly zero. Because of these inconsistencies we must
Non-Symmetrical

<table>
<thead>
<tr>
<th>$Z_1$</th>
<th>$Z_{110} - Z_2$</th>
<th>$Z_{110} - Z_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z_2$</td>
<td>$\sqrt{Z_{110}(Z_{220} - Z_{22S})}$</td>
<td>$\sqrt{(Z_{110})^2 - Z_{110}Z_{11S}}$</td>
</tr>
<tr>
<td></td>
<td>$\sqrt{Z_{220}(Z_{110} - Z_{11S})}$</td>
<td>$\sqrt{(Z_{220})^2 - Z_{220}Z_{22S}}$</td>
</tr>
<tr>
<td>$Z_3$</td>
<td>$Z_{220} - Z_2$</td>
<td>$Z_{110} - Z_2$</td>
</tr>
</tbody>
</table>

Symmetrical

| $Z_{110} = Z_{11}$ with 2-2 open; $Z_{11S} = Z_{11}$ with 2-2 shorted |
| $Z_{220} = Z_{22}$ with 1-1 open; $Z_{22S} = Z_{22}$ with 1-1 shorted |

**FIG. 1-1** "T" NETWORK MODEL OF UNKNOWN NETWORK
Table 1-1

IMPEDANCE MODEL AND BASE LOSS DETERMINED FOR PROTECTED MARK 7 MOD 0 PLUG

<table>
<thead>
<tr>
<th>Frequency (mc)</th>
<th>$Z_{in}$</th>
<th>$Z_{oc}$</th>
<th>$Z_{se}$</th>
<th>$Z_1$</th>
<th>$Z_2$</th>
<th>Base Loss (db)</th>
</tr>
</thead>
<tbody>
<tr>
<td>3</td>
<td>0.98+j0</td>
<td>102-j66.7</td>
<td>0.30</td>
<td>~0</td>
<td>97-j66.7</td>
<td>0</td>
</tr>
<tr>
<td>7.6</td>
<td>0.95+j0.39</td>
<td>49-j65.8</td>
<td>0+j0.6</td>
<td>~0</td>
<td>49-j65.6</td>
<td>0</td>
</tr>
<tr>
<td>30</td>
<td>0.98+j1.3</td>
<td>11.8-j28</td>
<td>0+j1.2</td>
<td>0.01+j0.6</td>
<td>11.8-j28.6</td>
<td>0</td>
</tr>
<tr>
<td>80</td>
<td>2.0+j5.0</td>
<td>4.3-j15</td>
<td>1.0+j4.5</td>
<td>0.4+j2.2</td>
<td>3.9-j17.2</td>
<td>1.43</td>
</tr>
<tr>
<td>200</td>
<td>6.0+j6.5</td>
<td>3.0-j14.5</td>
<td>3.0+j6.5</td>
<td>0.7+j2.86</td>
<td>3.4-j7.16</td>
<td>3.0</td>
</tr>
</tbody>
</table>
FIG.1-2. BASE LOSS OF PROTECTED MARK 7 MOD 0 IGNITION ELEMENT.
be doubtful of the reliability of this technique. However, since we seem to have missed by such a relatively narrow margin it seems advisable to make another trial. During the next period we will re-appraise this technique giving thought to the merits of describing the non-symmetrical model.

1.2 DC Evaluation of Protected MARK 7 MOD 0 Ignition Element

1.2.1 Constant Current Test at 0.1 millisecond

When the RF protected lot of MARK 7 MOD 0 ignition elements was produced in late 1959 two constant current evaluation tests were performed. At that time, it was intended to show that the protected plug with its low dc resistance would not seriously alter normal functioning of the completed ignition element. The shortest time used was 1.0 millisecond. We have completed an additional constant current test during this period using a pulse of 0.1 millisecond. The data sheet for this test is appended. Results are given in Table 1-2 contrasted to similar data for the unprotected (standard) ignition element. These data show that the incorporation of the attenuator has not adversely altered the items normal functioning sensitivity.

<table>
<thead>
<tr>
<th>Current for 50% Firing Prob: (amps)</th>
<th>Std. Dev. (log units)</th>
<th>Pulse Dura. (log units)</th>
<th>Sample Size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Protected 7.807</td>
<td>.89249</td>
<td>.01357</td>
<td>0.100</td>
</tr>
<tr>
<td>Unprotected 9.21</td>
<td>0.96412</td>
<td>.0164</td>
<td>0.100</td>
</tr>
<tr>
<td>(Standard)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 1-2

CONSTANT CURRENT SENSITIVITY (0.1 MILLISECOND) OF PROTECTED AND STANDARD MARK 7 MOD 0 IGNITION ELEMENT
1.2.2 Dynamic Resistance

Dynamic resistance characteristics of the protected MARK 7 were determined by passing constant current through the bridge wire and recording the voltage across the bridge as a function of time. These measurements, for input currents of from 3 to 10 amperes, are summarized in Table 1-3. Variation of $\frac{dr}{dt}$ with current is shown in Figure 1-3. When using these data in computing resistance, it is recommended that exposure time ($\Delta T$) be not longer than that indicated by the time curve included in Figure 1-3. Extrapolation for longer intervals will tend to show higher resistance than the true value since it does not take into account the cooling effect of the bridgewire environment.

Figure 1-4 depicts a typical trace of voltage vs. time due to a current through the bridge wire on which measurements of dynamic resistance were made.

1.2.3 Thermal Time Constant

The thermal time constant is defined as the time required for the bridgewire temperature to decay to 36.8% of the maximum temperature excursion after application of an input stimulus that does not cause the item to explode.

The thermal time constant of the protected MARK 7 was determined in the following manner. A current whose magnitude was small enough not to cause appreciable changes in the bridgewire and its environment was passed continuously through the bridgewire of the device before, during, and after application of a large current pulse of short duration (7 amperes for 100 $\mu$s). The monitoring current was held constant by the inclusion of a large current limiting resistor.

Since the monitoring current was constant, it was possible to use the potential across the bridgewire (observed with an oscilloscope) as a measure of the instantaneous value of resistance as the item cooled after application of the relatively large current pulse.
Table 1-3

DYNAMIC RESISTANCE MEASUREMENTS OF THE PROTECTED MARK 7 MOD 0 IGNITION ELEMENT

<table>
<thead>
<tr>
<th>Item No.</th>
<th>Input Current (amps)</th>
<th>Resistance Change ΔR (ohms)</th>
<th>Time interval at Resistance Change Δt (μ sec)</th>
<th>ΔR ohms/sec</th>
<th>Δt μ sec</th>
<th>(Averages)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>.047</td>
<td>910</td>
<td>52</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>.083</td>
<td>870</td>
<td>95</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>.067</td>
<td>800</td>
<td>84</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>3.0</td>
<td>.037</td>
<td>970</td>
<td>38</td>
<td>55</td>
<td>816</td>
</tr>
<tr>
<td>5</td>
<td>.015</td>
<td>360</td>
<td>42</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>.027</td>
<td>900</td>
<td>30</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>.039</td>
<td>900</td>
<td>43</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>.080</td>
<td>370</td>
<td>216</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>.060</td>
<td>360</td>
<td>167</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>10</td>
<td>.080</td>
<td>420</td>
<td>190</td>
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<tr>
<td>11</td>
<td>5.0</td>
<td>.080</td>
<td>380</td>
<td>211</td>
<td>217</td>
<td>382</td>
</tr>
<tr>
<td>12</td>
<td>.080</td>
<td>360</td>
<td>222</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>13</td>
<td>.100</td>
<td>400</td>
<td>250</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>14</td>
<td>.100</td>
<td>385</td>
<td>260</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>.080</td>
<td>380</td>
<td>222</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>16</td>
<td>.130</td>
<td>172</td>
<td>756</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>17</td>
<td>.100</td>
<td>176</td>
<td>568</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>18</td>
<td>7.5</td>
<td>.093</td>
<td>160</td>
<td>581</td>
<td>582</td>
<td>158</td>
</tr>
<tr>
<td>19</td>
<td>.069</td>
<td>160</td>
<td>431</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>.069</td>
<td>120</td>
<td>575</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>21</td>
<td>.110</td>
<td>140</td>
<td>917</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>22</td>
<td>.110</td>
<td>110</td>
<td>1000</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>23</td>
<td>10.0</td>
<td>.115</td>
<td>112</td>
<td>1027</td>
<td>956</td>
<td>123</td>
</tr>
<tr>
<td>24</td>
<td>.120</td>
<td>132</td>
<td>909</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>25</td>
<td>.130</td>
<td>140</td>
<td>929</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
**Figure 1-3.** Dynamic Resistance of Protected Mark 7 MQZO Ignition Element

(Under Quasi Adiabatic Conditions)
A typical oscillogram is shown in Fig. 1-5. The circuit used for these measurements is given in Fig. 1-6. Results of these tests appear in Table 1-4. Values range from 8.5 to 14.0 milliseconds, the grand average being 11.6.
Table 1-4

THERMAL TIME CONSTANT OF PROTECTED MARK 7 MOD 0 IGNITION ELEMENT

<table>
<thead>
<tr>
<th>Item No.</th>
<th>Time Constant T (msec)</th>
<th>Ave</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(three readings)</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>11.8 10.8 11.5</td>
<td>11.4</td>
</tr>
<tr>
<td>2</td>
<td>14.0 13.0 12.5</td>
<td>13.2</td>
</tr>
<tr>
<td>3</td>
<td>12.0 11.0 12.0</td>
<td>11.9</td>
</tr>
<tr>
<td>4</td>
<td>12.0 12.0 11.0</td>
<td>11.7</td>
</tr>
<tr>
<td>5</td>
<td>14.0 13.0 13.0</td>
<td>13.3</td>
</tr>
<tr>
<td>6</td>
<td>9.0 9.5 12.0</td>
<td>10.2</td>
</tr>
<tr>
<td>7</td>
<td>8.5 9.0 11.0</td>
<td>9.5</td>
</tr>
<tr>
<td>8</td>
<td>12.0 10.0 10.0</td>
<td>10.7</td>
</tr>
<tr>
<td>9</td>
<td>11.0 11.0 12.0</td>
<td>11.3</td>
</tr>
<tr>
<td>10</td>
<td>13.5 12.5 13.0</td>
<td>13.0</td>
</tr>
</tbody>
</table>

Grand Average 11.6

2. COMPONENT DEVELOPMENT

No work has been done on this phase during this period.

3. INSTRUMENTATION-POWER MEASUREMENTS BY VU, RANGE PROBE TECHNIQUE

Experimental results of our first attempt at evaluation of a differential power measurement technique, at 3 and 10 Gc, were given in the previous report. The data obtained was not completely conclusive; and the work has been continued in the hope of resolving some of the conflicts appearing during the first tests.
We were fortunate in being able to combine into one experiment additional tests with the differential power technique and initial tests with a slotted transmission line and calibrated traveling probe. This slotted line and traveling probe technique, while generally known, is not a commonly used method for measuring net power to a load. Preliminary investigations have indicated that this method may be of greater value to our work than the differential power method.

3.1 Basis of Probe-in-Slotted Line Method

This technique is clearly outlined in section 3-88 of the "Handbook of Electronic Measurements,"(1). A part of the text is quoted:

"The power is also given by

\[ P = \frac{V_{\text{max}}}{Z_0} \cdot \frac{V_{\text{min}}}{S} = \frac{V_{\text{max}}^2}{S} \cdot \frac{S}{Z_0} \]

where \( V_{\text{max}} \) is the RMS voltage at a point of voltage maximum and \( V_{\text{min}} \) is the RMS voltage at a point of voltage minimum on the line.

\[ S = \frac{V_{\text{max}}}{V_{\text{min}}} \]

The probe may be calibrated with known powers into a matched load and then used to measure the pertinent quantities in this equation. The voltage calibration then includes the characteristic impedance of the line, and the equation may be directly applied to the measurement of power delivered to the load."

This discussion suggests procedures which are highly applicable in our present RF work. First, a method for calibrating a crystal probe

(1) Handbook of Electronic Measurements VOL. I, edited by Moe Wind; Polytechnic Institute of Brooklyn, Microwave Research Institute; Contract Nos. AF-30(602)-677 and AF-30(602)-1578. (Quotation from section 3-88).
as a true RMS volt meter is implied. Secondly, using this calibrated probe, the values of maximum and minimum voltage read at points a quarter-wavelength apart on the line may be combined with the known characteristic impedance of the slotted line to obtain the net power toward the load. However, the effective point of measurement will still be some distance from the load. Under the most ideal conditions the first point of measurement is expected to be a voltage maximum approximately 1/4 wavelength away from the load and the companion measurement will occur at an additional 1/4 wavelength distance. However, we envision refinements which will allow us to estimate the power lost in the sections of transmission line between the load and the point where we effectively measure power. This will permit us to quote powers at the base of the termination, independent of systems losses.

3.1.1 Voltage Calibration of the Slotted Line Probe

We experienced no particular difficulties in calibrating the crystal probe in the carriage of a Hewlett-Packard 805A slotted line at 3 Gc. A Hewlett-Packard 434A calorimeter was an ideal self-indicating termination for the slotted line. Figure 3-1 is a block diagram of the requirements for the calibration.

With a fixed power output from the generator we record the microvolt meter reading and calorimeter indication. Since the calorimeter is 50 ohms and is terminating a 50 ohm system we expect a flat line. Actually there was a small residual VSWR, therefore for each power setting we recorded both the maximum and minimum voltage along the slotted line. For a flat lossless line the voltage (V) everywhere along it is related to the power (P) dissipated in the termination (R) by

\[ V = \sqrt{PR}. \]
We computed the value of the radical for the various power levels at which we recorded data and assigned this new value to the voltmeter reading. In this manner we obtained the calibration shown in Figure 3-2. Because of the residual VSWR we obtain two voltages for each power; the calibration curve is drawn as a visual average of the points.

3.1.2 Measurements of Power by Voltage "Min-Max" Method

With the travelling probe calibrated as described in this preceding paragraph, we are prepared to measure power for any arbitrary termination. Actually, the power measured in this manner is the power flowing toward the termination at a point in the transmission system located between the points of measurement. Working at 3000 Mc with a MARK 1 MOD 0 as termination, we found that we could obtain three voltage minimums and maximums alternately spaced along the slotted line. Thus we may determine the power flow at three equally spaced points along the line. If the line is relatively lossy we should note a significant difference between power measured at these points, decreasing as we approach the load. If they show little difference we
FIG 3-8 VOLTAGE POWER CALIBRATION
(Calendar meter as Load - 3000 Mc)
may assume the system to be relatively lossless, and the power flowing in the line should be the power dissipated in the termination.

A number of measurements were made by this technique and by the differential power method discussed last period. Details and results are given in the next section.

3.2 Differential Power and Voltage "Min-Max" Power Measurements Compared

With a MARK 1 MOD 0 squib plug as termination we endeavored to measure the power input to its base by both of the methods we have just discussed. So as to have a direct comparison of the two systems, we made both measurements simultaneously by placing the measuring equipment in series. Because each technique effectively measures the power flow at one point in the transmission line, the system placed farthest away from the load will indicate the power dissipated in the load plus the power absorbed by the other measuring system. In view of this we made two determinations, first with the dual directional coupler (differential power) nearest the load, then with the measurement systems interchanged. The two alternate system arrangements are shown in Figure 3-3, and the results are given in Tables 3-1 and 3-2.

For measurements of differential power the calibration procedure detailed in the previous month's report was used. The forward port output was found to give an indication of 9.44 mw per watt of main line forward power and the reflected port 9.62 mw/watt of reflected power. The calibration given in Figure 3-1 was used for reducing the voltage min-max data.

At 3000 Mc the slotted line was long enough to enable us to collect three pairs of min-max voltages, and we took full advantage of this condition. Since there did not appear to be any definite indication of a smooth decrease in power along the line we merely averaged the three results.
Figure 3-3: Equipment Arrangements for Power Measurements

(a) Directional Coupler Toward Load

(b) Slotted Line Toward Line
<table>
<thead>
<tr>
<th>Input Power (watts)</th>
<th>Minimum Reading</th>
<th>Maximum Reading</th>
<th>Voltage Min-Max Measurements</th>
<th>Differential Power Measurements</th>
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</thead>
<tbody>
<tr>
<td>2.7</td>
<td>4.4</td>
<td>4.4</td>
<td>7.36</td>
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<td>2.4</td>
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<td>1.9</td>
<td>3.32</td>
<td>3.75</td>
<td>8.37</td>
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<td>---------------------</td>
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<td>-----------------------</td>
<td>------------------------</td>
<td>-------------------------</td>
</tr>
<tr>
<td>2.8</td>
<td>54</td>
<td>5.08</td>
<td>28.5</td>
<td>2.45</td>
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<tr>
<td></td>
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<td></td>
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</tr>
<tr>
<td>2.4</td>
<td>47</td>
<td>4.44</td>
<td>25.2</td>
<td>2.17</td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.9</td>
<td>38.5</td>
<td>3.63</td>
<td>21.0</td>
<td>1.81</td>
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<td>1.5</td>
<td>30.5</td>
<td>2.88</td>
<td>18.5</td>
<td>1.59</td>
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</tbody>
</table>
For ease in comparison we have extracted the essential data from the detailed tabulations and presented it in summary form in Table 3-3. The voltage min-max power measurement is the lower value of the two simultaneous determinations whether or not it is measured nearest the load. The differential power measurements seem to be constant for any one system input power without regard to this sequence of the equipment. This permits us to surmise that the slotted line is essentially lossless, and the dual directional coupler introduces about 20% loss, or roughly 1 db.

For a Clairex cell reading of 25, dc power to the bridge wire is about 150 mw. Assuming that 500 Mc power would produce nearly the same cell reading as dc, and further assuming the min-max power to be the actual power input to the device, we can estimate the base loss, which comes out to be about 11.7 db; using differential power we would predict a loss of about 12.6 db. It is interesting to note that these predictions differ by about 1 db, or the amount of loss associated with the dual directional coupler.

These results do not allow us to conclude that we have, in fact, measured the power to the base of the device unless we can assume the transition between the slotted line and the load to be lossless. Since our data indicate a relatively low VSWR (~8 to 10) we may be justified in making such an assumption. Nevertheless, we will explore other means to validate the technique. We will attempt its validation for the case of high VSWR and correspondingly high system losses. Toward this end we will examine the possibility of the voltage min-max method being usable at 1000 Mc to determine the power to the base of the MARK 1 MOD 0. Previous experiments suggest that the bridge wire at 1000 Mc, although the VSWR is on the order of 50.
Table 3-3
SUMMARY OF POWER MEASUREMENTS

<table>
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<tr>
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<table>
<thead>
<tr>
<th>Differential Power Min-Max Power</th>
<th>Voltage Min-Max Power</th>
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</thead>
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</tr>
<tr>
<td>2.4</td>
<td>2.27</td>
</tr>
<tr>
<td>1.9</td>
<td>1.81</td>
</tr>
<tr>
<td>1.5</td>
<td>1.27</td>
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ACKNOWLEDGEMENTS

Efforts of Raymond Raksnis and Kenneth Fertner for the impedance study and Victor Goldie, Michael Kelly and Philip McKeaney for the dc tests detailed in Section I are gratefully acknowledged. For the contents of Section 3 we are indebted to the efforts of John Warren and the consultations of George McKay.

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Group Leader

Norman P. Faunce
Project Leader

Approved by;

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Applied Physics Laboratory

Francis L. Jackson
Director of Laboratories
APPENDIX

CONSTANT CURRENT EVALUATION DATA

for

PROTECTED MARK 7 MOD 0 IGNITION ELEMENT

0.1 msec PULSE DURATION
<table>
<thead>
<tr>
<th>ITEM NO.</th>
<th>FUNCTIONING LEVELS (in %)</th>
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</thead>
<tbody>
<tr>
<td>1</td>
<td>X</td>
</tr>
<tr>
<td>2</td>
<td>X</td>
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<td>4</td>
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<tr>
<td>5</td>
<td>X</td>
</tr>
<tr>
<td>6</td>
<td>X</td>
</tr>
</tbody>
</table>

**Secondary Statistics**

- For "o":
  - \( A = \frac{N}{N} \)
- For "x":
  - \( A = \frac{N}{N} \)

**Primary Statistics**

- \( \sigma = \sqrt{\frac{N}{N}} \)
- \( c = \sqrt{\frac{N}{N}} \)
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